

# 1-loop effects of MSSM particles in Higgs productions at the ILC

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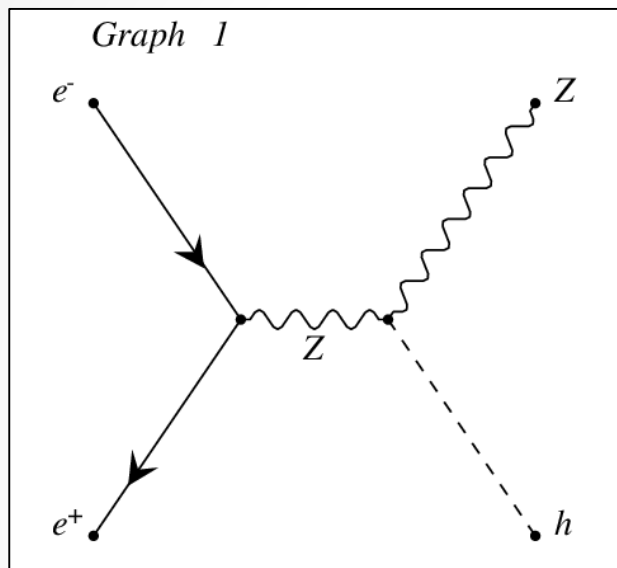


# OUTLINE

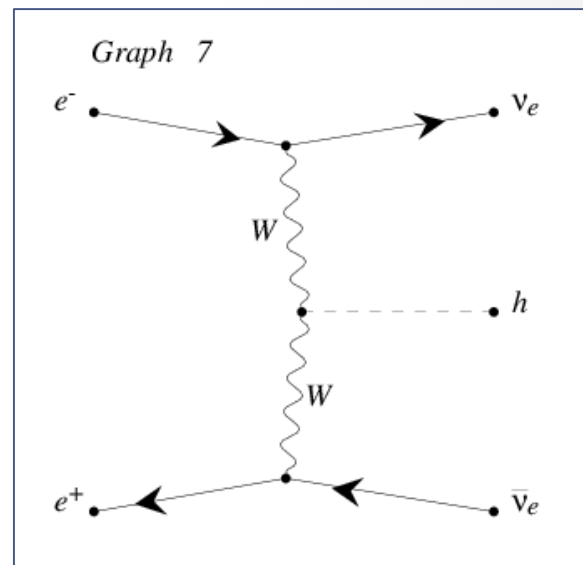
- Introduction(What)
- How(GRACE/SUSY)
- Results
- Summary

# Introduction

# SUSY indirect detection in Higgs production at the ILC

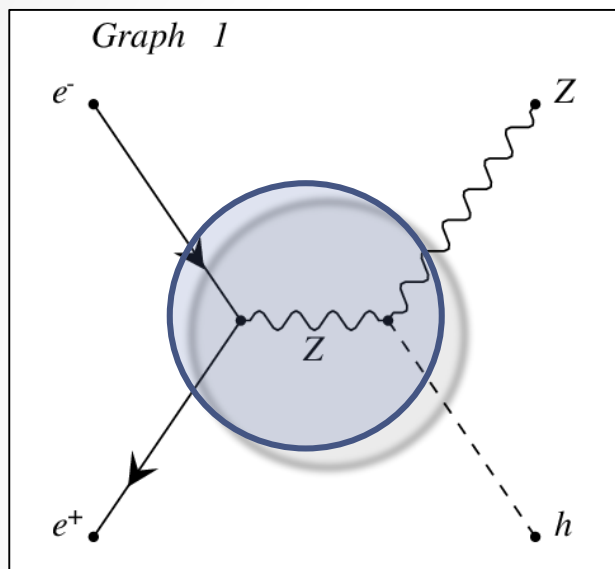


Zh production

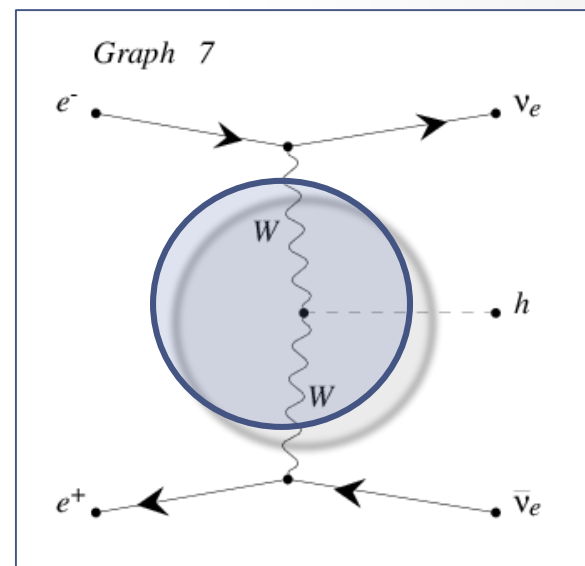


W fusion

# SUSY indirect detection in Higgs production at the ILC



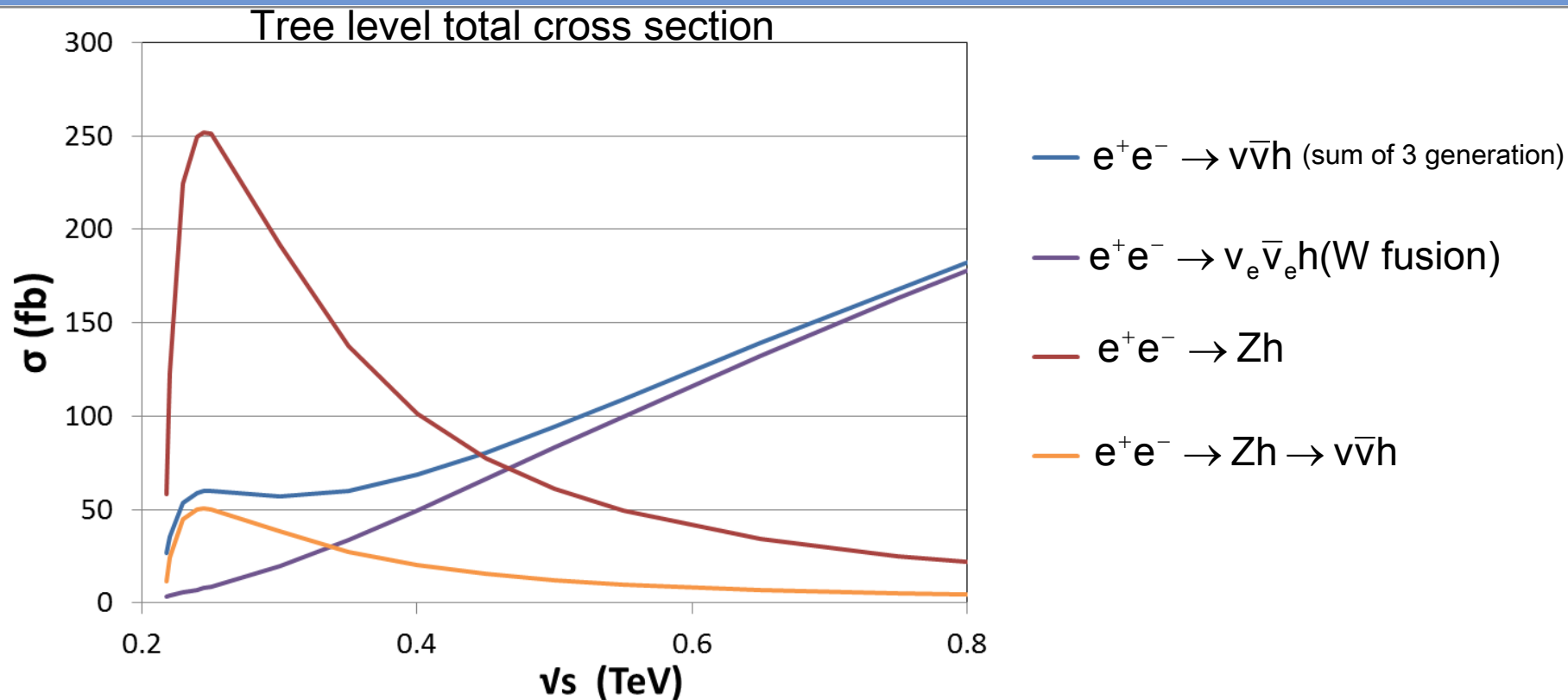
Zh production



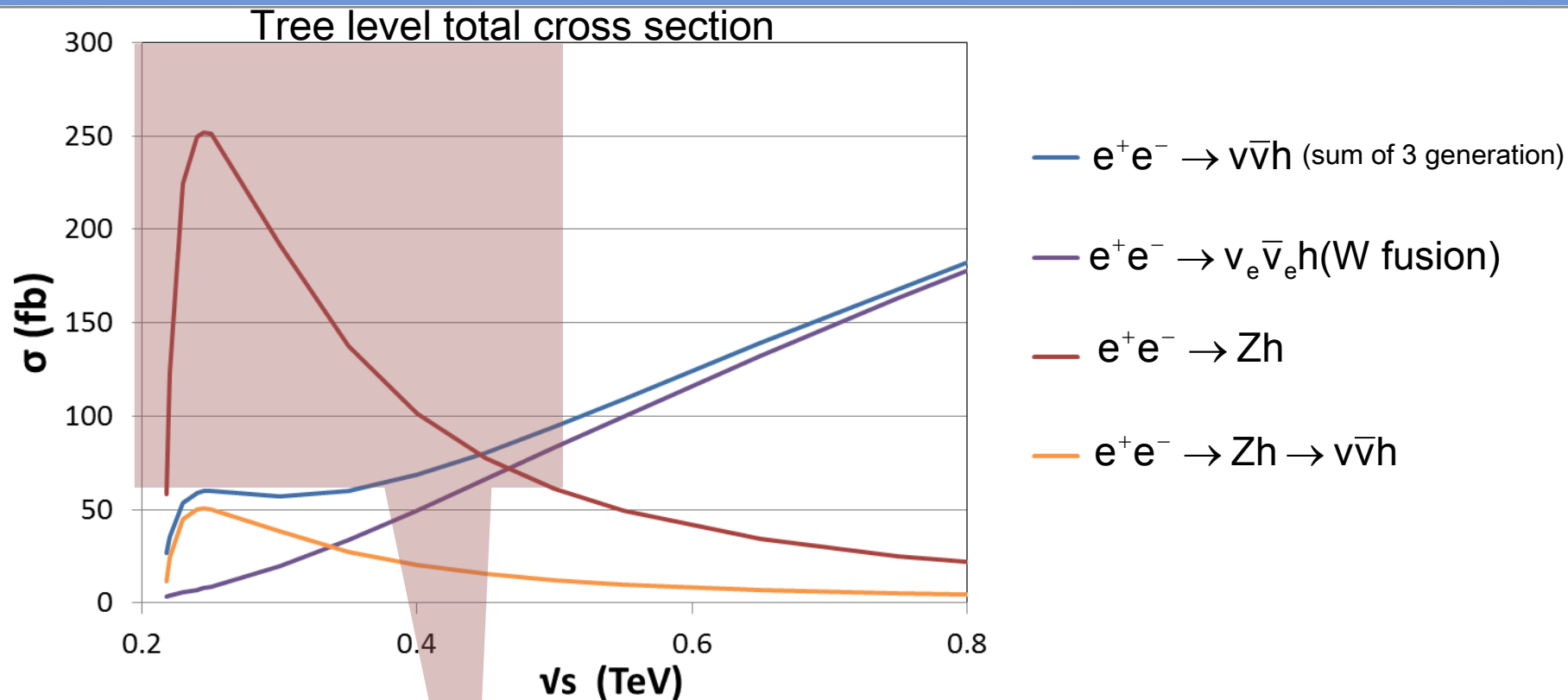
W fusion

Is the 1-loop effect of virtual MSSM particles statistically significant ?

# SUSY indirect detection in Higgs production at the ILC

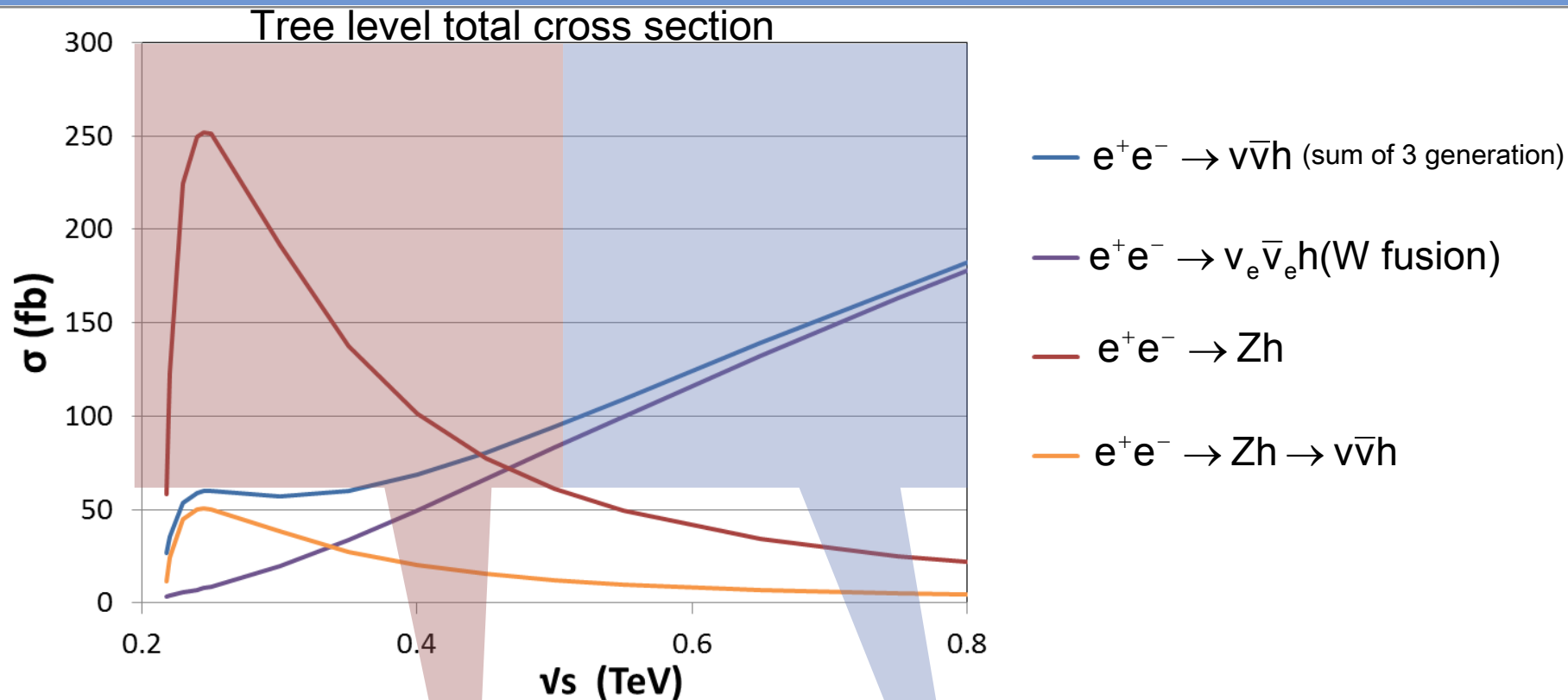


# SUSY indirect detection in Higgs production at the ILC



The cross section of  $Zh$  is large at low energy region

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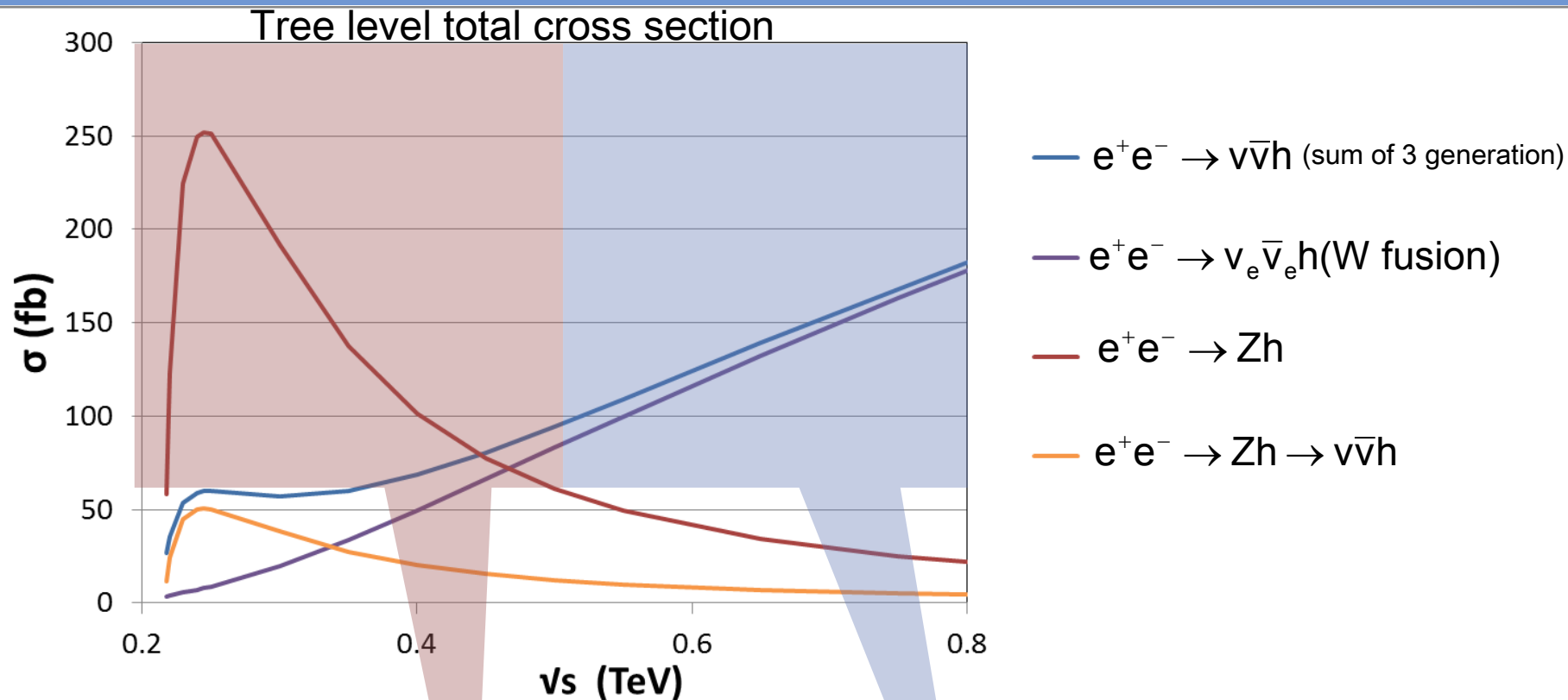


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The cross section of  $\nu\bar{\nu}h$  is large at high energy region



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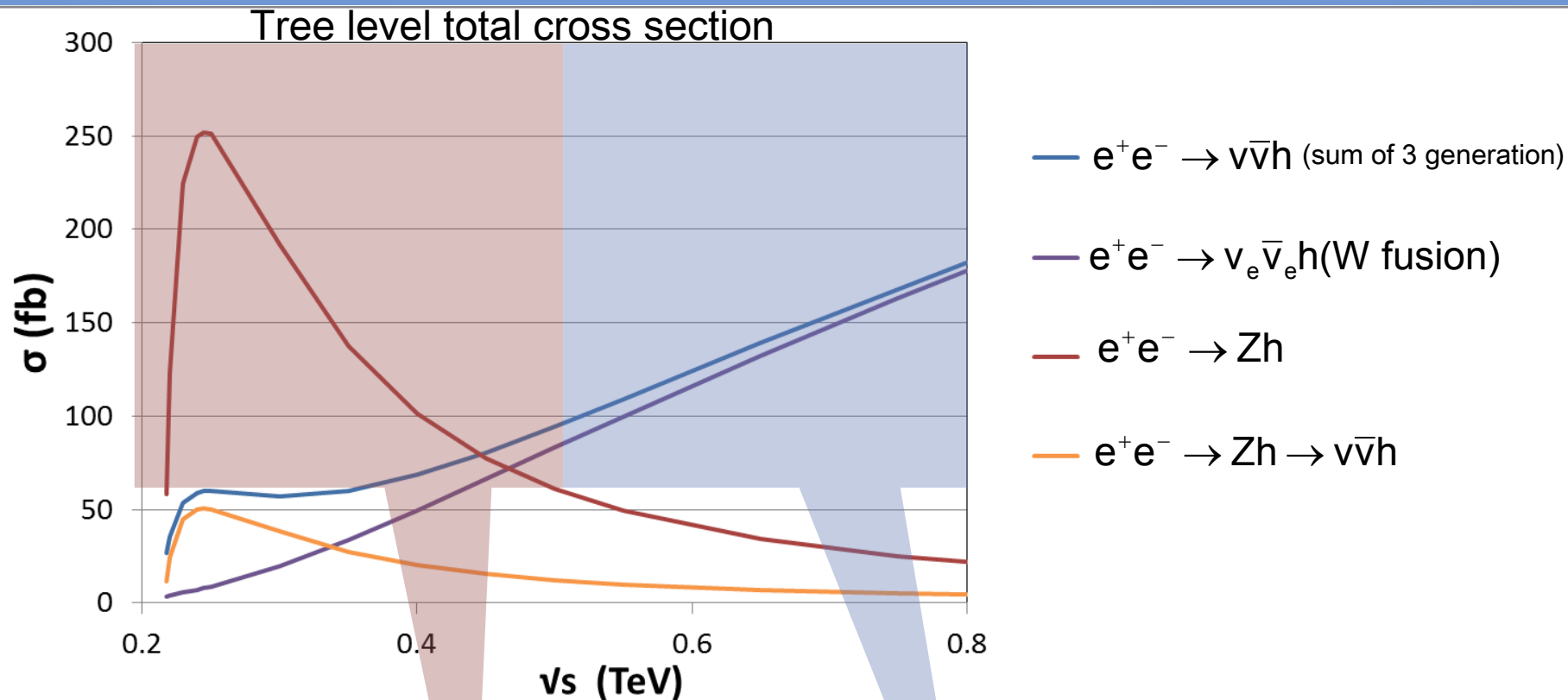


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The accurate measurement of SM Higgs is expected

# SUSY indirect detection in Higgs production at the ILC



The cross section of  $Zh$  is large at low energy region

The cross section of  $\nu\bar{\nu}h$  is large at high energy region

The accurate measurement of SM Higgs is expected

At the same time, We want to focus on the effect of MSSM

# Selection of sets (Zh)

we have taken into account

- Higgs mass ( $m_h(\text{exp})=125.09 \pm 0.24 \text{ GeV}$ )
- B physics constraint ( $b \rightarrow s\gamma, B_s \rightarrow \mu\mu$ )
- muon g-2 constraint 
 $a_\mu(\text{exp}) - a_\mu(\text{SM}) = (25.9 \pm 8.1) \times 10^{-10}$   
SuSpect2 (A.Djouadi, J.Kneur and G.Moultaka)
- DM thermal relic density 
 (Planck data of  $\Omega h^2$ )  
micrOMEGAs (G. Belanger, F. Boudjema, A. Pukhov, A. Semenov)
- LHC direct search of sparticles

	light stop $\cong 300\text{GeV}$	heavy stop $\cong 1000\text{GeV}$
The DM abundance is explained by Co-annihilation of stau and LSP	set <b>1</b>	set <b>2</b>
The DM abundance is explained by Co-annihilation of stop and LSP	set <b>3</b>	inconsistent with muon g-2 (LSP is too heavy)

# Selection of sets (W fusion)

Signal higgs + missing

SM

$$e^+e^- \rightarrow \nu\bar{\nu}h$$

MSSM

$$e^+e^- \rightarrow \tilde{\chi}_1^0\tilde{\chi}_1^0h$$

(This study does not focus on this)

We have selected the set  
neutralino pair is **not** produced.

$$(\tilde{\chi}_1^0 \geq 500\text{GeV})$$

We pay attention to the case

“**only** the effects of virtual MSSM  
particles are statistical significant”

# the set (W fusion)

Higgs (consistent with the observed mass)

ElectroWeak particles  
(Only these contribution don't explain muon g-2)

QCD particles

set 10			
h	H	A	H <sup>+</sup>
125.2	2000	2000	2002
$\tilde{\chi}_1^+$	$\tilde{\chi}_2^+$		
583.3	1376		
$\tilde{\chi}_1^0$	$\tilde{\chi}_2^0$	$\tilde{\chi}_3^0$	$\tilde{\chi}_4^0$
552.8	588.2	614.8	1376
$\tilde{\ell}_1$	$\tilde{\ell}_2$	$\tilde{\nu}_\ell$	
601.5	651.7	646.9	
$\tilde{\tau}_1$	$\tilde{\tau}_2$	$\tilde{\nu}_\tau$	
589.5	662.5	646.9	
$\tilde{u}_1$	$\tilde{u}_2$	$\tilde{d}_1$	$\tilde{d}_2$
5000	5000	4800	5000
$\tilde{t}_1$	$\tilde{t}_2$	$\tilde{b}_1$	$\tilde{b}_2$
1798	2508	2200	2501
$\theta_\tau$	$\theta_b$	$\theta_t$	
1.164	1.539	1.481	
$M_1$	$M_2$	$M_3$	
585.0	1370	2500	
$\mu=586, \tan \beta=30$			

- How (GRACE/SUSY)

(before and after the discovery of Higgs)

# GRACE/SUSY

☆ The system that can automatically calculate cross sections or decay widths in SM and MSSM

\* GRACE/SUSY [tree version (opened to public)]

Comput.Phys.Commun.153:106-134,2003 download : <http://minami-home.kek.jp/>

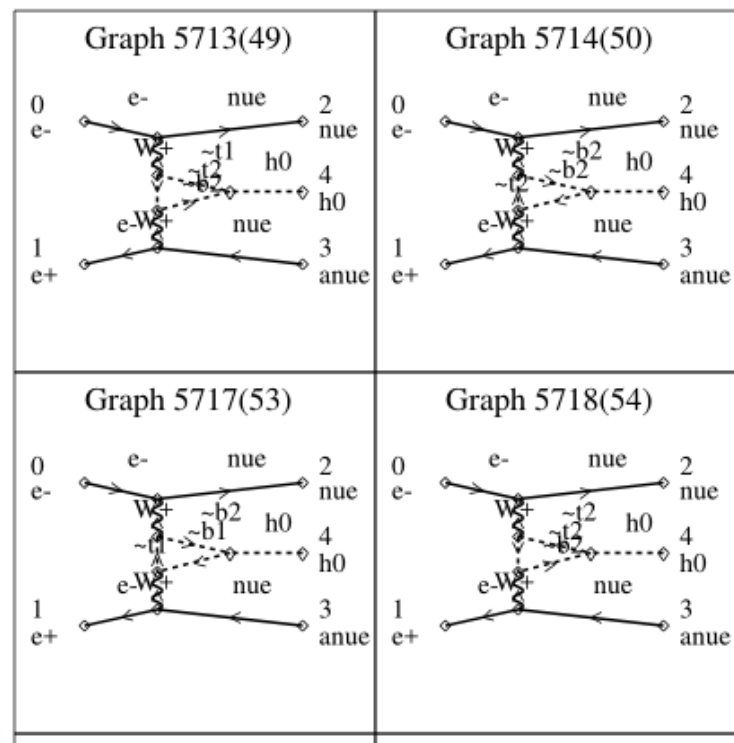
\* GRACE/SUSY-loop [1-loop version (unopened to public)]

Phys.Rev.D75:113002,2007

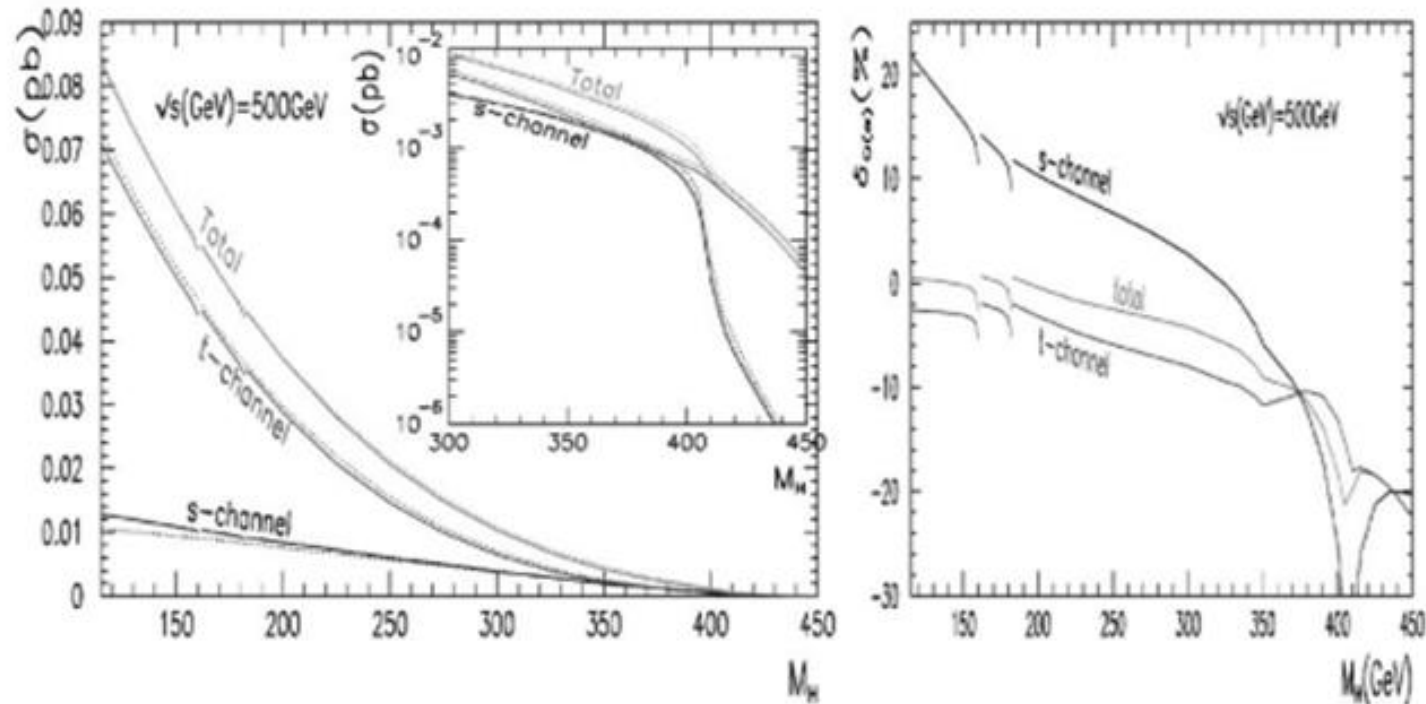
1. Feynman diagrams
2. Physical amplitudes
3. Phase space Integration
4. Event generation
5. Various Self-checks



We can check the validity of numerical calculation



# GRACE (before the discovery of higgs)



SM full 1-loop correction of  $e^+ e^- \rightarrow \nu\bar{\nu} h$  have calculated with using GRACE in 2003

G. Bélanger , F. Boudjema , J. Fujimoto , T. Ishikawa , T. Kaneko, K. Kato, Y. Shimizu, Physics Letters B 559 (2003) 252–262

Denner et al., NPB660(2003)289

Before the discovery of Higgs,  
GRACE have been used with Higgs mass as a free parameter.

- Higgs mass was final free parameter in SM.



# GRACE (after the discovery of Higgs)

After the discovery of Higgs, GRACE is used with Higgs mass as a fixed parameter for the search of MSSM that have many free parameters.  
For example, in this way,

step1, we can generate all diagrams.

$$e^+ e^- \rightarrow \nu_e \bar{\nu}_e h \text{ full 1-loop MSSM diagrams} \cdot \cdot \cdot 13793 \text{ diagrams}$$

step 2, we can select diagrams.

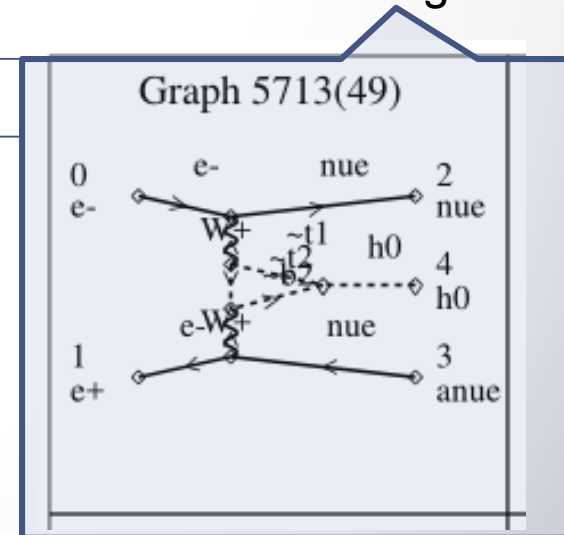
By selecting diagrams that WW fusion in internal line, they are reduced to 239 diagrams

step 3, we can check whether a renormalization works well.

we have confirmed(self- check)  
the cancelation of ultraviolet or infrared divergence

and

independence on the cut off energy between hard and soft photon



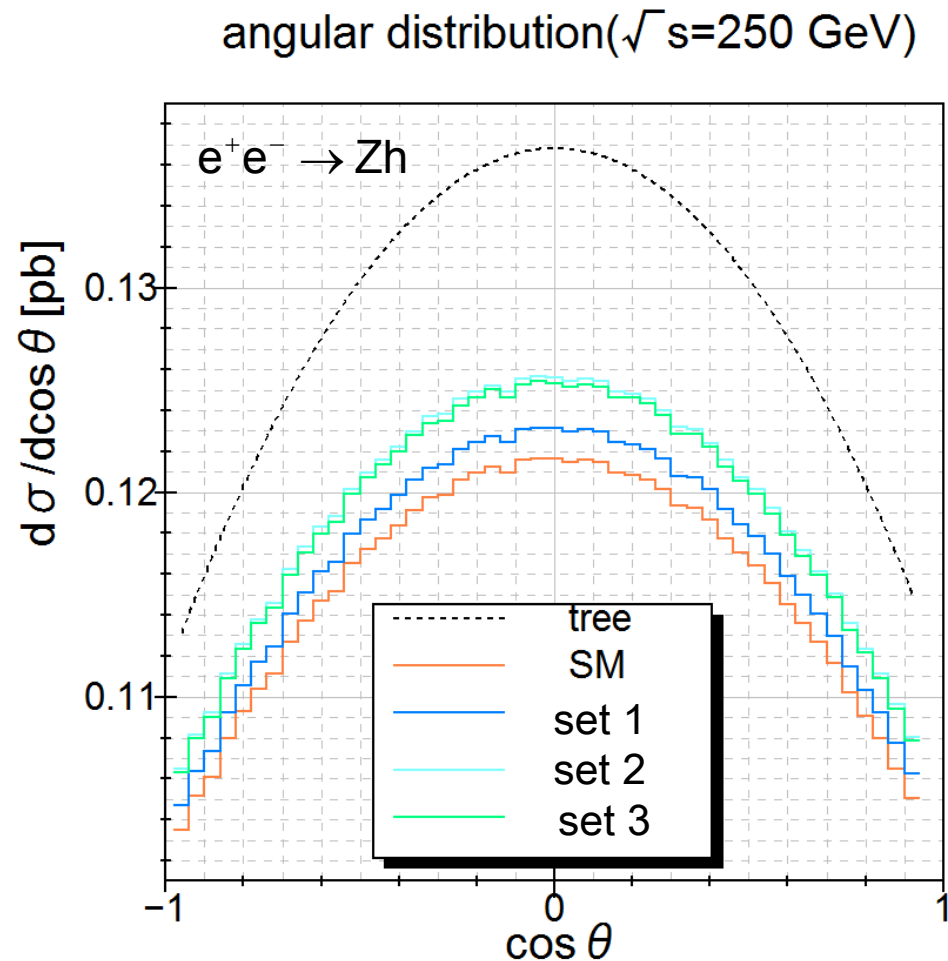
step 4, actual calculations

# Results

## (ZH,W fusion)

# Angular distribution(1-loop level)

- $\theta$  is the Z generation angle.
- The 1-loop correction for the tree level is negative.
- The correction of MSSM for SM is positive.



# MSSM 1-loop effect

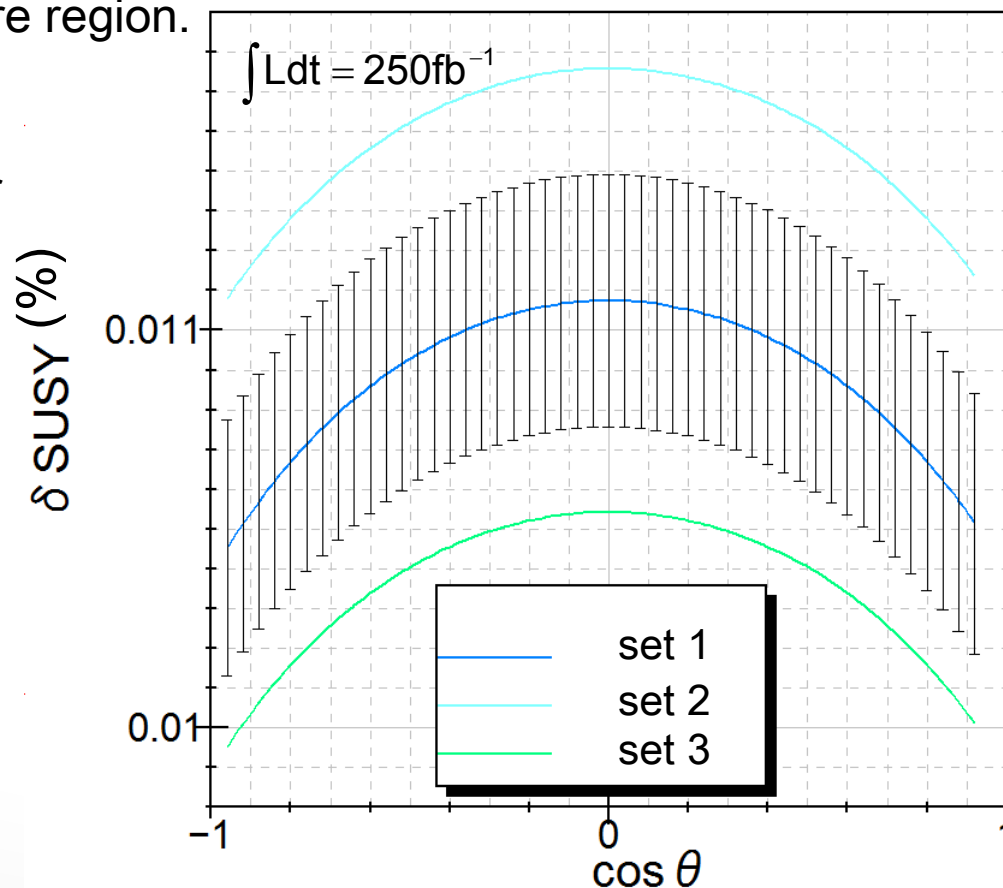
- We have defined the correction ratio  $\delta$
- We have compared with the statistical error (assumed the luminosity that planned in the ILC).

H.baer et al,  
The International Linear Collider Technical Design Report - Volume 2: Physics (2013)

- The 1-loop effect is 11% in the entire region.
- The 1-loop effect for SM is larger than the error.
- The difference among sets is larger than the error.

$$\delta_{\text{SUSY}} = \frac{\frac{d\sigma_{\text{SUSY1-loop}}}{d\cos\theta} - \frac{d\sigma_{\text{SM}}}{d\cos\theta}}{\frac{d\sigma_{\text{tree}}}{d\cos\theta}}$$

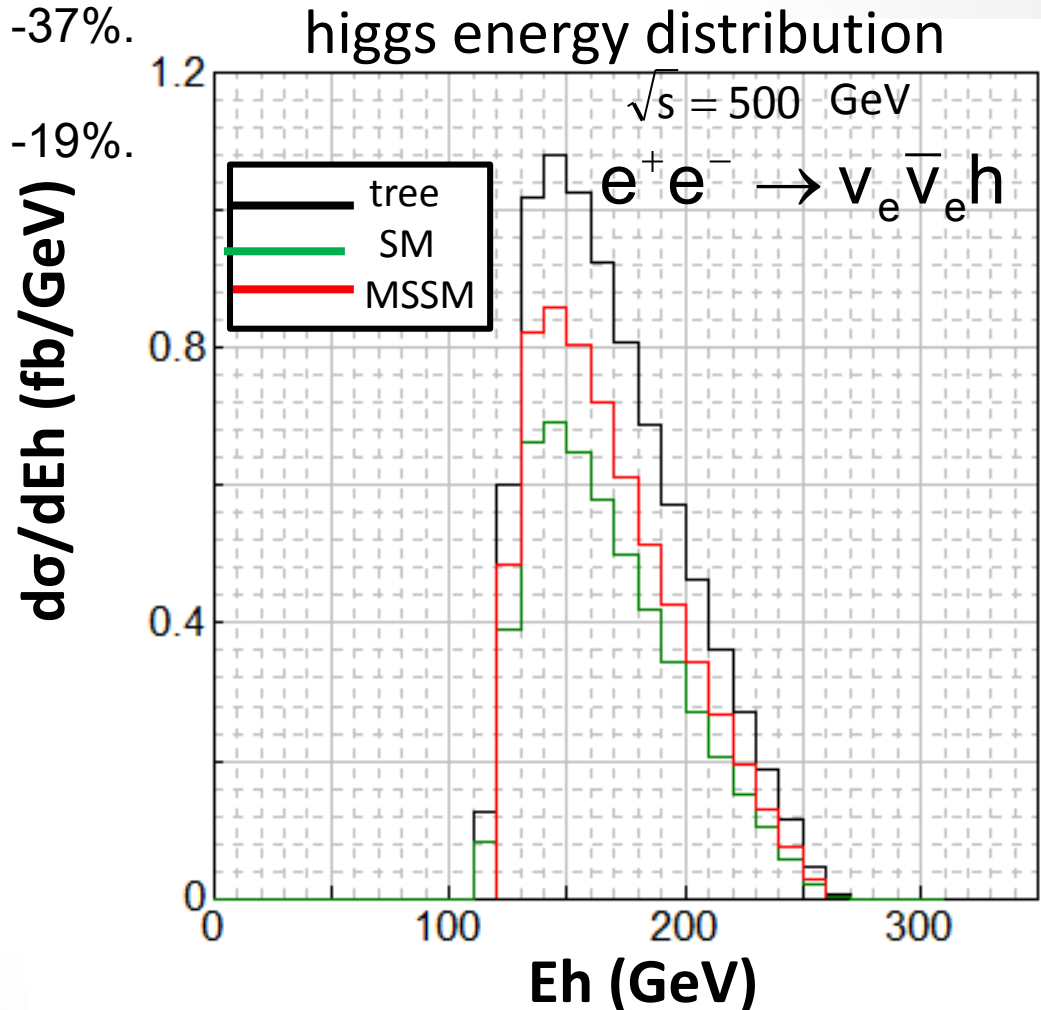
correction ratio ( $\sqrt{s}=250$  GeV)



# Energy distribution (1-loop level)

- ❑ 1-loop correction for the tree level is negative.
- ❑ MSSM correction for SM is positive.
- ❑ The correction of SM total cross section for the tree level is -37%.
- ❑ The correction of MSSM total cross section for the tree level is -19%.

preliminary

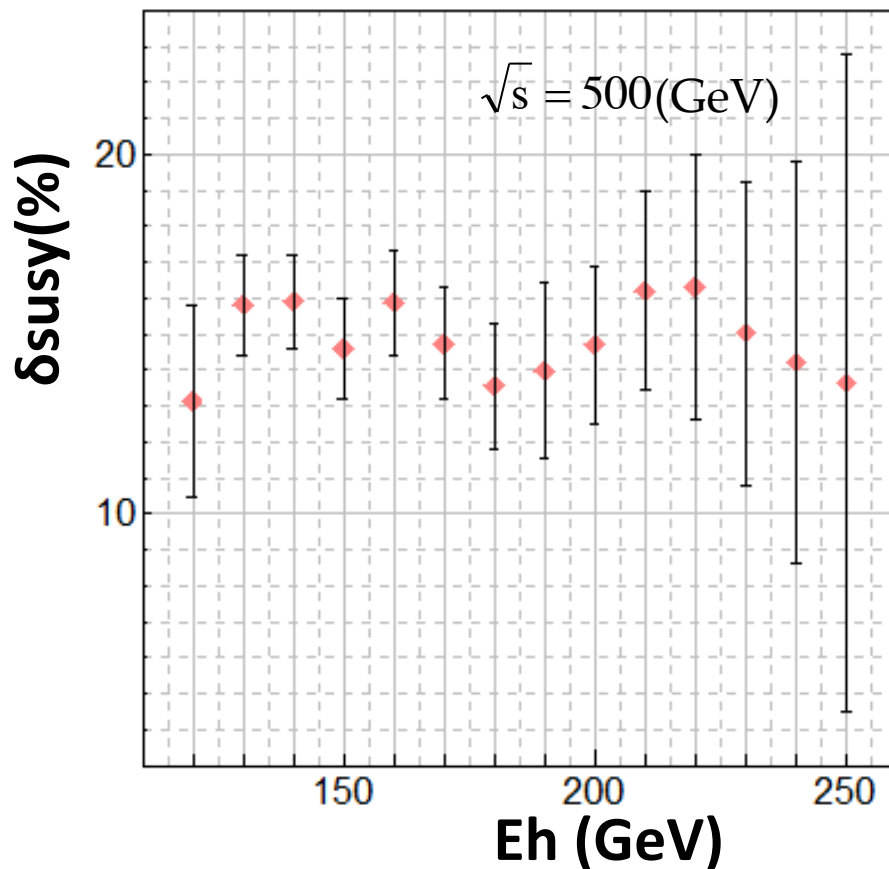


# MSSM 1-loop effect

- We have defined the correction ratio  $\delta$ .
- We have compared with Monte Carlo integration error.
- The correction ratio is 15% in the entire region.
- The 1 loop effect is larger than the error.

$$\delta_{\text{SUSY}} = \frac{\frac{d\sigma_{\text{SUSY1-loop}}}{dE_h} - \frac{d\sigma_{\text{SM}}}{dE_h}}{\frac{d\sigma_{\text{tree}}}{dE_h}}$$

preliminary



# summary

# summary

- We select sets that consistent with Higgs mass, B physics, DM relic density, LHC direct search of sparticles, and muon  $g-2$ (in Zh)
- We have probed statistical significance at the ILC.
- In W fusion calculation, We have considered a set neutralino is not produced, and investigate whether only one loop effect is statistically significant.

## conclusion

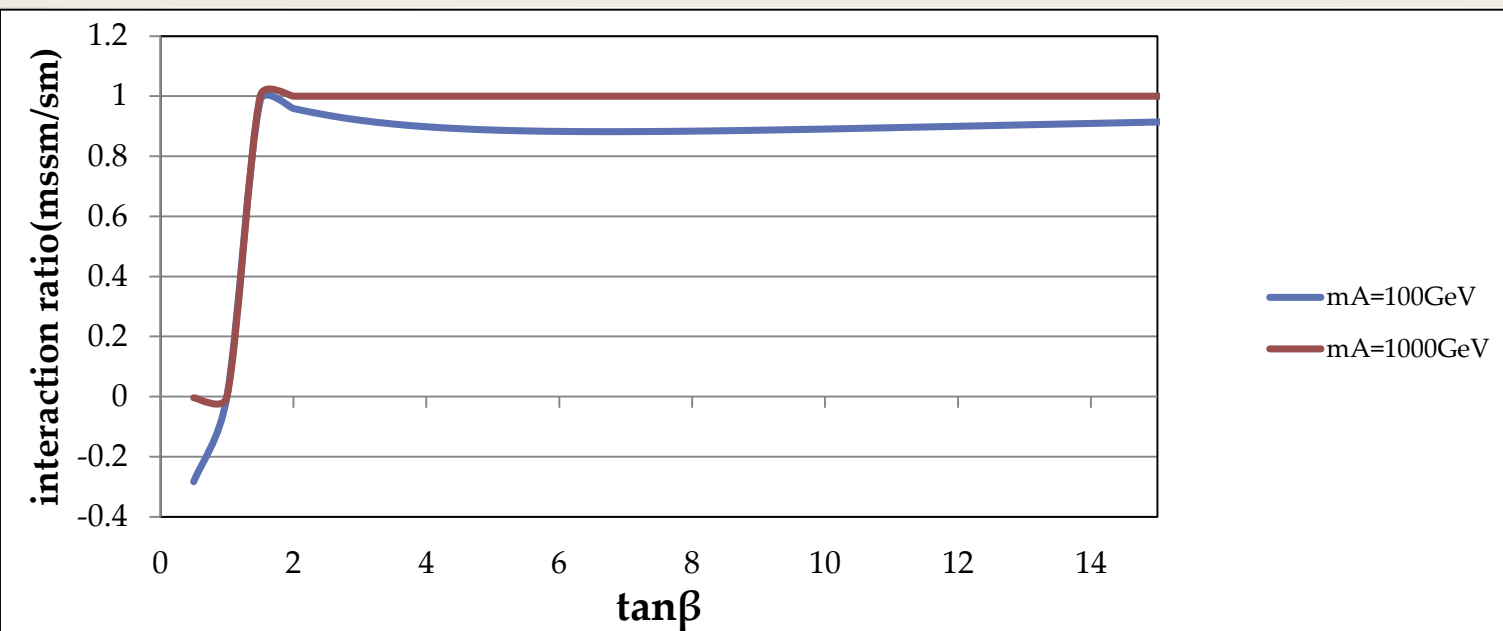
**GRACE/SUSY is very Useful for the search of MSSM particles!!**



back up

# Higgs-Gauge-boson-Gauge-boson

$$L = + gM_W [\cos(\alpha - \beta)H^0 - \sin(\alpha - \beta)h^0]W_\mu^+ W^{-\mu} \\ + \frac{g_Z}{2} M_Z [\cos(\alpha - \beta)H^0 - \sin(\alpha - \beta)h^0]Z_\mu Z^\mu.$$



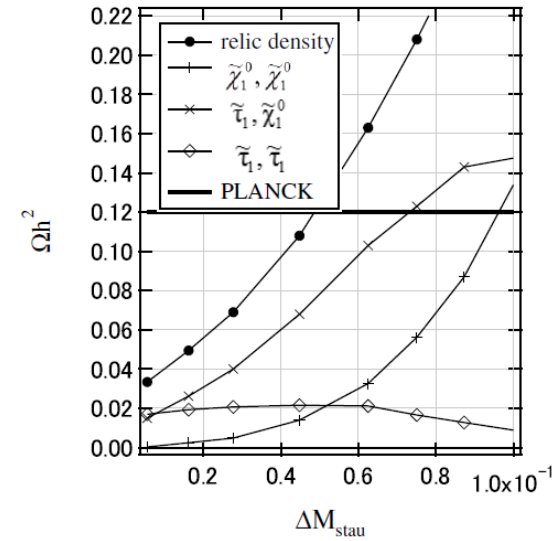
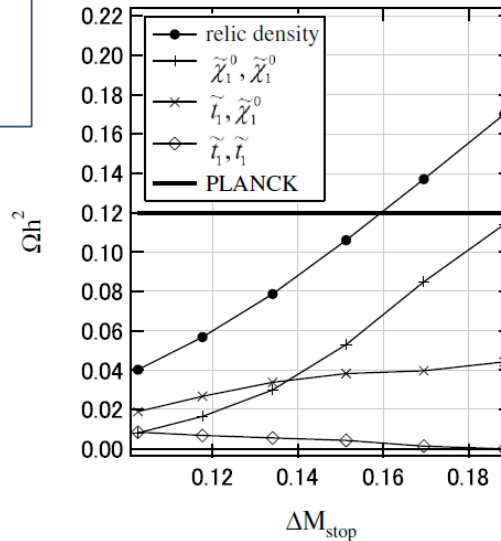
$$d\sigma_{L\&S}^{M,G}(k_c) \equiv d\sigma_{\text{virtual}}^{M,G} + d\sigma_{\text{soft}}^G \quad \leftarrow \text{The part compared in the } \delta\text{susy}$$

$$d\sigma_{1\text{loop}}^{M,G} \equiv d\sigma_{\text{tree}} + d\sigma_{L\&S}(k_c)^{M,G} + \int_{k_c} \frac{d\sigma_{\text{hard}}^G}{dE_\gamma} dE_\gamma$$

canceled each other, because they are common in SM and MSSM

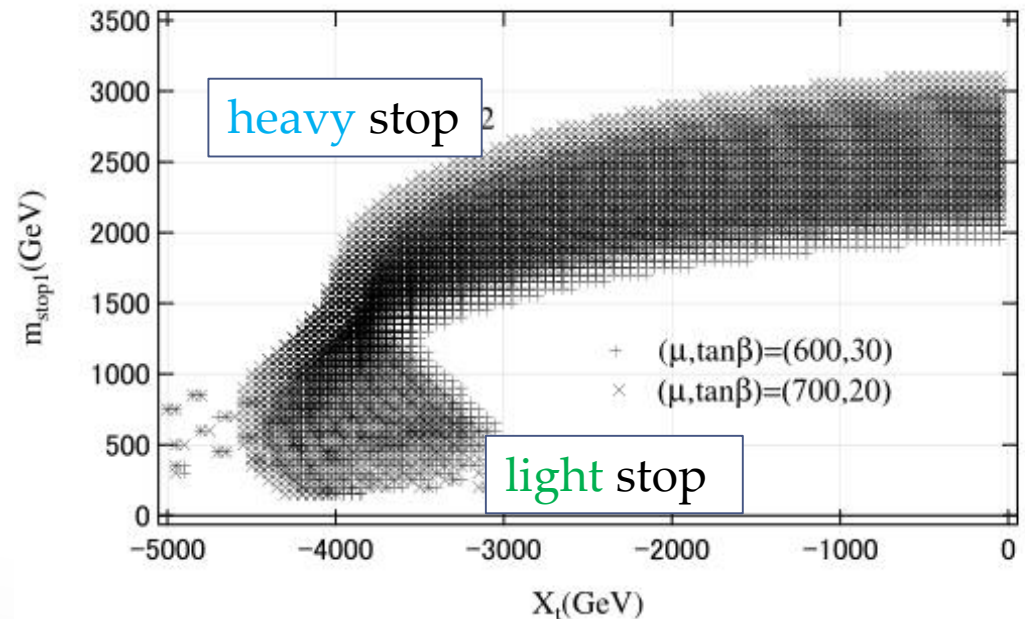
# Classification of sets

Sfermion co-annihilation scenario  
in Bino Dark Matter



micrOMEGAs (G. Belanger, F. Boudjema, A. Pukhov, A. Semenov)

Stop that consistent with Higgs mass



SuSpect2 (A.Djouadi, J.Kneur and G.Moultaka)

# Selection of sets (Zh)

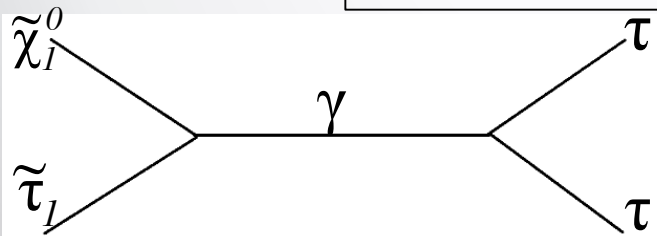
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- DM thermal relic density (Planck data of  $\Omega h^2$ )
- LHC direct search of sparticles

Our sets have almost pure Bino DM  
(No mix with Higgsino or Wino)

Then, the stop1 or the stau1 mass  
are constrained  
(sfermion co-annihilation scenario)

G. Bélanger LAPTH-Annecy



	light stop	heavy stop
	$\cong 300 \text{ GeV}$	$\cong 1000 \text{ GeV}$
The DM abundance is explained by Co-annihilation of stau and LSP	set 1	set 2
The DM abundance is explained by Co-annihilation of stop and LSP	set 3	inconsistent with muon g-2 (LSP is too heavy)