

CPP2010 summary

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CPP2010
KEK, Tsukuba
23–25 September, 2010

A Starting Point

- Lyon 1990 (AIHENP)

People from various nations surprisingly found that all the members are involved in the same problem.

Since then, 20 years passed ...

Experiments in energy frontier

- LHC(2009~)
 $p(7\text{TeV})+p(7\text{TeV})$ (Now, 3.5+3.5)
- ILC(20xx~)
 e^+e^- $W=250\text{GeV}\sim 500\text{GeV}\sim 1\text{TeV}\sim?$
- Toward the Theory of Everything

Higgs processes, Full 1-loop RC available

$$e^+e^- \rightarrow \nu\bar{\nu}H$$

GRACE, PLB559(2003)252
Denner et al., NPB660(2003)289

$$e^+e^- \rightarrow t\bar{t}H$$

GRACE, PLB571(2003)163
You et al., PLB571(2003)85
Denner et al., PLB575(2003)290

$$e^+e^- \rightarrow ZHH$$

GRACE, PLB576(2003)152
Zhang et al., PLB578(2004)349

$$e^+e^- \rightarrow e^+e^-H$$

GRACE, PLB600(2004)65

$$e^+e^- \rightarrow \nu\bar{\nu}\gamma \quad \nu = \nu_\mu, \nu_e$$

GRACE, NIM A534(2004)334

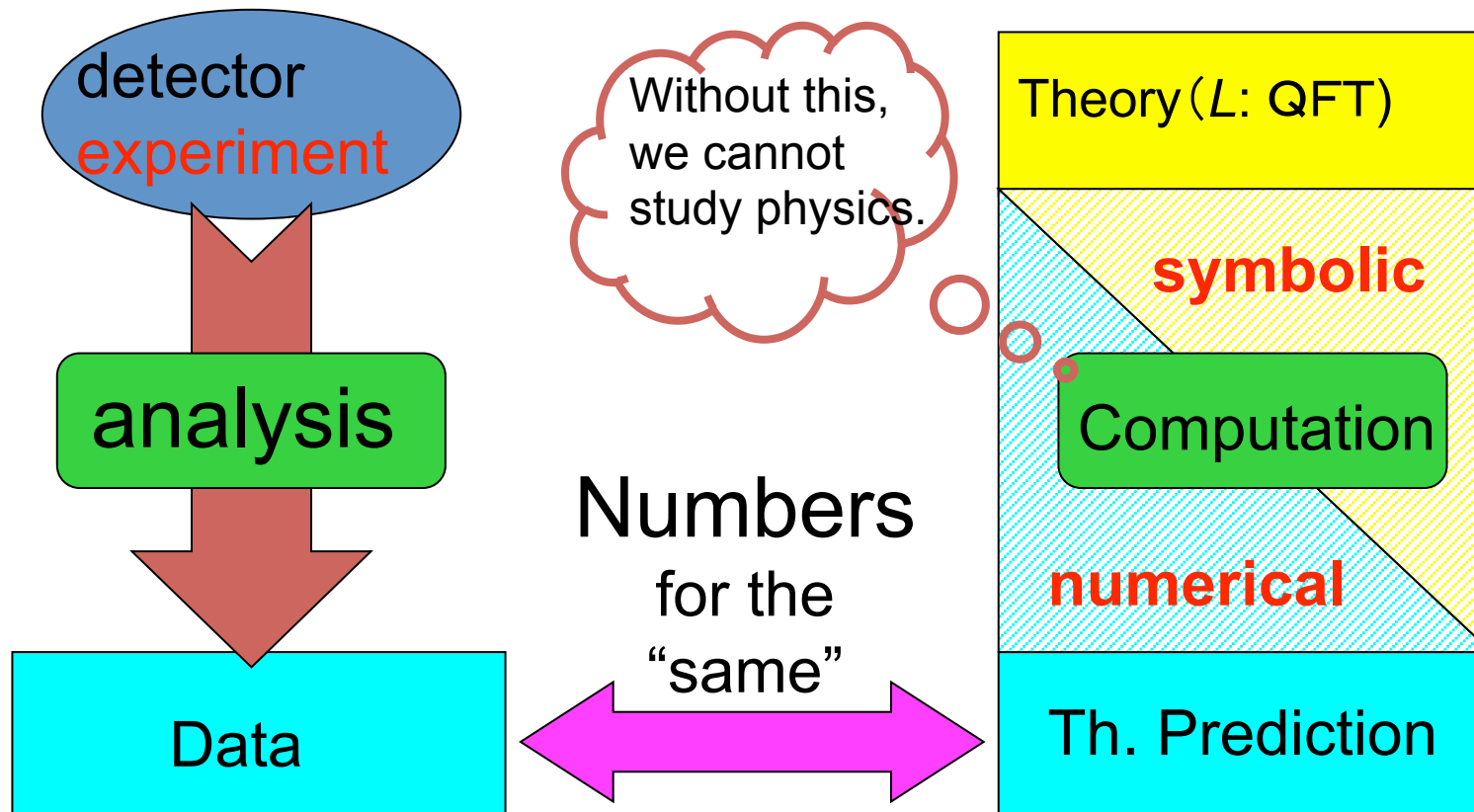
$$e^+e^- \rightarrow \nu\bar{\nu}HH$$

GRACE, Talk by Y.Yasui at
Durham(Sep.2004)

ILC: essential

**ALL done by
automation**

Theory and Experiment



Human's Properties (H.Takahashi-sensei)

- 第1条人間は
気まぐれである
- 第2条人間は
なまけもので
ある
- 第3条人間は
不注意である
- 第4条人間は
根気がない
- 第5条人間は
単調を嫌う
- 第6条人間は
のろみである
- 第7条人間は
論理的思考力
が弱い
- 第8条人間は
何をするかわ
からない

(8) It is
impossible to
predict what a
human will do.

Automatic Computation

*“Render unto Computer the things
which are Computer's”*

Lagrangian in the standard model

$$L = L(QCD) + L(EW)$$

Quantum field theory

strong

$$L(QCD) = -\frac{1}{4} G_{\mu\nu}^a G^{\mu\nu a} + \sum_q \bar{q}(i\gamma^\mu D_\mu - m)q + L(g.f.)$$

Electro-weak

$$L(EW) = -\frac{1}{4} F_{\mu\nu}^a F^{\mu\nu a} + \sum \bar{L} i\gamma^\mu D_\mu L + \sum \bar{R} i\gamma^\mu D_\mu R$$

$$+ (D_\mu \phi)^* (D^\mu \phi) - V(\phi) - \sum_{up} f_u \bar{L}_u \tilde{\phi} R_u - \sum_{down} f_d \bar{L}_d \phi R_d$$

$$+ L(g.f.)$$

g.f.=gauge fixing term & ghost term

How to solve QFT

- Strong coupling region (large g) :
Non-perturbative; Lattice QCD
- Weak coupling region (small g) : perturbative

$$F = F_0 + g^2 F_1 + g^4 F_2 + g^6 F_3 + \dots$$

Lowest order term (tree) may not have sufficient accuracy. Then We need higher order term(loop).

How to compute?

- Method based on Feynman diagrams

→ This talk

Procedure : Well established

“...religious battle between Feynmanians and Unitarians...” Joey Huston

- Non-feynman diagramatic methods

Coverage is extending

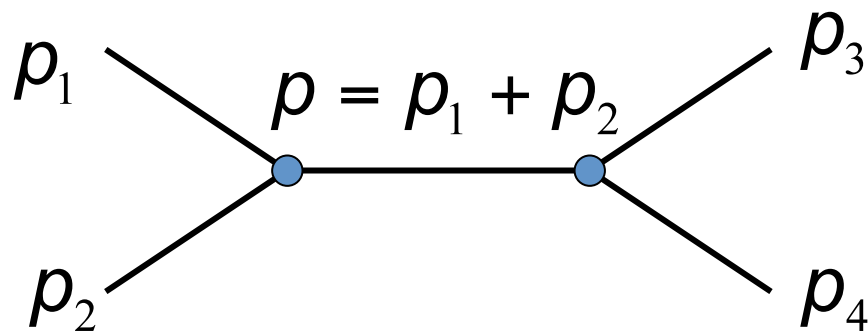
-- ALPHA(ALPGEN) ▪ ▪ tree : Finie freedom → amplitude

-- unitarity method ▪ ▪ effective in some cases

e.g. Multi-gluon amplitude in QCD

Feynman diagrams

tree

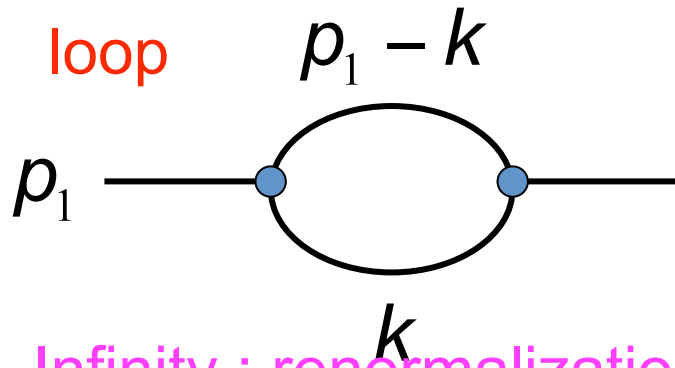


Amplitude T

$$F(p_1)F(p_2)V(p_1, p_2)D(p) \\ \times V(p_3, p_4)F(p_3)F(p_4)$$

Product of the functions
for each components

loop



Amplitude T

$$\int F(p_1)V D(p_1 - k)D(k)VF(p_1)d^4k$$

Products of functions

Integrals over indefinite momenta

Infinity : renormalization

Discover new particles implicitly

Hard calculation

Automatic computations and event generators, tree level

From Lagrangian to Feynman rules

- [LanHEP](#) (native symbolic language)
- [FeynRules](#) (Mathematica)

Tree level hard process integrand generator

- [CompHEP](#) (Squared amplitude, many models including MSSM), [CalcHEP](#) (SM, MSSM, + many)
- [Grace](#) (Helicity amplitudes, SM),
- [FDC](#) (Wang)
- [COMIX](#) (multi-leg tree level event generator, color recursive relation, many legs)
- [AMEGIC++](#) (parton level generator)
- [HELAC/Phegas](#) (dyson-schwinger)
- [O'Mega](#) (alpha algorithm)

General purpose mainly tree level (all decay, $2 \rightarrow 2$, $2 \rightarrow 3$, some $2 \rightarrow 4$, ISR, PS and Hadronisation)

- [Pythia++](#), [Ariadne](#), [MC++](#)
- [Herwig++](#)
- [Isajet](#)

General purpose event generators based on automatic integrand calculations

- [Whizard](#) (O'Mega)
- [Sherpa](#) (using Comix and AMEGIC++, CKKW, Pythia (or Pythia like))
- [Madgraph](#), [MadEvent](#)
- Graceful (based on Grace, interfaced to Pythia) in progress ...

Specific set of event generators

- [Gr@ppa](#) (Grace for matrix elements and Pythia/Herwig for parton shower/Hadronization)
- [AlpGen](#) (multi parton generation)

Parton shower matching

- [CKKW](#), [POWHEG](#), [MLM](#), Subtraction method (matrix element matching with shower MC)

Event database:

- MC database (CompHEP)
- [JETWEB](#)

Dubinin's
Talk

Wang's
Talk

Jimbo's
Talk

Automatic computations and event generators, NLO,...

- [RESBOS](#) (Q_T resummation NLO/NNLO, no parton shower necessary) lepton distributions in Drell-Yan-like processes); inclusive with respect to hadronic radiation

NLO hard process

NLO event generators (specific processes)

- [MC@NLO](#) (Herwig + Subtraction methods: H, single Boson, single top, lepton pairs, H + W/Z, ...)
- [MCFM](#) (full spin correlation, Wbb, ...)
- [BlackHat](#) (one-loop, W/Z+3,4 jets)
- [NLOjet++](#) ([Catani-Seymour dipole subtraction method](#))
- [Rocket](#) (N-gluon amplitude, 2-q + N-g, W + 2-q + N-g, W + 4 q + Ng... N > 20)
- [CutTools](#) (one-loop amplitudes at integrand level)
- [JETRAD](#) (inclusive 1 and 2 jet production)
- JETI
- [FeynCalc](#) (Mathematica/Form Passarino-Veltman reduction of one-loop amplitudes to standard scalar integrals) FeynArt, FeynRules, ...
- [Grace one-loop](#)
- [FDC \(loop\)](#)
- [Golem](#) (one-loop amplitude up-to six legs)
- [Phox family JetPhox](#) (inclusive γ /hadron+jet, [Diphox](#) (hadron production of 2 γ , hadron+ γ , hadron+hadron)

Reiter's
Talk

Wang's
Talk

Jimbo's
Talk

Denis Perret-Gallix

SUSY specific and Cosmology

Spectrum calculations (RGE codes)

- [Isasusy](#)
- [Softsusy](#)
- Spheno
- Suspect

Amplitude calculation Tree level

- [Grace/Susy](#) (MSSM)

One-loop dedicated

- Prospino
- Hprod

One-loop General

- Grace-susy One-loop
- FormCalc
- SloopS

Cosmology

- [Micromegas](#): relic density computation based on LANHEP, CALCHEP
- DarkSusy
- NeutDriver
- IsaRed

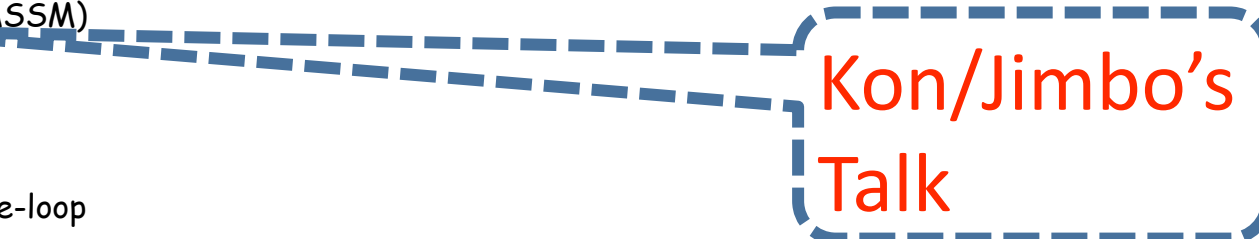
Decay code

- HDECAY
- NMHDECAY
- SDECAY

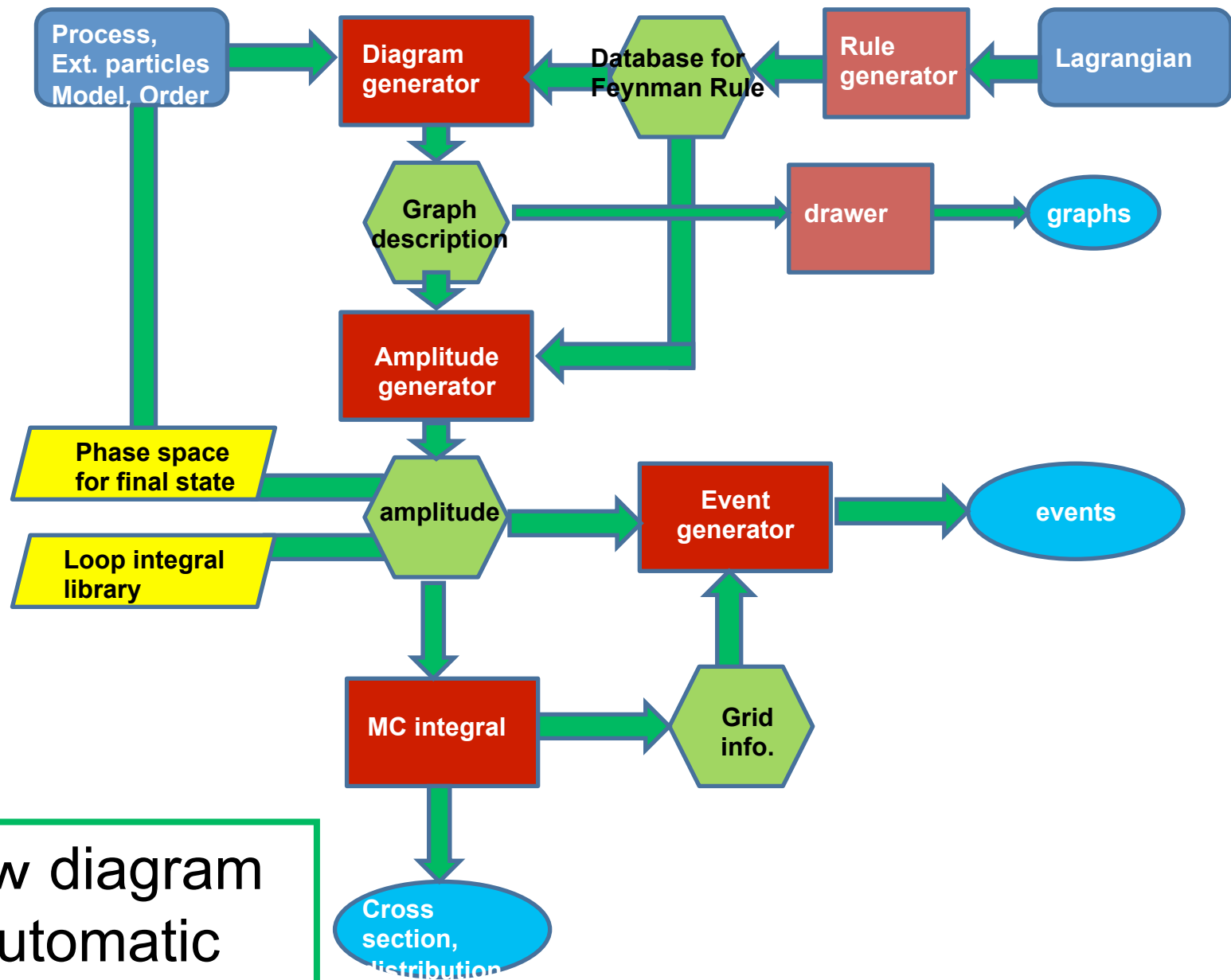
Fitters

- Fittino
- Sfitter

SLHA



Kon/Jimbo's
Talk



Flow diagram
of automatic
computation

From Lagrangian to Feynman Rule

* LanHEP (A. Semenov)

<http://theory.sinp.msu.ru/~semenov/lanhep.html>

* FDC (J.-X. Wang)

www.ihep.ac.cn/lunwen/wjx/public_html



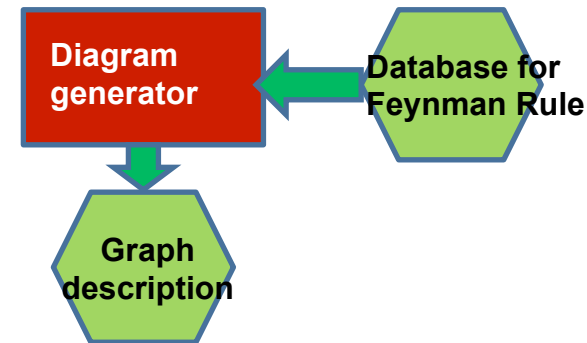
LanHEP+CompHEP(Dubinin's talk)

Add a new interaction easily to the SM.

→ BMS study

Graph generation

- * QGRAF (P. Nogueira)
<http://cfif.ist.utl.pt/~paulo/qgraf.html>
- * GRACE (T. Kaneko)
- * FeynArts (T. Hahn)
- * FDC (J.-X. Wang)
www.ihep.ac.cn/lunwen/wjx/public_html



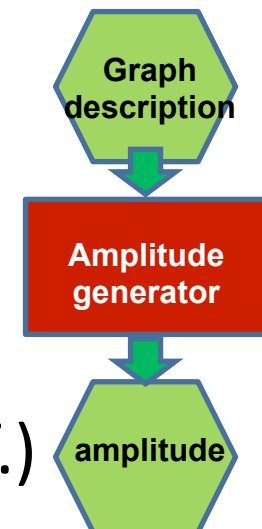
Importance of symbolic manipulation system
FORM (Vermaseren's talk)

GRAPH to Amplitude

Complex processes: Produced code is huge!

(Number of diagrams and each diagram itself.)

Required robust and powerful system.



QED : number of diagrams

Process	Loop	diagrams	Process	Loop	diagrams
$e^- \rightarrow e^-$	1	1	$e^- e^- \rightarrow e^- e^-$	1	10
	2	3		2	94
	3	18	$e^+ e^- \rightarrow e^+ e^-$	1	10
	4	153		2	94
	5	1638		3	1136
	6	20898	$e^+ e^- \rightarrow e^+ e^- \gamma$	1	72
$\gamma \rightarrow \gamma$	1	1	$e^+ e^- \rightarrow e^+ e^- \gamma \gamma$	0	40
	2	3		1	564
	3	18	$e^+ e^- \rightarrow e^+ e^- e^+ e^-$	0	36
	4	153		1	552
$e^+ e^- \rightarrow \gamma$	1	1	$e^+ e^- \rightarrow e^+ e^- \mu^+ \mu^-$	0	36
	2	7		1	552
	3	72	$e^+ e^- \rightarrow e^+ e^- \mu^+ \mu^- \gamma$	0	252
	4	891	$e^+ e^- \rightarrow e^+ e^- 2(\mu^+ \mu^-)$	0	1728
	5	12672	$\gamma \gamma \rightarrow \gamma \gamma$	1	6
	6	202770		2	60

T.Kaneko, S.Kawabata, Y.Shimizu, CPC 43 (1987) 279

also T.Sasaki, J.Comput. Phys. 22 (1976) 189

Cross section

$$d\sigma = (\text{factors}) \times \left| \sum T \right|^2 \times (p.s.)$$

Phase space
for final state

amplitude

$$(p.s.) = (2\pi)^4 \delta\left(\sum_{final} p_j - P_0\right) \prod_{final} \frac{d^3 p_j}{2E_j (2\pi)^3}$$

LHC, ILC $\rightarrow$ multi-body final states are important
multiple integration : Numerical integration (adaptive MC)

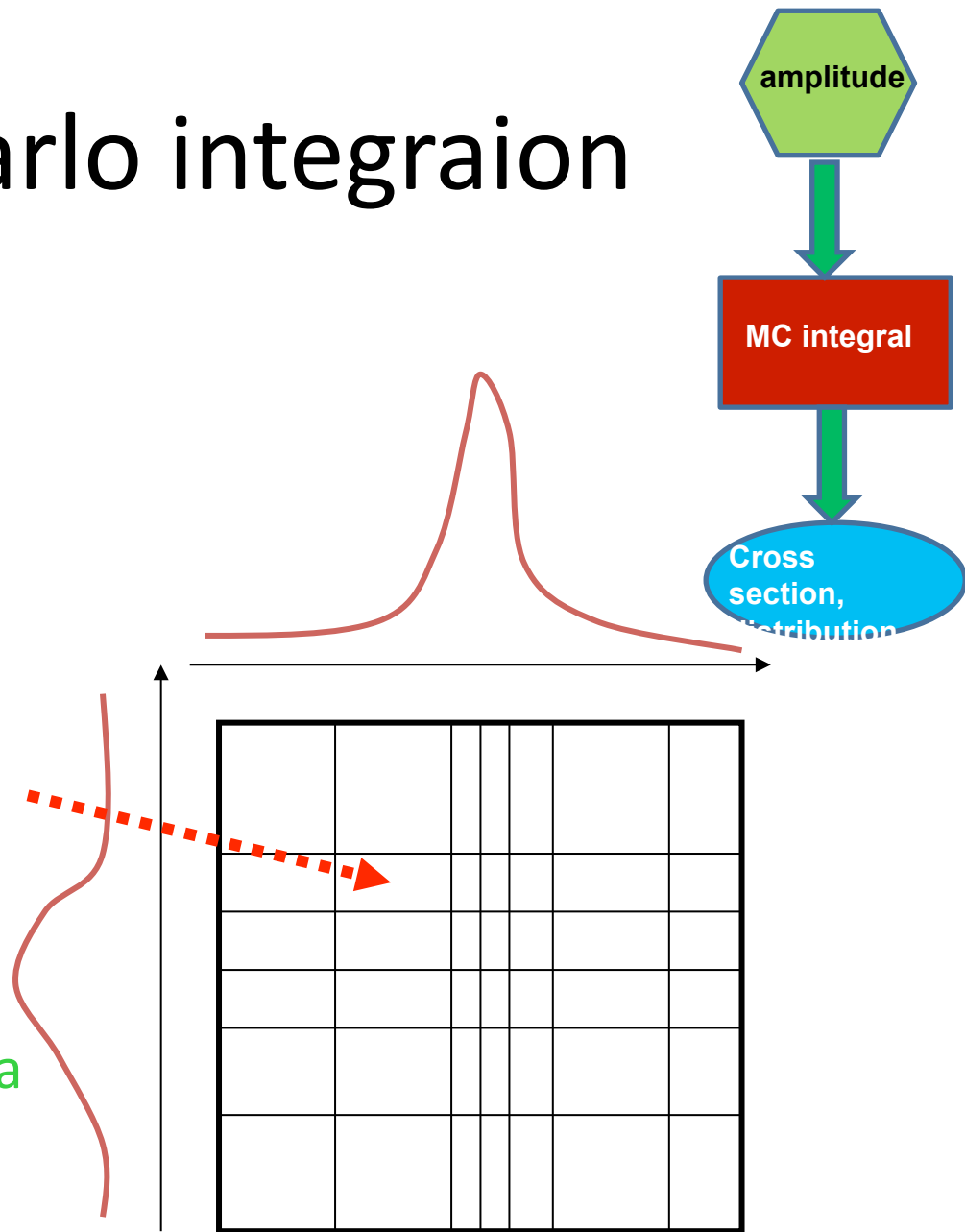
Integrand : several singularity originating from physical reasons (Infrared, collinear, resonance, forward angle, gauge cancelation, ...)

How to choose variables ? (e.g., Dubinin's talk)

MonteCarlo integraion

VEGAS, BASES
importance and
stratified sampling
adjust grid so that
weights in each
hypercube are
uniform

→ Only possible when each
singularity is assigned to a
specific variable



Loop integral



1-loop

Reduction
momentum or
Feynman x ?



$$\int d^n \ell \frac{\{1, \ell^\mu, \ell^\mu \ell^\nu, \ell^\mu \ell^\nu \ell^\rho, \dots\}}{(\ell^2 - m_1^2 + i\varepsilon)((\ell + p_1)^2 - m_2^2 + i\varepsilon)((\ell + p_{12})^2 - m_3^2 + i\varepsilon) \dots}$$

Loop integrals

1-loop

Many good libraries and formulas

e.g.

Golem

Kaneko: analytical formulas by hypergeometric functions clear and well-organized structure

Main target : 2-LOOP

Sector Decomposition(Ueda)

- Sector decomposition disentangles overlapping singularities in multi-dimensional integration

$$\int_0^1 dx \int_0^1 dy \frac{f(x, y)}{(x+y)^{2-\epsilon}} \quad f(x, y) : \text{finite} \quad \epsilon \rightarrow +0$$

singular when simultaneously $x, y \rightarrow 0$

Split integration domain

$x > y$ Remap to [0:1]

$y > x$

Factor out x

Similarly $x \rightarrow \tilde{x}y$

singular behavior is factorized as non-singular powers of one variable $x \rightarrow 0$

$$= \int_0^1 dx \int_0^x dy \frac{f(x, y)}{(x+y)^{2-\epsilon}} + \int_0^1 dy \int_0^y dx \frac{f(x, y)}{(x+y)^{2-\epsilon}}$$

$$= \int_0^1 dx \int_0^1 d\tilde{y} \frac{x d\tilde{y}}{(x+x\tilde{y})^{2-\epsilon}} f(x, x\tilde{y})$$

$$= \int_0^1 dx \int_0^1 d\tilde{y} \frac{1}{x^{1-\epsilon}} \frac{f(x, x\tilde{y})}{(1+\tilde{y})^{2-\epsilon}} + \int_0^1 d\tilde{x} \int_0^1 dy \frac{1}{y^{1-\epsilon}} \frac{f(\tilde{x}y, y)}{(1+\tilde{x})^{2-\epsilon}}$$

$$\int_0^1 dx \frac{f(x)}{x^{1-\epsilon}} = \int_0^1 dx \frac{f(0)}{x^{1-\epsilon}} + \int_0^1 dx \frac{f(x) - f(0)}{x^{1-\epsilon}} = \frac{f(0)}{\epsilon} + \int_0^1 dx x^\epsilon \frac{f(x) - f(0)}{x}$$

singular when $x \rightarrow 0$

pole

non-singular at $x \rightarrow 0$

Test Implementation(Ueda)

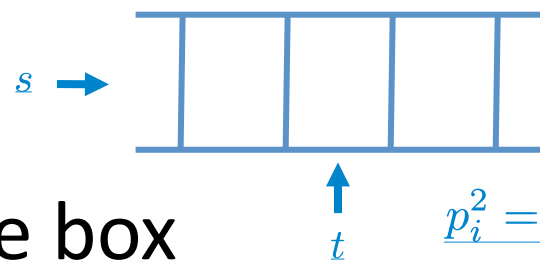
- Our test implementation
 - Dual cone construction
 - Convex hull - Incremental algorithm
 - Triangulation
 - Our own simple algorithm; Neither unique, nor optimum
 - Written in Python (and very slow)

of generated sectors

Diagram	A	B	C	S	X	our method
Box	12	12	12	12	12	12
Double box	755	586	586	362	293	266
Triple box	M	114256	114256	22657	10155	6568
D420	8898	564	564	180	F	168

Our method gives less number of sectors than other methods !!

An Example Calculation(Ueda)



$$= \Gamma(4 + 3\epsilon) \left[\sum_{i=0}^6 \frac{C_i}{\epsilon^i} + \mathcal{O}(\epsilon) \right]$$

- On-shell triple box

Taking symmetries into account, Strategy X and our method generate

Strategy X : 4143 terms (ratio ~ 1.55)
 Out method : 2670 terms

	Strategy X		Our method		Exact value
C_6	0.098765(± 0.000004)	1.4s	0.098765(± 0.000003)	0.7s	0.098765
C_5	-0.767001(± 0.000027)	10.7s	-0.767001(± 0.000033)	4.4s	-0.767001
C_4	1.977227(± 0.000156)	2.9m	1.977224(± 0.000326)	1.1m	1.977227
C_3	-0.753089(± 0.001144)	26.6m	-0.753088(± 0.001192)	10.1m	-0.753080
C_2	-4.749675(± 0.006682)	2.5h	-4.749694(± 0.003523)	1.3h	-4.749610
C_1	2.016040(± 0.042107)	6.9h	2.016607(± 0.014341)	4.1h	2.016790
C_0	21.673992(± 0.268047)	16.4h	21.692735(± 0.067518)	9.9h	21.692455

$s = -1, t = -3$, integrated by Cuba1.7 (Vegas) 10Mpts, Xeon X5560 (2.80GHz) x 8cores

16.4h / 9.9h 1.66

Analytical result: V.A. Smirnov, Phys.Lett.B567 (2003) 193

XLOOPS-GiNaC(Do)

Gram determinant problem free.

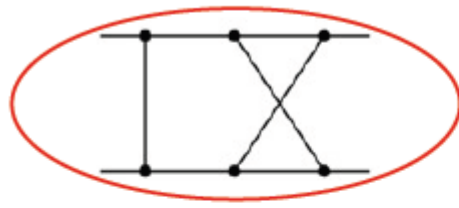
Tensor integrals are automatically decomposed into integrals of components of internal momenta. No matrix inversion!

Complex mass is possible.

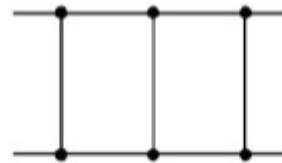
Numerical comparison in one-loop, two-loop in progress.

2-loop in XLOOPS-GiNaC(Do)

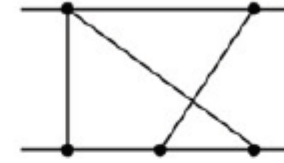
- We are interested in a subgroup of Scalar Two-loop box integral (crossed and planar topologies)



(a)



(b)



(c)

$$S_0 = 4 \int_0^\infty dl_\perp dk_\perp \int_{-\infty}^\infty \frac{dl_0 dl_1 dl_2 dk_0 dk_1 dk_2}{P(l)P(l+k)P(k)}$$

$$P(l) = \prod_i^{N_l} [(l + q_i)^2 - m_i^2 + i\eta] , \quad P(k) = \prod_n^{N_k} [(k + q_n)^2 - m_n^2 + i\eta]$$

$$P(l+k) = \prod_j^{N_{lk}} [(l+k+q_j)^2 - m_j^2 + i\eta]$$

Kreimer Phys.Lett.B347, 1995; Kreckel, Eur.Phys.J.C6 1998

Direct computation method(Yuasa)

Analytical computation

-> **epsilon** infinitesimal

-> complex analysis

$$I = \lim_{\varepsilon \rightarrow 0} \int_0^1 dx \int_0^{1-x} dy \frac{1}{D(x,y) - i\varepsilon}$$

Sometimes $D=0$ in
the integral region

$$\Re(I(\varepsilon_l)) = \int_0^1 dx \int_0^{1-x} dy \frac{D(x,y)}{D(x,y)^2 + \varepsilon_l^2},$$

$$\Im(I(\varepsilon_l)) = \int_0^1 dx \int_0^{1-x} dy \frac{\varepsilon_l}{D(x,y)^2 + \varepsilon_l^2}$$

Keep **epsilon** FINITE

Denominator > 0

Numerical integration

$$\varepsilon_l = \frac{\varepsilon_0}{c^l}, \quad c > 1$$

Extrapolate $I(\varepsilon_l)$

and get the result when ε becomes 0

using ε -algorithm by P.Wynn.

ε -algorithm: a math-magic

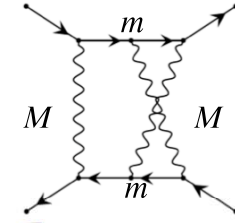
2.5
2.666666667
2.708333333
2.716666667
2.718055556
2.718253968
2.718278770



e=2.718281828

$$\tau_{k,\lambda+1} = \tau_{k+1,\lambda-1} + \frac{1}{\tau_{k+1,\lambda} - \tau_{k,\lambda}}$$

Two-loop non-planar box



$$\mathcal{I} = - \int_0^1 dx_1 dx_2 dx_3 dx_4 dx_5 dx_6 dx_7 \delta(1 - \sum_{\ell=1}^7 x_\ell) \frac{\mathcal{C}}{(\mathcal{D} + i\epsilon\mathcal{C})^3},$$

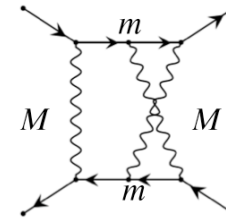
$$\begin{aligned} \mathcal{D} = & -\mathcal{C} \sum x_\ell m_\ell^2 \\ & + \{s(-x_1x_5x_6 + x_2x_3x_4 + x_2x_3x_5 + x_2x_3x_6 + x_2x_3x_7 + x_2x_6x_7 + x_3x_4x_5) \\ & + t(x_1(x_4x_7 - x_5x_6)) \\ & + p_1^2(x_1(x_2x_4 + x_2x_5 + x_2x_6 + x_2x_7 + x_4x_5 + x_5x_6)) \\ & + p_2^2(x_1(x_3x_4 + x_3x_5 + x_3x_6 + x_3x_7 + x_5x_6 + x_6x_7)) \\ & + p_3^2(x_1x_5x_6 + x_1x_5x_7 + x_2x_4x_7 + x_2x_5x_7 + x_3x_5x_6 + x_3x_5x_7 + x_4x_5x_7 + x_5x_6x_7) \\ & + p_4^2(x_1x_4x_6 + x_1x_5x_6 + x_2x_4x_6 + x_2x_5x_6 + x_3x_4x_6 + x_3x_4x_7 + x_4x_5x_6 + x_4x_6x_7)\} \end{aligned}$$

and

$$\mathcal{C} = (x_1 + x_2 + x_3 + x_4 + x_5)(x_1 + x_2 + x_3 + x_5 + x_6 + x_7) - (x_1 + x_2 + x_3)^2.$$

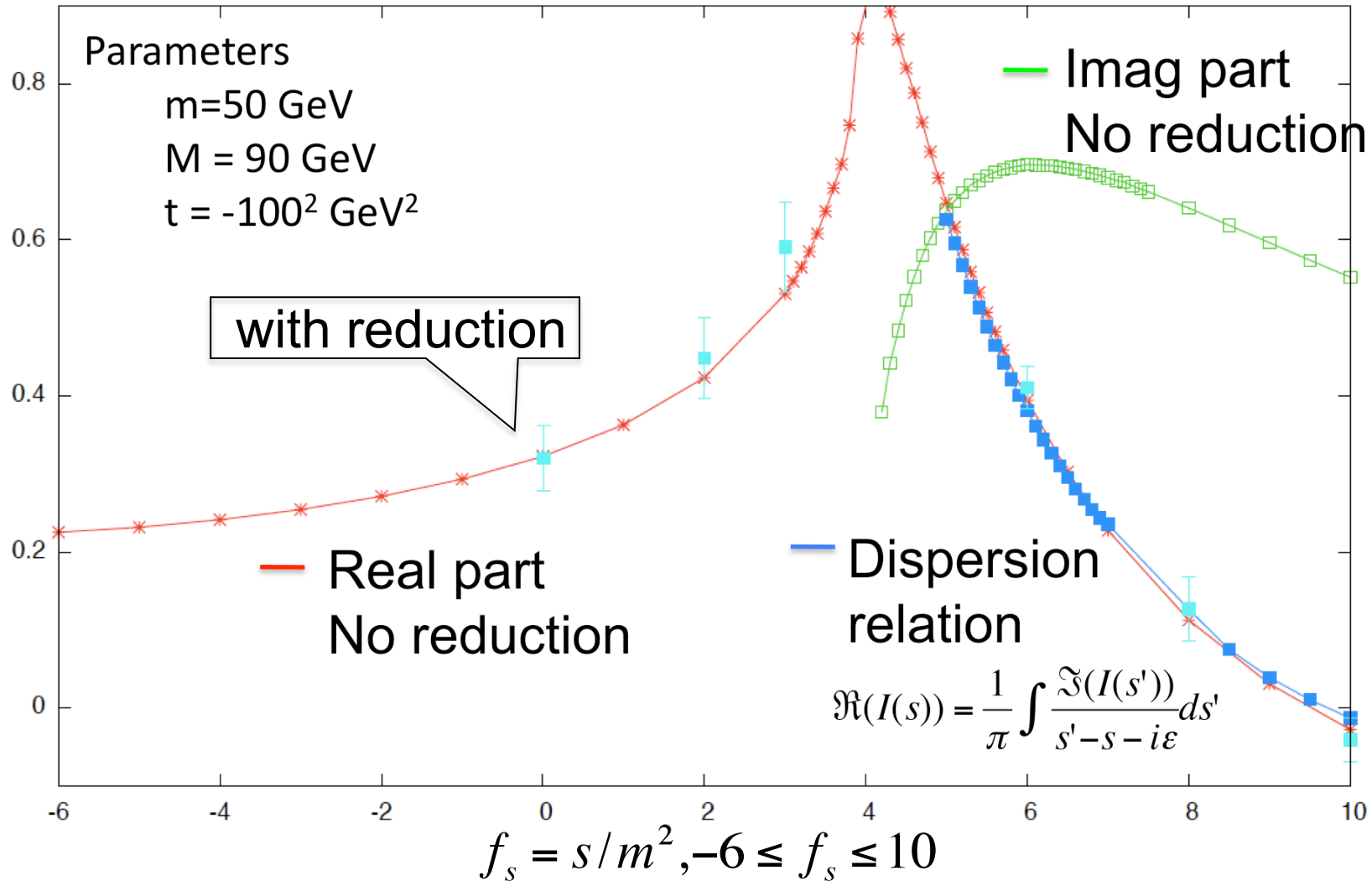
Here, $s = (p_1 + p_2)^2 = (p_3 + p_4)^2$, $t = (p_1 + p_3)^2 = (p_2 + p_4)^2$ and $p_1 + p_2 + p_3 + p_4 = 0$.

Example of direct computation method two-loop **non-planar** box with masses



YUASA

$\times 10^{-12}$



ε - δ method(de Doncker)

$$\frac{1}{D - i\delta}$$

original direct method
Keep **delta** finite

$$\left(\frac{1}{D - i\delta} \right)^{K+\varepsilon}$$

Also keep n-dimension
as $n=4+2$ **epsilon**

$$\frac{1}{\varepsilon} C_{-1} + C_0 + O(\varepsilon)$$

Extract infrared pole
numerically with delta
regularization

Precision control

Long digit computation is required:

- To get the precise results
- To avoid instabilities

Singularity

REAL: e.g., IR divergence, Landau singularity, ...

INSTABILITY: e.g. Gram-determinant in numerator reduction

Gram-det.=0 ... skip calculation (measure=0)

Gram-det. **is not 0 but very small**

→ stabilized by the long digit computation

(e.g. , Le,D.N. : **small DetG expansion or using quadruple precision**)

An example : Long digit computation is required

- $f = 333.75 \cdot (b^{**6})$
+ $(a^{**2}) \cdot \{11 \cdot (a^{**2}) \cdot (b^{**2}) - (b^{**6}) - 121 \cdot (b^{**4}) - 2\}$
+ $5.5 \cdot (b^{**8}) + a / (2 \cdot b),$
where $a=77617.0$, $b=33096.0$.

by C. Hu, S. Xu and X. Yang

- $f = 1.1726039400531786318588349045201801$
w/ Quadruple precision
- Analytical result = - 54767/66192
= - 0.82739605994682136814116509547981370
- Using the new Octuple precision library in [HMLib](#):
 $f = - 0.827396059946821368141165095479816$
with lost bits = 121

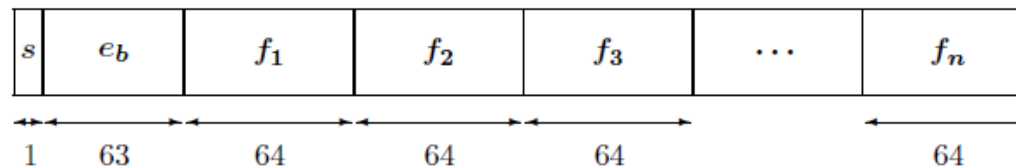
Exflib(Fujiwara)

Key features

- 60 – 20,000 decimal digit arithmetic
- range : $10^{-10^{18}}$ – $10^{10^{18}}$
- basic four rules, built-in functions
- polymorphic interface in C++, FORTRAN90
- instruction level optimization in assembly language

64-bit unsigned integer array

Data structure of exfloat



$$(-1)^s \times 2^{e_b - \text{BIAS}} \times \left(1 + \sum_{i=1}^n \frac{f_i}{2^{64i}} \right)$$

A mult-precision library

HMLib: New FORTRAN Library for High-speed Multiprecision operations

- Library in FORTRAN ← available for any architectures
- Based on Integer operations → fast & “lost bits” information for subtraction.
- For the octuple floating point operations:
based on IEEE754,
1 bit for sign, 15 bits for exponent,
240 bits for mantissa.
- For example **Number of lost digit is reported!**
call Q4ADDSUB(A,B,C,I,IBIT) :
for add/sub in Quad.
- MULT/DIV,SQRT,LOG,ATAN2 ... are also available

Hardware: quadruple precision

GRAPE-DR



512PE(90nm,200mm²) 200MHz
400Gflops/chip(Single Precision)
200 Gflops/chip(Double Precision)

5GFLOPS in quad-precision



GRAPE-MP (semi-custom)
Chip for quad-precision

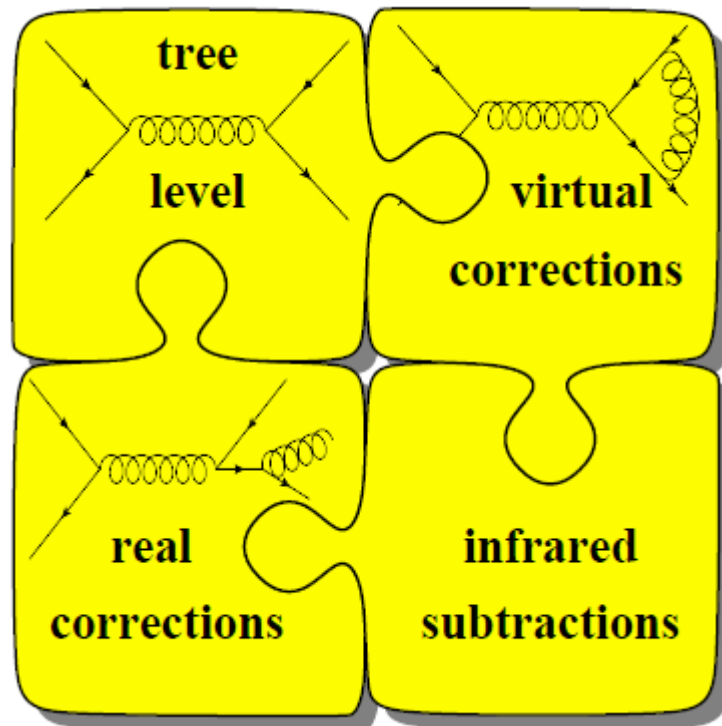


Test
board

GRAPE-MP project is working

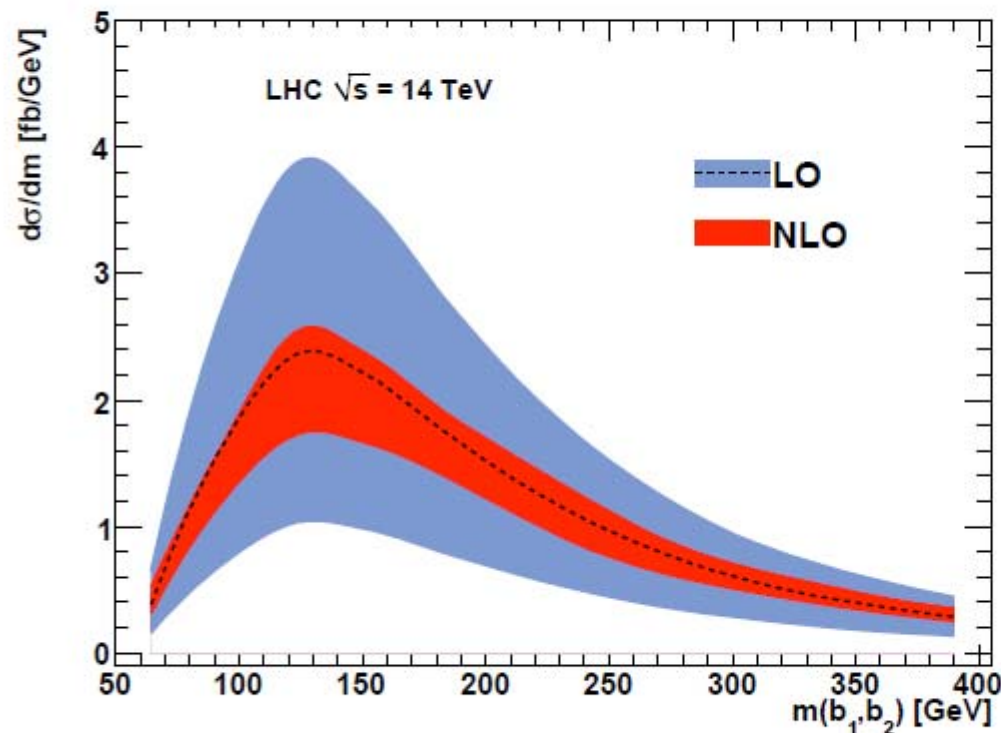
Physcal results

NLO by GOLEM/SAMURAI



$q\bar{q} \rightarrow b\bar{b}b\bar{b}$: Results

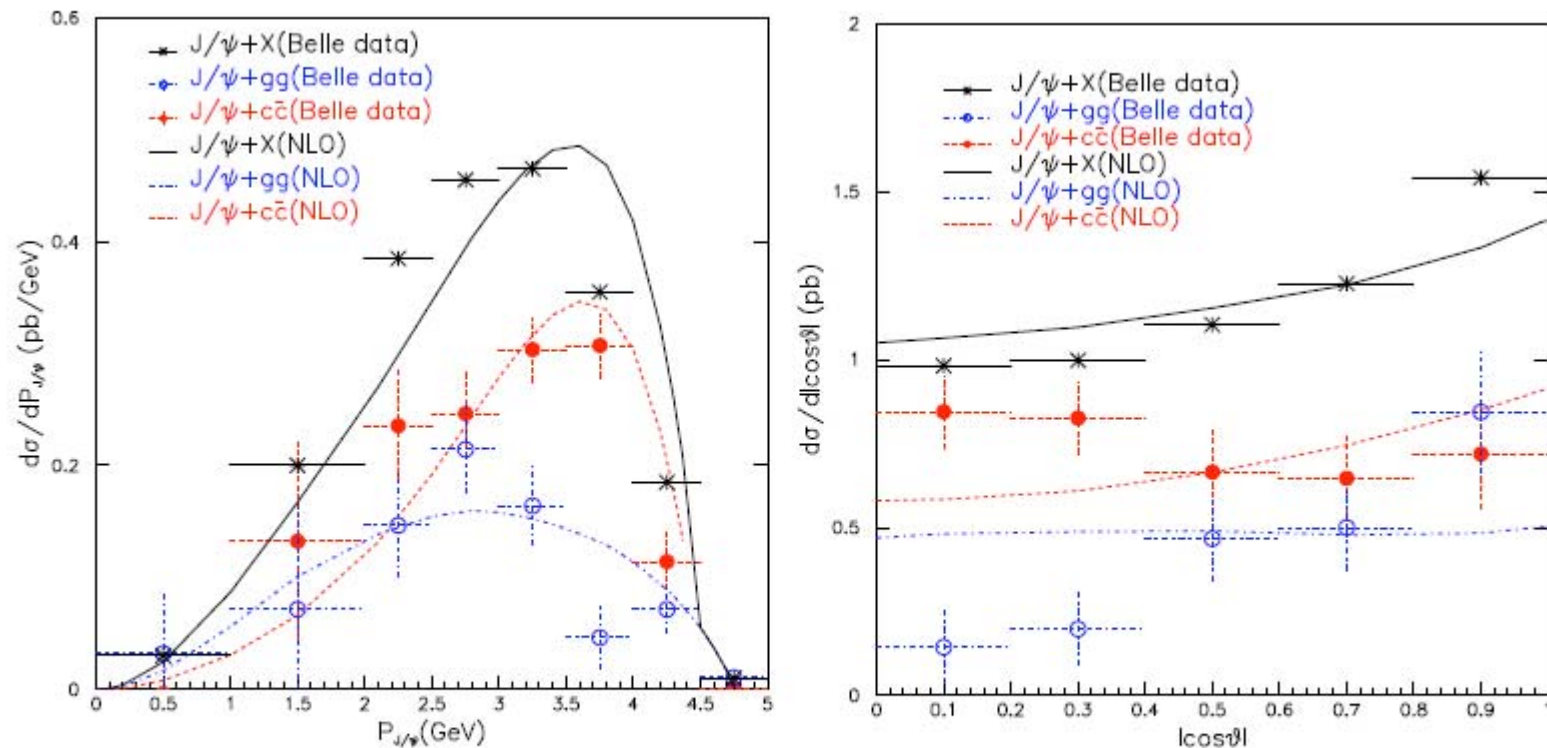
m_{bb} of leading b -jets



- ▶ significant reduction of scale dependence
- ▶ plateau region around $x = 0.5$
- ▶ stabilization of result
- ▶ error bands:
 $\mu_0/4 < \mu_R < 2\mu_0$
- ▶ complete analysis after inclusion of all channels

$$\sqrt{s} = 14 \text{ TeV}, \mu_R = \frac{1}{2} \sqrt{\sum_j p_T^2(b_j)}, \mu_F = 100 \text{ GeV}, m_b = 0$$

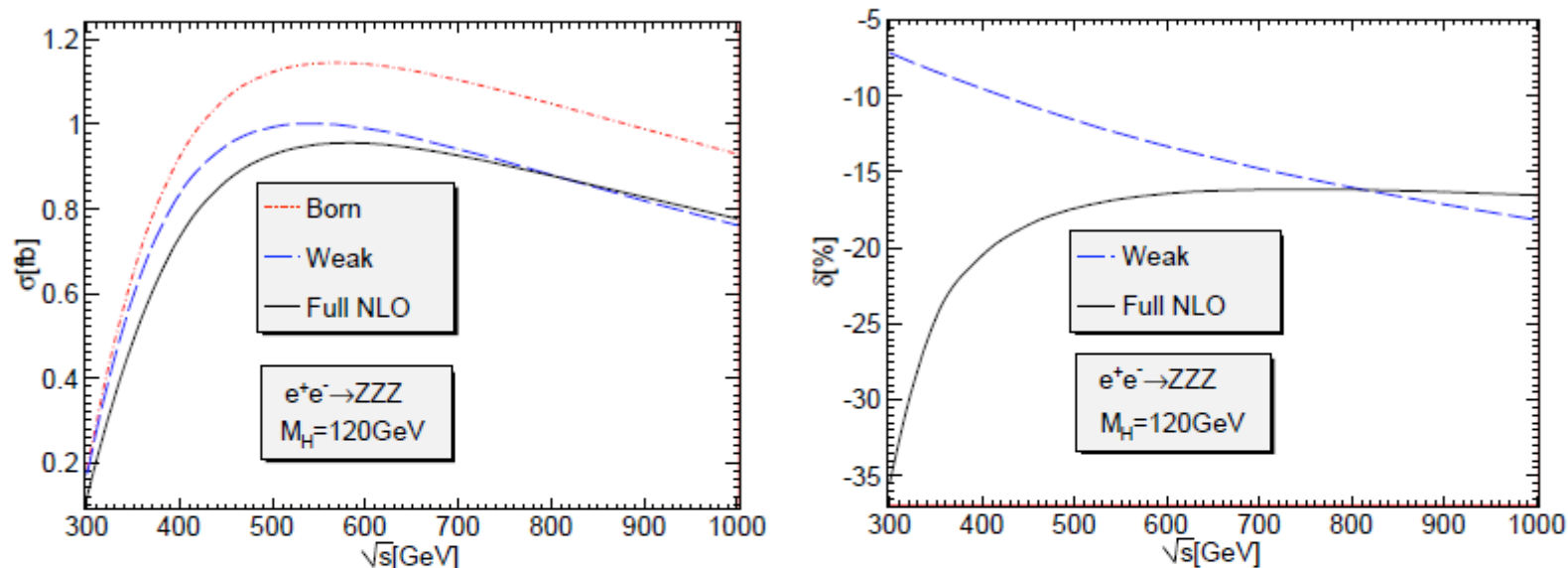
Heavy quarkonium production: FDC-LOOP (Wang)



Momentum distribution of inclusive J/ψ production with $\mu = \mu^*$ and $m_c = 1.4$ GeV is taken for the $J/\psi cc$ channel. The contribution from the feed-down of ψ' has been added to all curves by multiplying a factor of 1.29.

EW 1-loop tri-boson production(Le)

$e^+e^- \rightarrow ZZZ$: Total Xsection



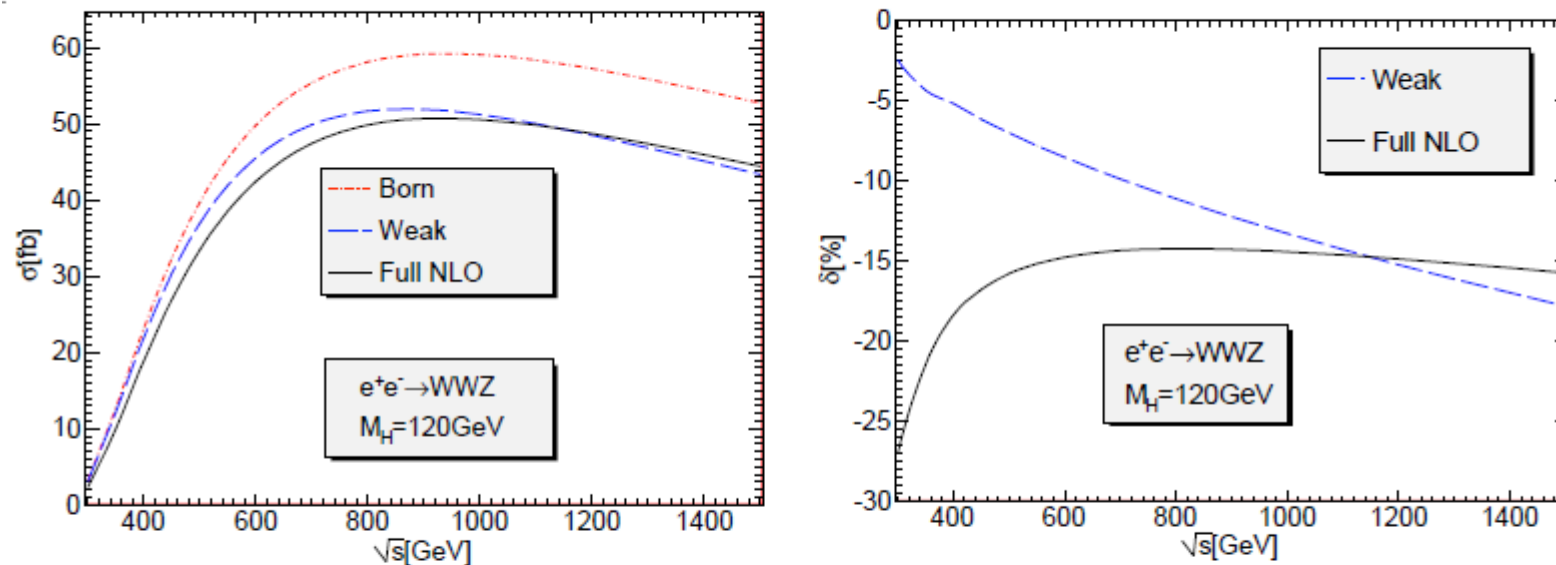
Input parameters: $\alpha_{G_\mu} = \sqrt{2}G_\mu s_W^2 M_W^2 / \pi = \alpha(0)(1 + \Delta r)$

$$\delta Z_e^{G_\mu} = \delta Z_e - \frac{1}{2}(\Delta r)_{1\text{-loop}}.$$

- Total Xsection peak about 1fb is at $\sqrt{s} \approx 550 \text{ GeV}$.
- The weak correction goes from -12% to -18% when $\sqrt{s}$ increases from 500GeV to 1TeV.

EW 1-loop tri-boson production(Le)

$$e^+e^- \rightarrow W^+W^-Z: \text{Total Xsection}$$



- Total Xsection peak about 50fb (50 times larger than σ_{ZZZ}) is at $\sqrt{s} \approx 900$ GeV.
- Large Sudakov corrections at high energies: $\propto \log(M_W^2/s)$, $\propto \log^2(M_W^2/s)$.
- The weak correction goes from -7% to -18% when $\sqrt{s}$ increases from 500GeV to 1.5TeV.

Light Higgs at LHC:CompHEP (Dubinin)

Example: regularization of the amplitude $pp \rightarrow \gamma + 3 \text{ jet}$ (QCD misidentification (or fake) background $[\text{jet} \rightarrow \gamma]$ to the light Higgs boson signal at the LHC in the channel $\gamma\gamma + \text{jets}$). 50 partonic subprocesses in the «hash-model» format, each of them includes 30-40 diagrams with 10-20 singularities. Total number of QCD diagrams about 2000

	subprocess	$\sigma, [\text{pb}]$	$\frac{\sigma}{\sigma_{\text{max}}}$
1	$u\#, u\# \rightarrow A, G, u\#, u\#$	514.1	0.36
2	$u\#, U\# \rightarrow A, G, u\#, U\#$	123.2	0.09
3	$u\#, U\# \rightarrow A, G, d\#, D\#$	0.3	0
4	$u\#, U\# \rightarrow A, G, G, G$	2.4	0
5	$u\#, d\# \rightarrow A, G, u\#, d\#$	208.1	0.15
6	$u\#, D\# \rightarrow A, G, u\#, D\#$	101.4	0.07
7	$u\#, G \rightarrow A, u\#, u\#, U\#$	52.5	0.04
8	$U\#, G \rightarrow A, u\#, d\#, D\#$	30.3	0.02
9	$u\#, G \rightarrow A, G, G, u\#$	1397.7	1
10	$U\#, u\# \rightarrow A, G, u\#, U\#$	125.7	0.09
11	$U\#, u\# \rightarrow A, G, d\#, D\#$	0.3	0
12	$U\#, u\# \rightarrow A, G, G, G$	2.4	0
13	$U\#, U\# \rightarrow A, G, U\#, U\#$	19.1	0.01
14	$U\#, d\# \rightarrow A, G, U\#, d\#$	41.9	0.03
15	$U\#, D\# \rightarrow A, G, U\#, D\#$	17.2	0.01
16	$U\#, G \rightarrow A, u\#, U\#, U\#$	8.5	0.01
17	$U\#, G \rightarrow A, U\#, d\#, D\#$	4.5	0
18	$U\#, G \rightarrow A, G, G, U\#$	196.5	0.14
19	$d\#, u\# \rightarrow A, G, u\#, d\#$	206.9	0.15
20	$d\#, U\# \rightarrow A, G, U\#, d\#$	41.9	0.03
21	$d\#, d\# \rightarrow A, G, d\#, d\#$	49.7	0.03
22	$d\#, D\# \rightarrow A, G, u\#, U\#$	0.1	0
23	$d\#, D\# \rightarrow A, G, d\#, D\#$	23.3	0.02
24	$d\#, D\# \rightarrow A, G, G, G$	0.4	0
25	$d\#, G \rightarrow A, u\#, U\#, d\#$	23.9	0.02

$d\#, G \rightarrow A, d\#, d\#, D\#$	8.0	0
$d\#, G \rightarrow A, G, G, d\#$	195.2	0.14
$D\#, u\# \rightarrow A, G, u\#, D\#$	98.7	0.07
$D\#, U\# \rightarrow A, G, U\#, D\#$	17.6	0.01
$D\#, d\# \rightarrow A, G, u\#, U\#$	0.1	0
$D\#, d\# \rightarrow A, G, d\#, D\#$	23.2	0.02
$D\#, d\# \rightarrow A, G, G, G$	0.4	0
$D\#, D\# \rightarrow A, G, D\#, D\#$	9.0	0
$D\#, G \rightarrow A, u\#, U\#, D\#$	9.6	0
$D\#, G \rightarrow A, d\#, D\#, D\#$	2.8	0
$D\#, G \rightarrow A, G, G, D\#$	69.1	0.05
$G, u\# \rightarrow A, u\#, u\#, U\#$	53.3	0.04
$G, u\# \rightarrow A, u\#, d\#, D\#$	29.7	0.02
$G, u\# \rightarrow A, G, G, u\#$	1400.0	1
$G, U\# \rightarrow A, u\#, U\#, U\#$	9.5	0
$G, U\# \rightarrow A, U\#, d\#, D\#$	4.5	0
$G, U\# \rightarrow A, G, G, U\#$	198.6	0.14
$G, d\# \rightarrow A, u\#, U\#, d\#$	23.8	0.02
$G, d\# \rightarrow A, d\#, d\#, D\#$	7.7	0
$G, d\# \rightarrow A, G, G, d\#$	190.9	0.13
$G, D\# \rightarrow A, u\#, U\#, D\#$	9.9	0
$G, D\# \rightarrow A, G, G, D\#$	2.9	0
$G, D\# \rightarrow A, G, G, D\#$	68.8	0.05
$G, G \rightarrow A, G, u\#, U\#$	277.9	0.20
$G, G \rightarrow A, G, d\#, D\#$	69.5	0.05
$pp \rightarrow A, j, j, j$	5970.4	

CompHEP (Dubinin)

New Features in CompHEP 4.4 (Interfaces)

- CompHEP->PYTHIA (CPYTH) (ready)
- CompHEP->PYTHIA-TAUOLA (ready)
- CompHEP->HERWIG (ready)
- CompHEP->HERWIG++ (in progress)
- Interfaced to Exp. Collaboration SW:
SIMDET(ILC), CMKIN(CMS), ATHENA(ATLAS) and D0
(Tevatron) Run II software.
- Macros of interface to ROOT graphics (in progress)
- Output Events are ready for LCG MCDB Data Base

Event generator

Strong request from experimentalists

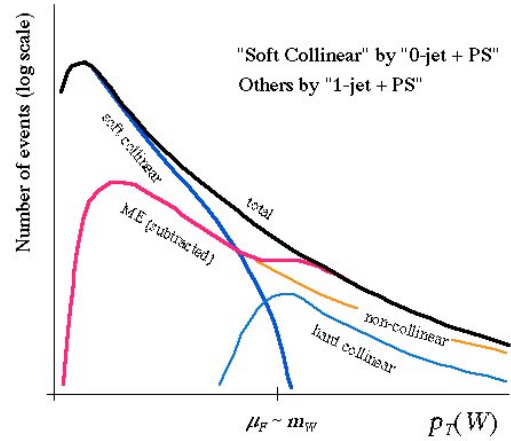
Cross section calculation etc. by theorists is NOT enough!

Generate 4-vectors of final state particles, hopefully in equal weights

“Requirement” list, or, what EG (Kurihara)

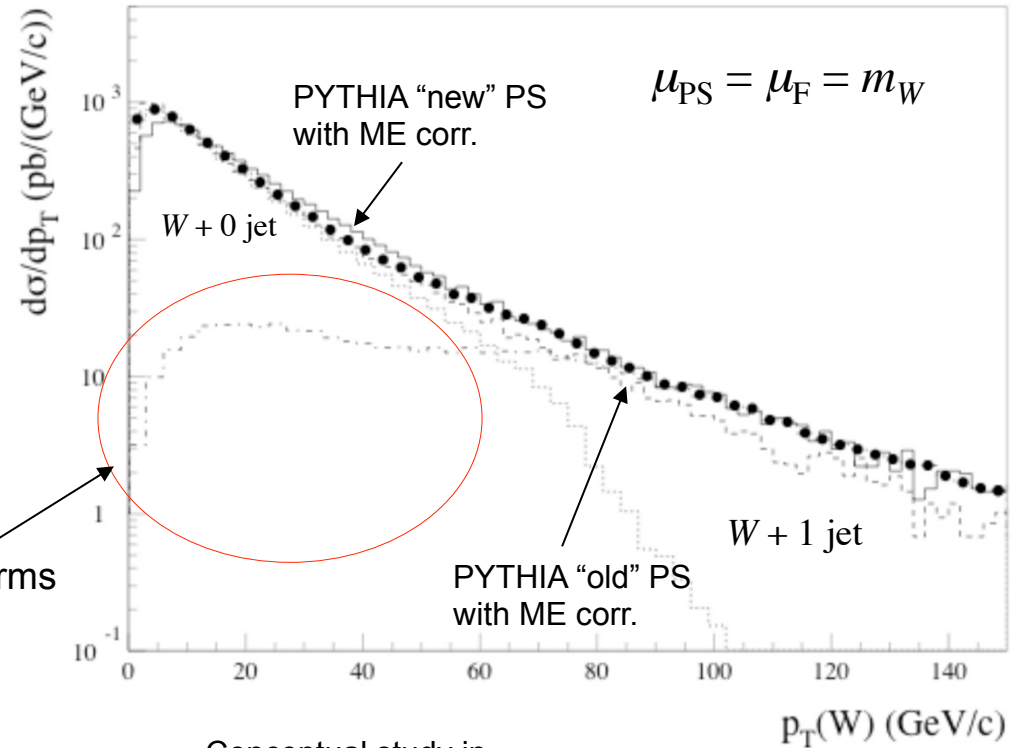
- What is a “must” for EG at LHC-era?
 - $\sigma_{\text{tree}} \times (\text{K-factor}) \rightarrow \text{NLO ME}$
 - ME/PS Matching
 - Fast & Stable Numerical Calculation
 - High Generation Efficiency
 - Fully Exclusive
 - Non-p Effects if necessary
 - LHA-Compliant Interface

W production @LHC(ODAKA)



My prospect at PhysSim WS
at KEK in 2004

Non-collinear terms



Conceptual study in

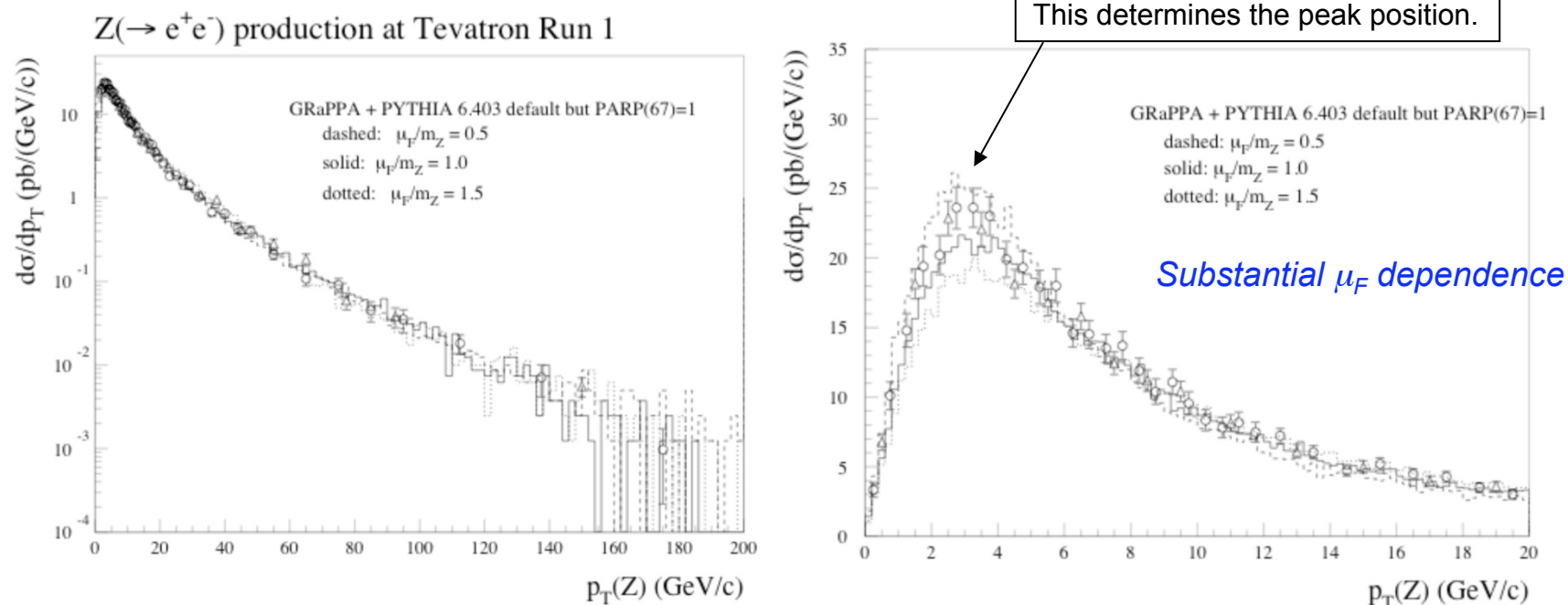
S. Odaka and Y. Kurihara, Eur. Phys. J. C 51 (2007) 867; hep-ph/0702138

Low- Q simulations by PYTHIA/HERWIG are yet to be applied.

Z production at Tevatron (ODAKA)

GR@PPA 2.8 + PYTHIA 6.4

PYTHIA for simulating soft PS ($1.0 < Q < 4.6$ GeV), **primordial k_T** ($\langle k_T \rangle = 2.0$ GeV/c), hadronization, and decays



Circles: CDF, Phys. Rev. Lett. 84, 845 (2000)

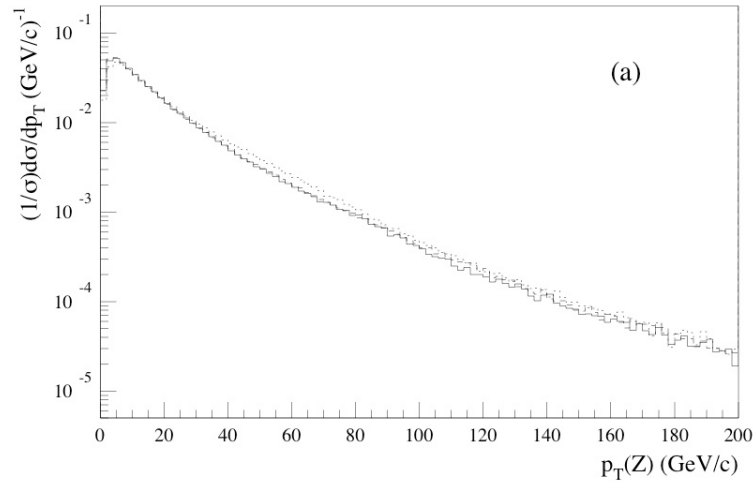
Triangles: D0, Phys. Rev. D 61, 032004 (2000) $\times 1.12$

D0 data and simulations are normalized to the total cross section of CDF.

Nearly perfect through the entire measurement range

No tunable parameter in GR@PPA

Z production @LHC (ODAKA)

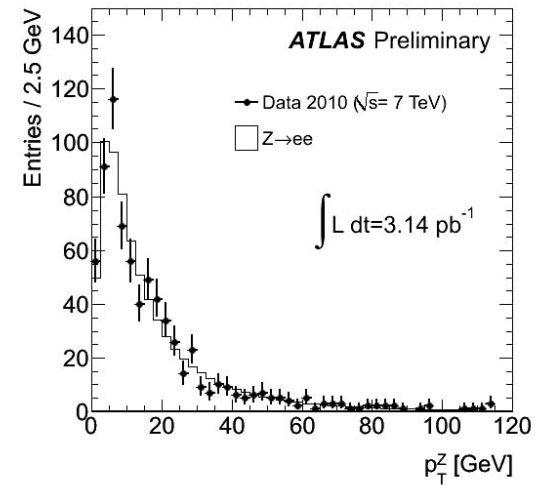
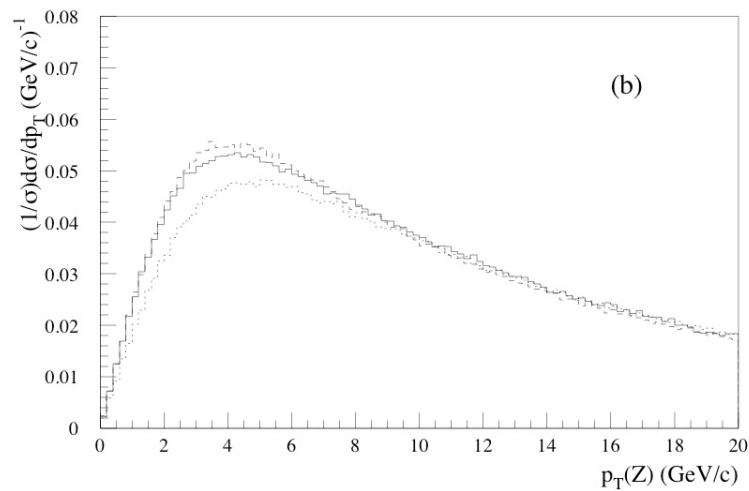


Solid: GR@PPA 2.8 + PYTHIA 6.421

Dashed: PYTHIA 6.421 built-in with new PS

Dotted: HERWIG 6.510

We will be able to plot measurement results soon.



Heavy quark mass effect on photon SF (Sasaki)

Master integral for 3-body phase-space

● The easiest master integral

$$\begin{aligned}
 & \text{Diagram: A circle with a vertical dashed line and a horizontal solid line intersecting at the center. Four external lines (two on the left, two on the right) meet the circle at the intersection points.} \\
 & = \int dP S^{(3)} \\
 & = S^{2\epsilon} \frac{s}{128\pi^3} \left(1 - \frac{4m^2}{s}\right)^{\frac{5}{2}} \left\{ 1 - \epsilon \left[3 \log\left(1 - \frac{4m^2}{s}\right) + 2 \log s - \psi^{(0)}\left(\frac{3}{2}\right) + \psi^{(0)}\left(\frac{1}{2}\right) \right] + \mathcal{O}(\epsilon^2) \right\} S_1\left(\frac{s}{4m^2}\right)
 \end{aligned}$$

$$\begin{aligned}
 S_1(a) = \frac{1}{4(1-a)^{\frac{5}{2}}} & \left\{ -3a^2 \log[a(1-a)] + 2a^2 \log[a + \sqrt{1-a} - 1] - a^2 (\tanh^{-1} \sqrt{1-a}) \right. \\
 & \left. + a\sqrt{1-a} + 2\sqrt{1-a} - 4a(1-a) \log[-a + \sqrt{1-a} + 1] + 2a \log[a(1-a)] \right\}
 \end{aligned}$$

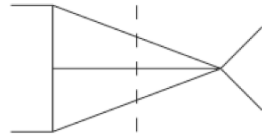
can be evaluated analytically

$$\beta_{12} = \beta_{12}(t, u)$$

● Other master integrals are difficult to calculate analytically

$$\begin{aligned}
 & \text{Diagram: A triangle with a vertical dashed line and a horizontal solid line intersecting at the center. Four external lines (two on the left, two on the right) meet the triangle at the intersection points.} \\
 & = \frac{1}{(4\pi)^D} \frac{1}{\Gamma(D-3)} (s-q^2)^{3-D} \int_0^\pi d\theta \sin^{D-3} \theta \int_0^\pi d\phi \sin^{D-4} \phi \int_0^{(s-q^2)(1-\frac{4m^2}{s})} dt \int_{q^2 t/(s-q^2)}^{(s-4m^2)-t} du \\
 & \left(1 - \frac{4m^2}{s-t-u}\right)^{\frac{D-3}{2}} \left\{ (s-t-u) t \left[(s-q^2)u - q^2 t \right] \right\}^{\frac{D-4}{2}} \frac{-2}{s-t-q^2} \frac{1}{\{1 + \beta_{12} \cos \theta\}}
 \end{aligned}$$

Heavy quark mass effect on photon SF (Sasaki)



$$= \frac{s}{128\pi^3} \left(1 - \frac{4m^2}{s}\right)^{\frac{5}{2}} \times \frac{-1}{s \left(1 - \frac{4m^2}{s}\right)^{\frac{1}{2}}} (1-x) \times S_{D0d}\left(\frac{4m^2}{s}, x\right)$$

$$S_{D0d}(a, x) \equiv \int_0^1 dy \int_0^1 dz \frac{1-y}{\sqrt{\tilde{A}}} \log \left| \frac{2A + B + 2\sqrt{A(A+B+C)}}{-2A + B + 2\sqrt{A(A-B+C)}} \right|$$

$$\tilde{A} = \left[1 - y(1-a)\right]^2 + 2(1-x)(1-a) \left[-(1-a)y^2z + y(1+a-az) + z - 1\right] + (1-x)^2(1-a)^2 \left[1 - (1-y)\right]$$

$$A = s^2 \frac{1-a}{(1-x)^2} \frac{(1-y)z}{a + (1-a)(1-y)z} \left\{ \left[1 - y(1-a)\right]^2 + 2(1-x)(1-a) \left[-(1-a)y^2z + y(1+a-az) + z - 1\right] + (1-x)^2(1-a)^2 \left[1 - (1-y)z\right]^2 \right\}$$

$$B = 2s^2 \sqrt{\frac{(1-a)(1-y)z}{a + (1-a)(1-y)z}} \frac{(1-a)(1-x)(1-y)z + (1-a)(x+y) + a}{(1-x)^2[1-y(1-a)]} \left\{ \left[1 - y(1-a)\right]^2 - (1-x)(1-a) \left[(1-y)(1-z) - y\right] \right\}$$

$$\sqrt{A+B+C} = \frac{s}{(1-x)} \left[(1-a)(1-x)(1-y)z + (1-a)(x+y) + a \right] + \frac{s}{(1-x)[1-y(1-a)]} \sqrt{\frac{(1-a)(1-y)z}{a + (1-a)(1-y)z}} \times \left\{ \left[1 - y(1-a)\right]^2 - (1-x)(1-a) \left[(1-y)(1-z) - y\right] \right\}$$

● Most of the master integrals for real emission are hard to be calculated analytically

● Numerical analysis of these master integrals are in progress.

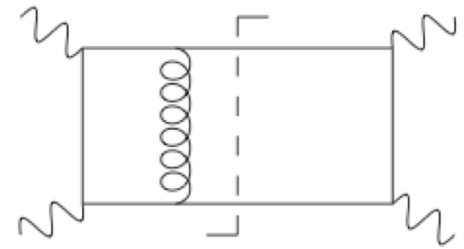
Heavy quark mass effect on photon SF (Sasaki)

- The heavy quark mass effects on the photon structure functions are investigated in parton model up to the NLO
- Using Cutkosky rule and reduction method, structure functions are expressed in terms of the master integrals.
- The master integrals for virtual corrections are evaluated

Ultraviolet divergence are canceled

Infrared divergence are remained

should be canceled when contribution of real gluon emission diagrams is added



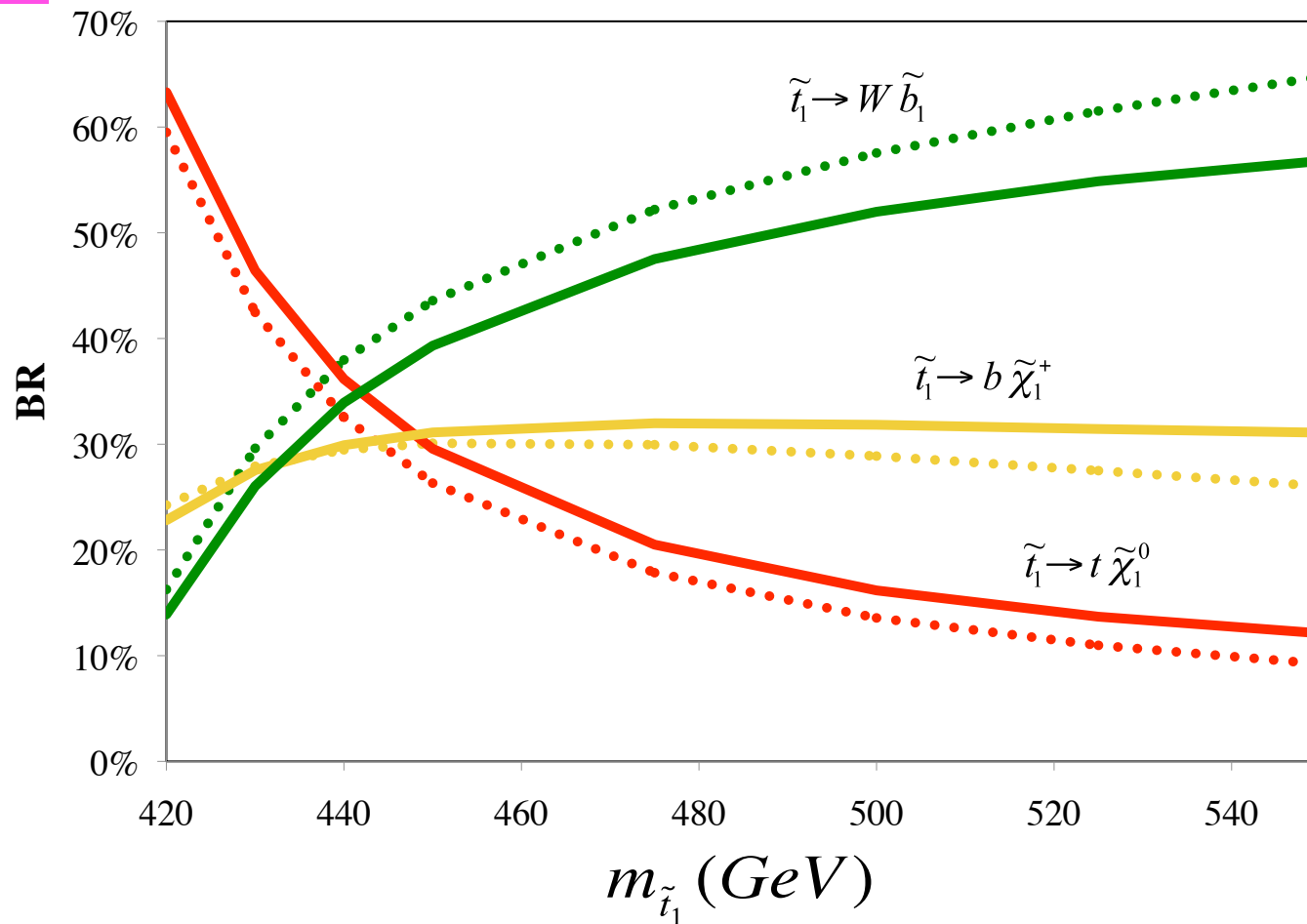
- Analysis of the real gluon emission diagrams in progress

MSSM 1-loop corrections (Kon)

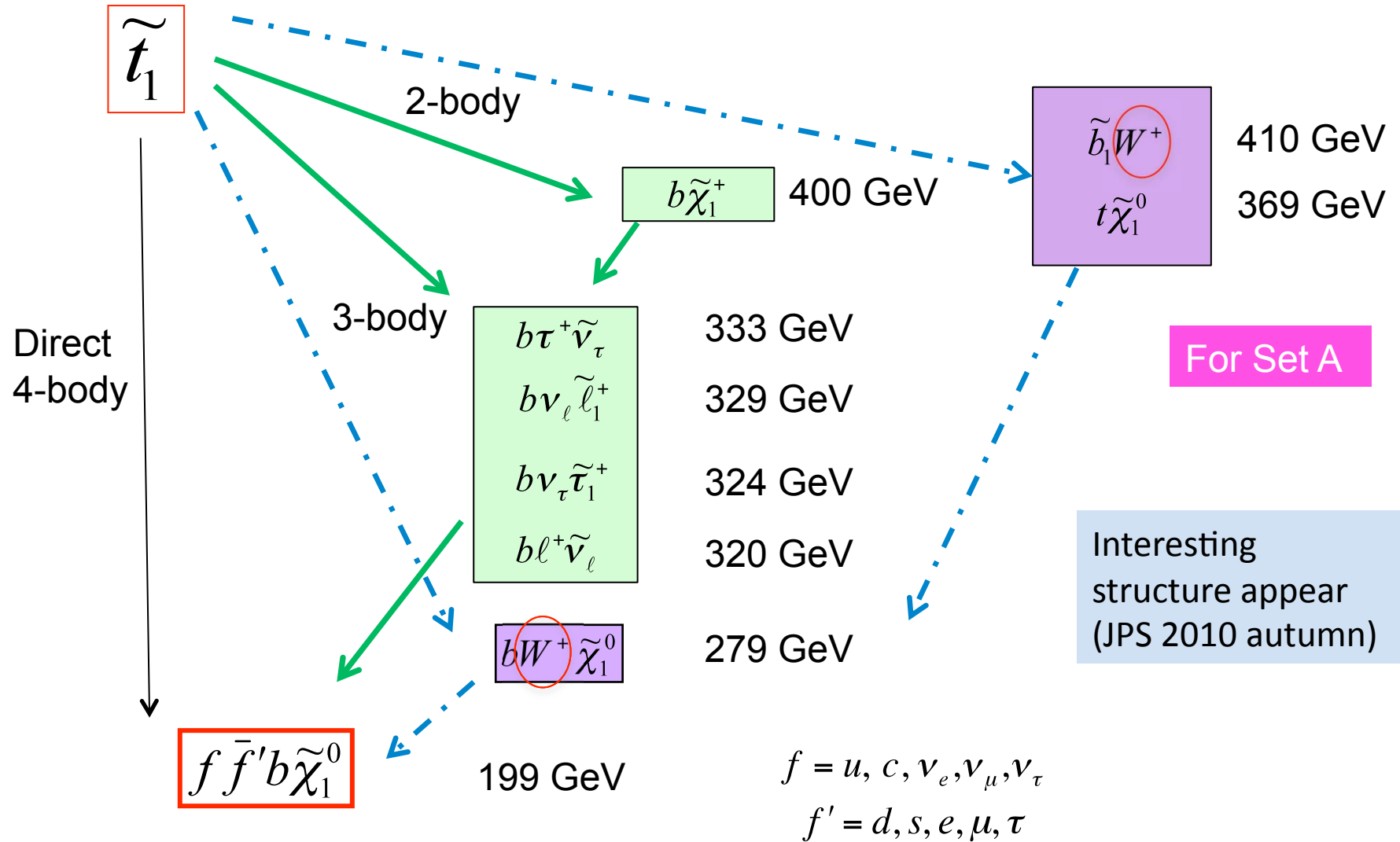
$m_{\tilde{t}_1}$ dependence of branching ratios

For Set A

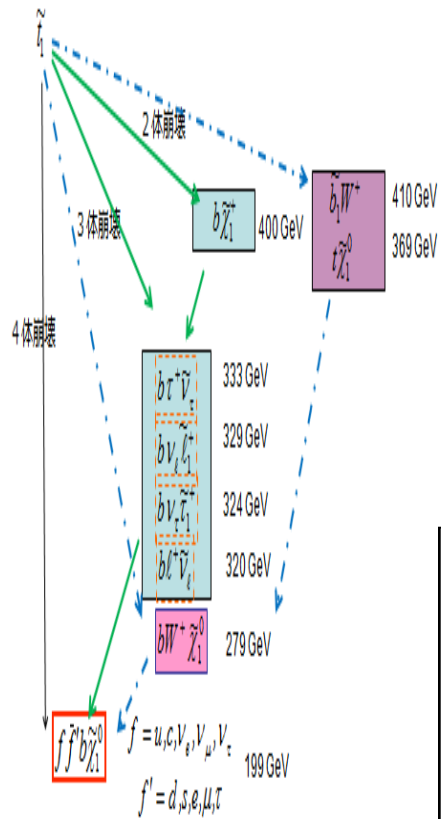
----- tree
—— 1-loop
(QCD + ELW)



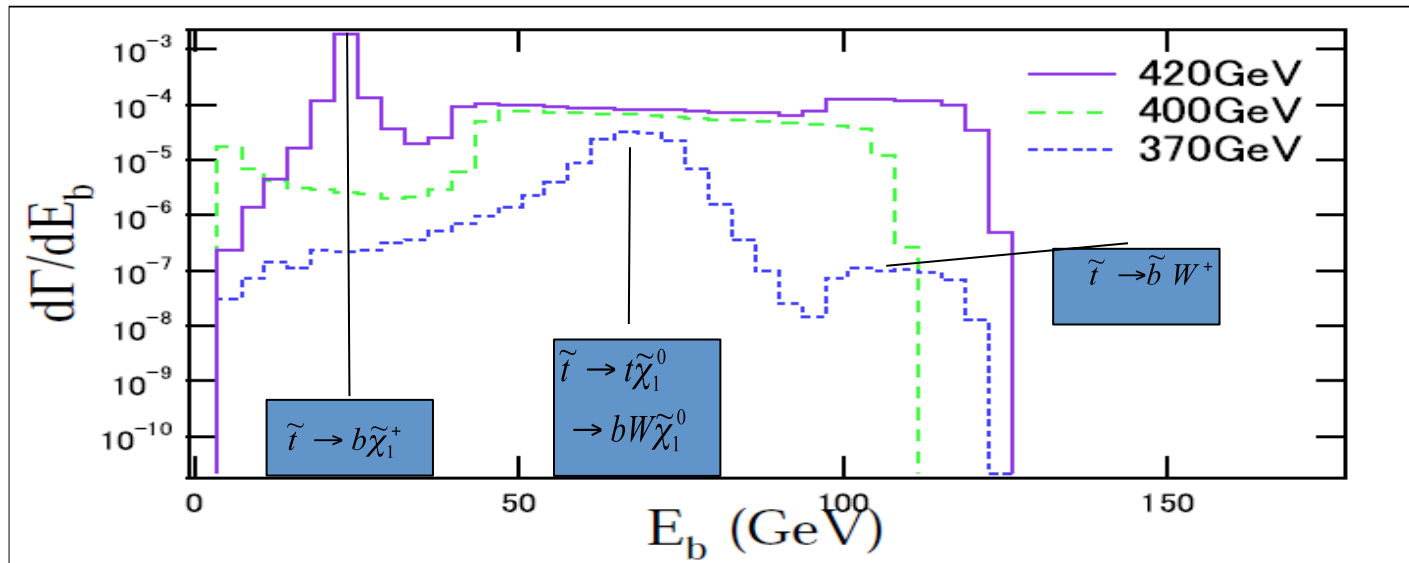
Analysis of 4-body decays for a parameter set (Kon)



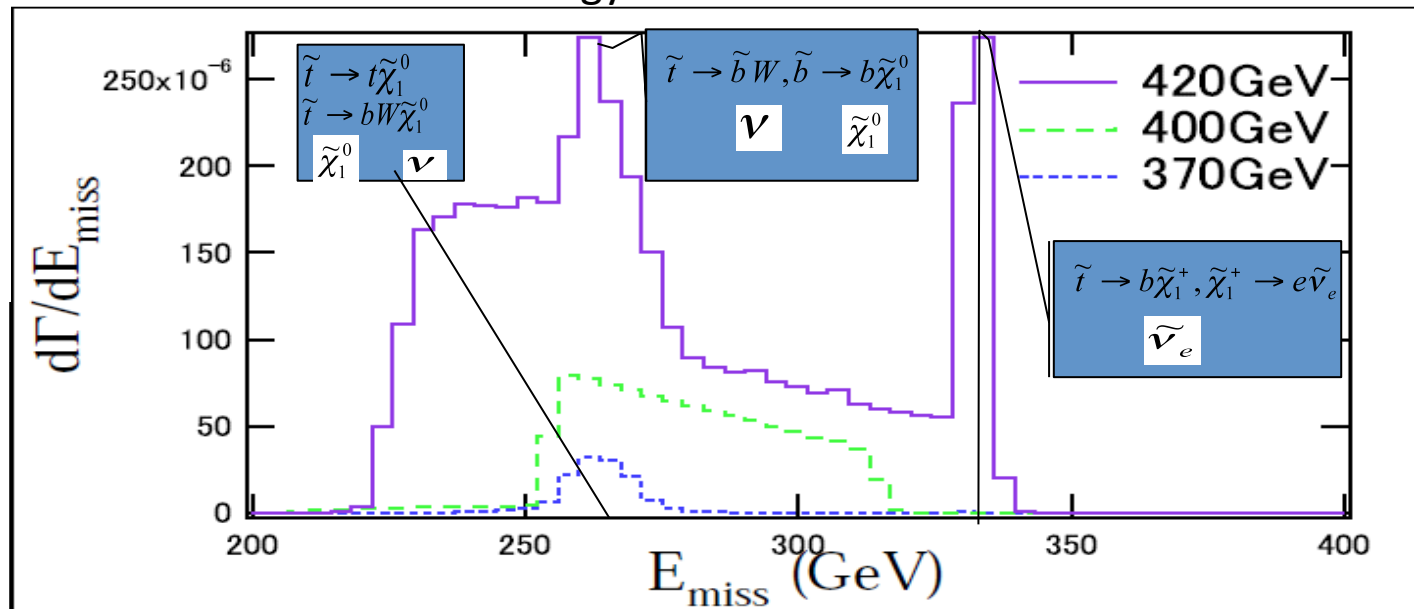
$$\tilde{t} \rightarrow e^+ \nu_e b \tilde{\chi}_1^0$$



Energy distribution of b-quark



Invisible energy distribution



How to confirm

Systematic check of the computation : Large scale, hard to check

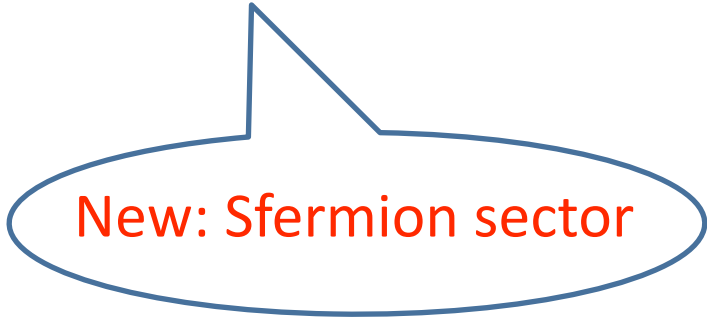
UV cancelation

IR cancelation

Interchange ordering

Gauge invariance check

... NLG mode ([Jimbo's talk](#), [Le's talk](#)) : useful



New: Sfermion sector

Final words

- “Computation” is essential for the comparison between experiment and theory
-> Study SM, and also BMS
- Automatic computation is an indispensable tool for current and future HEP
-> produce theoretical prediction with enough accuracy
-> computers are the ‘detectors’ for theorists
- Armored by the automated system, we have obtained important physical results and also have contributed to the event generator development.

Final words(cont.)

- Acceleration of hardware and parallelization, high-speed algorithm, symbolic systems, reliability, ... are important for ultra-size computation.

(8) It is impossible to predict what a human will do.

FUTURE: Let's make unpredictable progress by human power.