

Recent Physical Results using GRACE/SUSY

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(presented by T.Kon)



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\$ Introduction

- SUSY model
 - : a hopeful candidate for the BSM
 - * naturalness, dark-matter, gauge unification
 - : many new particles with mass $O(\text{TeV})$ are predicted
- SUSY-particles = sparticles (and light Higgs)
 - : important targets of High Energy Exp & Obs
- We must handle a large number of Feynman diagrams in the SUSY phenomenology



GRACE/SUSY

\$ GRACE/SUSY

* tree ver. Ref. **Comput.Phys.Commun.153:106-134,2003**

download : <http://minami-home.kek.jp/>

* 1-loop ver. Ref. **Phys.Rev.D75:113002,2007**

Cf. Jimbo-san's talk
"sfermion NLG"

Input file (example)

Tree

$$\tilde{t}_1 \rightarrow b e^+ \tilde{\nu}_e$$

1-loop (QCD)

```
Model="mssm.mdl";  
Process;  
  elwk = {2}; qcd = {0};  
  Initial={st1};  
  Final  ={b positron snu-e};  
  kinem="1301";  
Pend;
```

```
Model="mssmnlg_j2_q.mdl";  
Process;  
  elwk = {2,2}; qcd = {0,2};  
  Initial={st1};  
  Final  ={b positron snu-e};  
  kinem="1301";  
Pend;
```

\$ MSSM parameter sets for stop decay

- Why stop decay ?

$$\begin{pmatrix} \tilde{t}_L \\ \tilde{t}_R \end{pmatrix} \leftrightarrow \begin{pmatrix} t_L \\ t_R \end{pmatrix} \quad -L_t^{mass} = \begin{pmatrix} \tilde{t}_L^* & \tilde{t}_R^* \end{pmatrix} \begin{pmatrix} m_{\tilde{t}_L}^2 & m_{\tilde{t}_{LR}}^2 \\ m_{\tilde{t}_{LR}}^2 & m_{\tilde{t}_R}^2 \end{pmatrix} \begin{pmatrix} \tilde{t}_L \\ \tilde{t}_R \end{pmatrix}$$

$$\begin{pmatrix} \tilde{t}_1 \\ \tilde{t}_2 \end{pmatrix} = \begin{pmatrix} \cos \theta_t & \sin \theta_t \\ -\sin \theta_t & \cos \theta_t \end{pmatrix} \begin{pmatrix} \tilde{t}_L \\ \tilde{t}_R \end{pmatrix} \quad m_{\tilde{t}_{LR}}^2 \equiv -m_t(\mu \cot \beta + A_t)$$

$$m_{\tilde{t}_1}^2 = \frac{1}{2} \left[(m_{\tilde{t}_L}^2 + m_{\tilde{t}_R}^2) \mp \sqrt{(m_{\tilde{t}_L}^2 - m_{\tilde{t}_R}^2)^2 + 4m_{\tilde{t}_{LR}}^4} \right]$$

Possibly

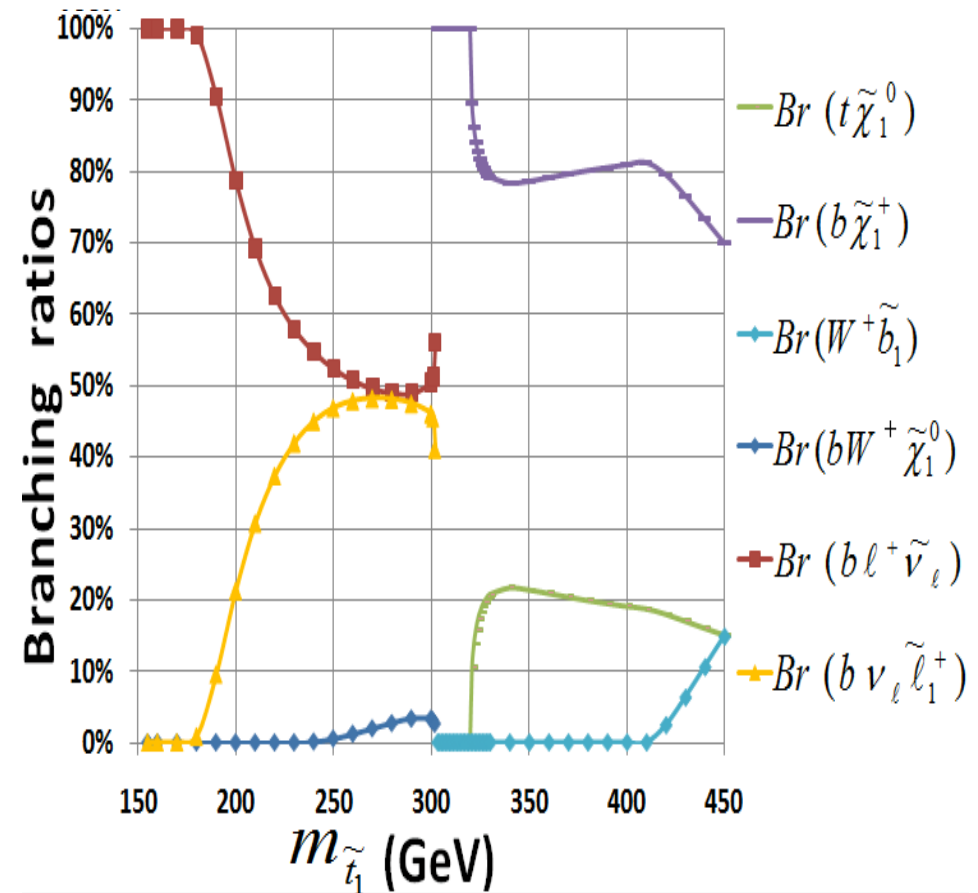
- $m_{\tilde{t}_1} < m_{\tilde{q}}$ $\tilde{q} = \tilde{u}, \tilde{d}, \tilde{c}, \tilde{s}, \tilde{b}$
- simple 2-body decay modes : Forbidden
 $\tilde{t}_1 \not\rightarrow t\tilde{\chi}_1^0 \quad \tilde{t}_1 \not\rightarrow t\tilde{g}$

☆ mass, decay modes
: depend sensitively on
MSSM parameters

- Typical MSSM parameter sets

	Set A	Set B
$\tan\beta$	10	10
μ	-750	-750
M_2	400	300
$m_{\tilde{\chi}_1^0}$	194.6	146.1
$m_{\tilde{\chi}_1^+}$	396.1	298.0
$m_{\tilde{g}}$	1390	1042
θ_t	0.8π	0.8π
$m_{\tilde{\ell}_1}$	325.0	170.0
$m_{\tilde{\nu}_\ell}$	317.0	150.0

(masses in GeV)



\$ 1-loop correction for decay widths

of Feynman diagrams

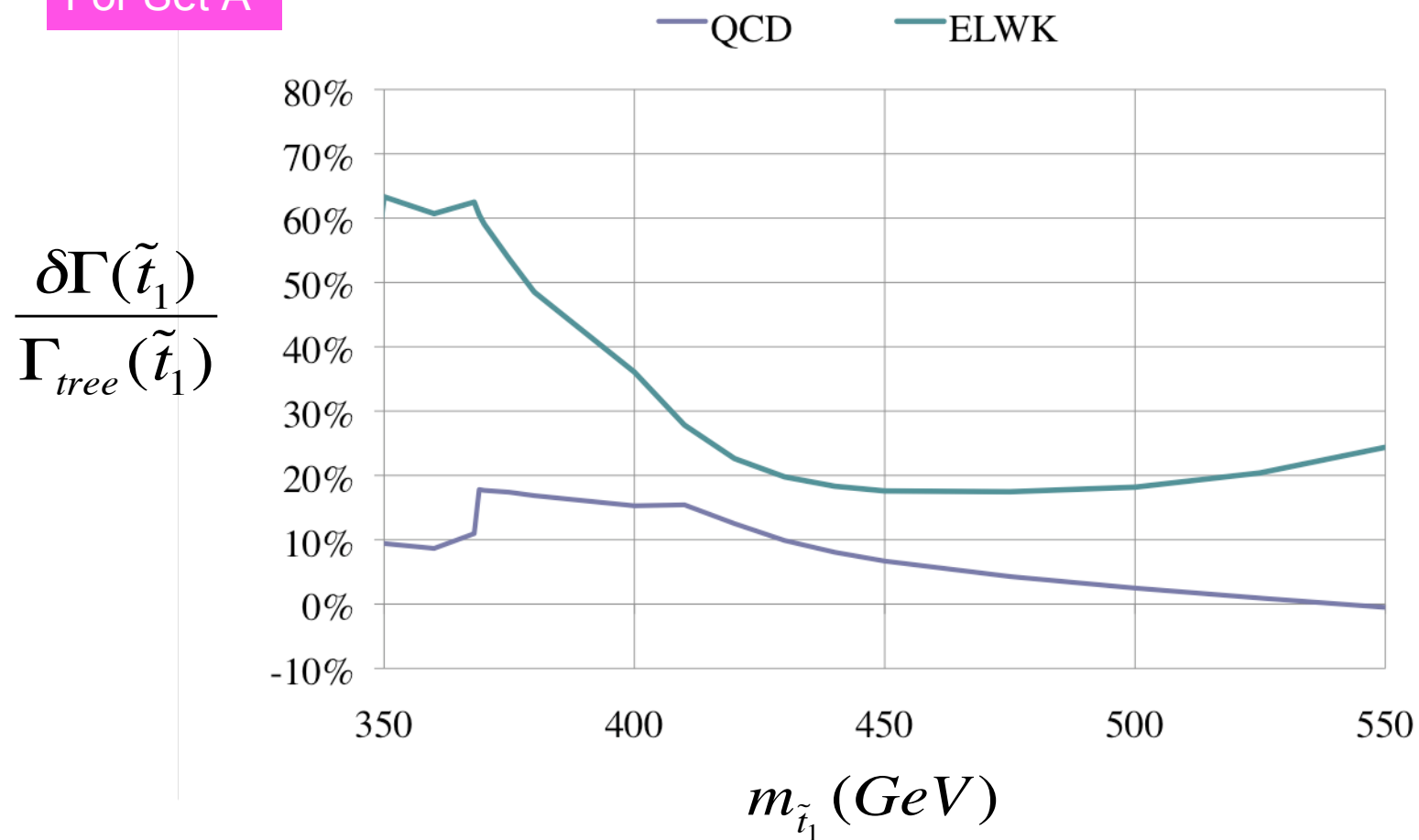
	Tree	QCD	ELWK
$\tilde{t}_1 \rightarrow W^+ b \tilde{\chi}_1^0$	5	78	1786
$\tilde{t}_1 \rightarrow b \ell^+ \tilde{\nu}_\ell$	2	12	490
$\tilde{t}_1 \rightarrow b \nu_\ell \tilde{\ell}_1^+$	2	12	426
$\tilde{t}_1 \rightarrow b \tilde{\chi}_1^+$	1	6	86
$\tilde{t}_1 \rightarrow t \tilde{\chi}_1^0$	1	6	104
$\tilde{t}_1 \rightarrow \tilde{b}_1 W^+$	1	17	126

For Set A

For Set B

$m_{\tilde{t}_1}$ dependence of corrections for total width

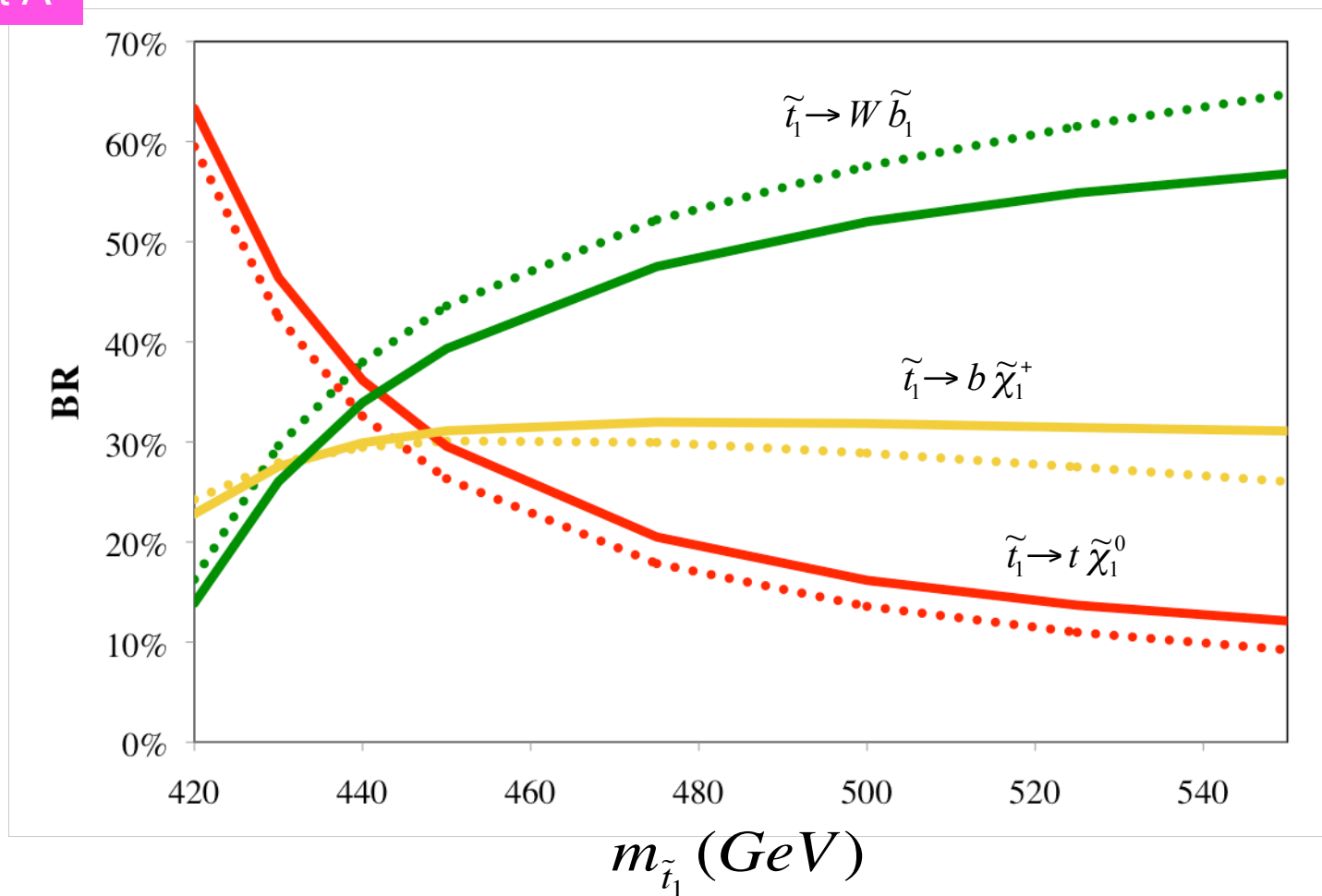
For Set A



$m_{\tilde{t}_1}$ dependence of branching ratios

For Set A

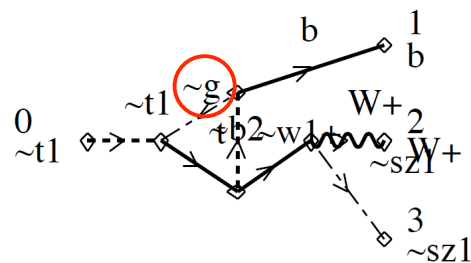
----- tree
—— 1-loop
(QCD + ELW)



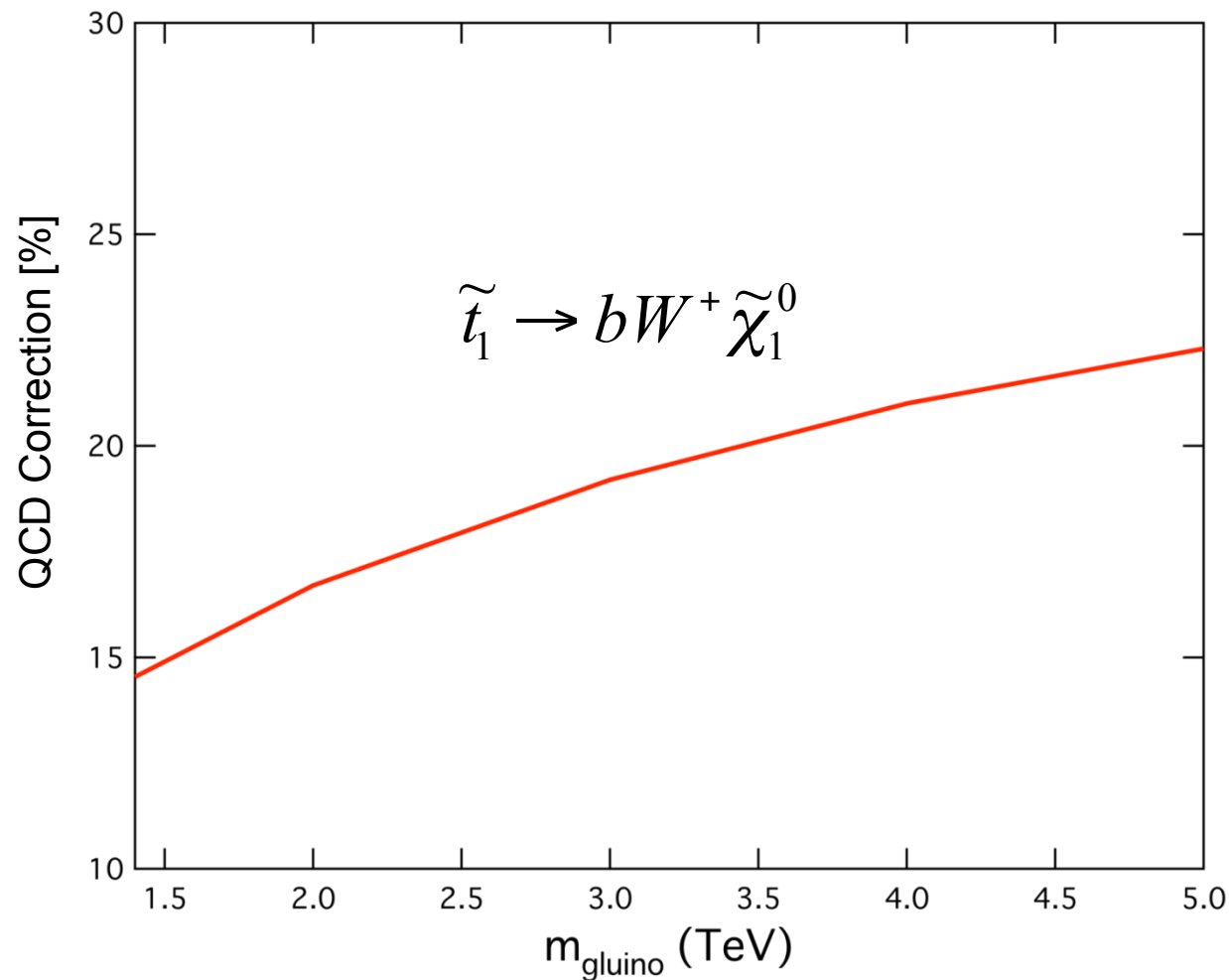
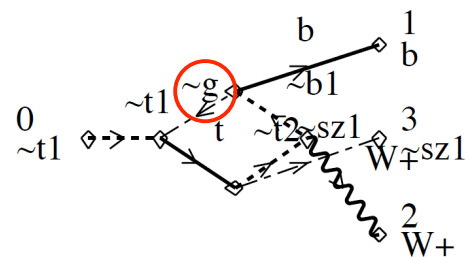
$m_{\tilde{g}}$ dependence of QCD corrections

For Set A

Graph 22

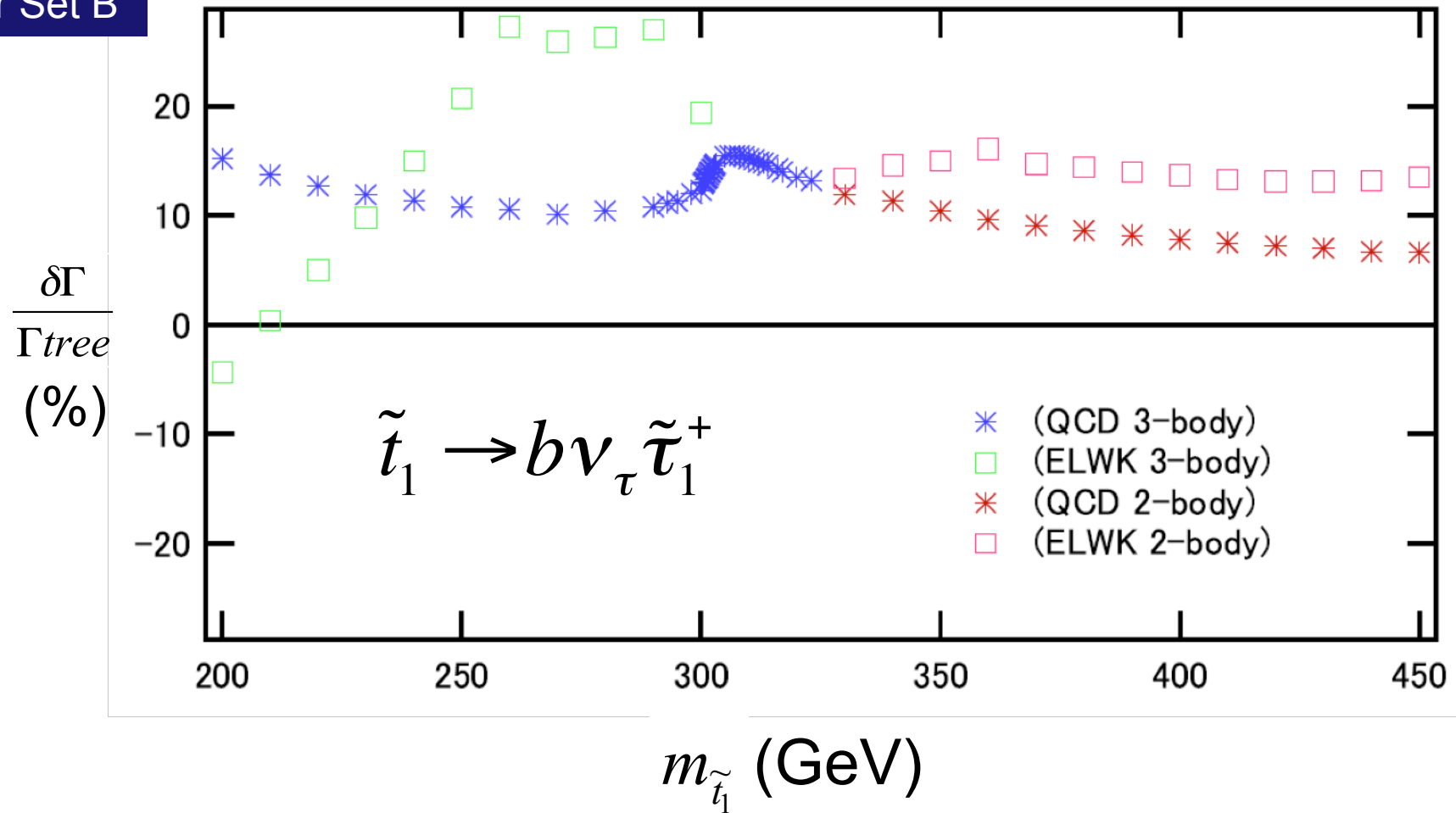


Graph 32

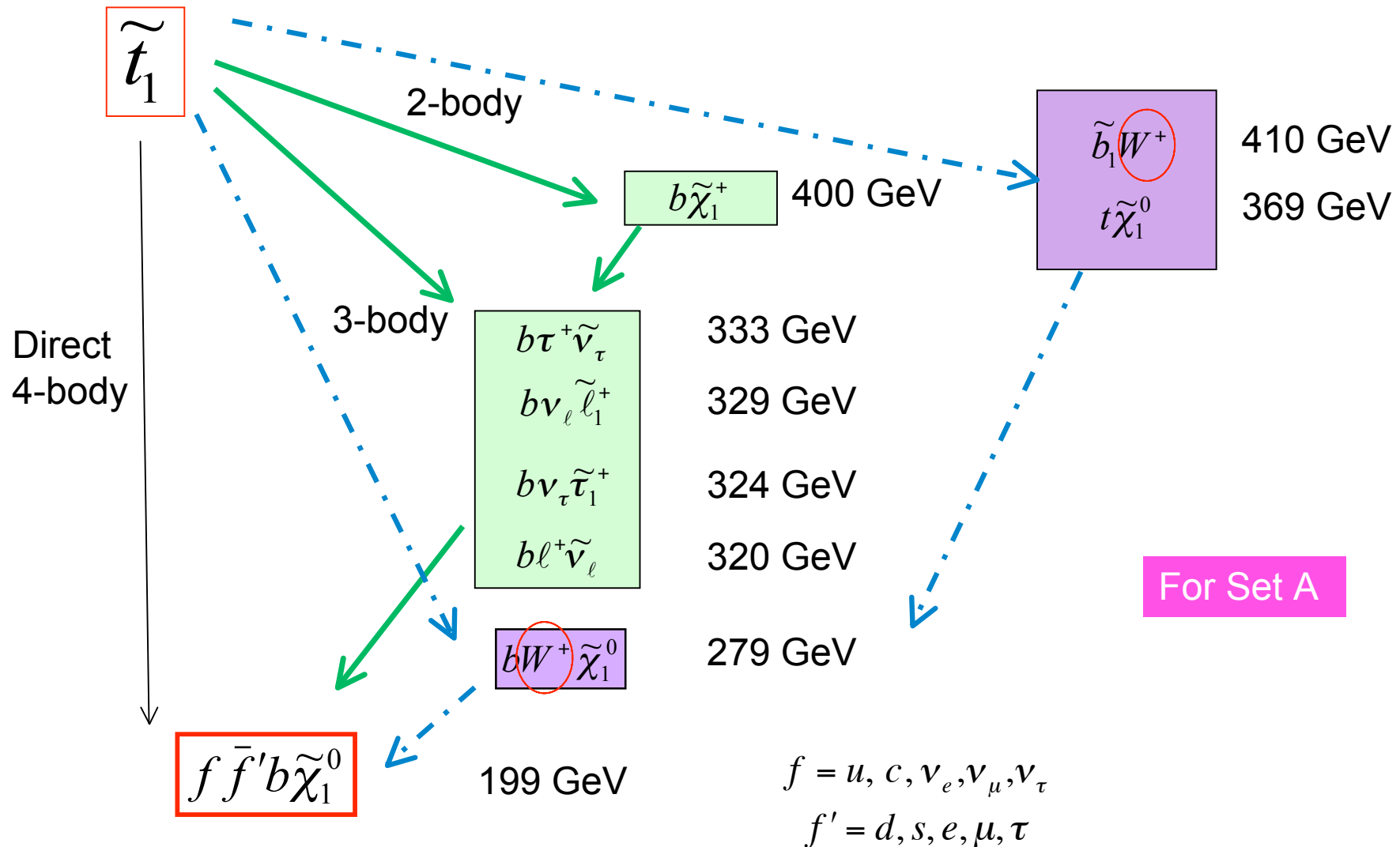


$m_{\tilde{t}_1}$ dependence of corrections for partial width

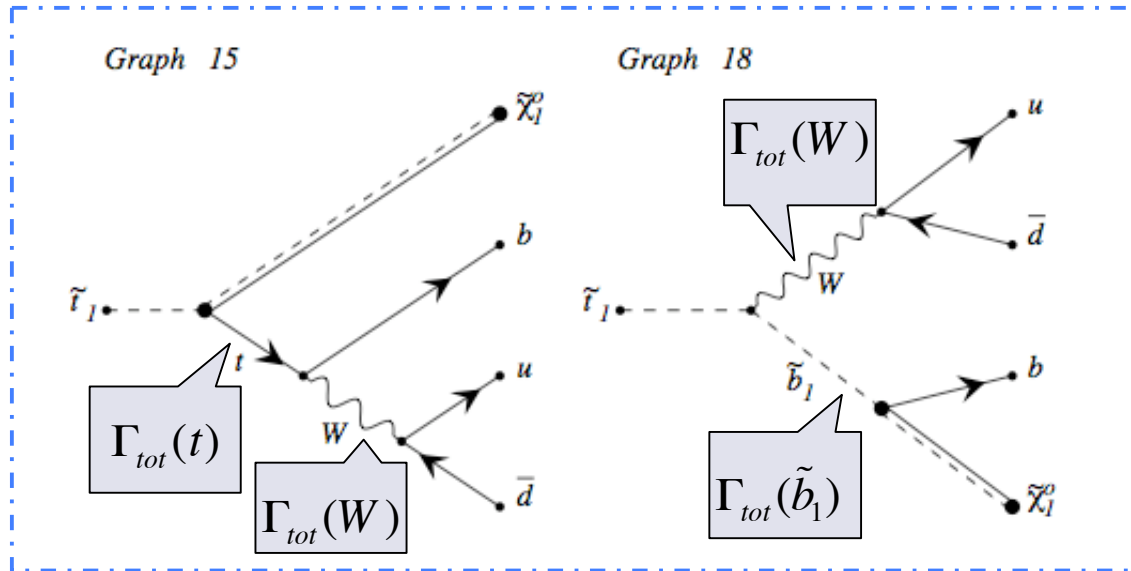
For Set B



\$ Analysis of 4-body decays

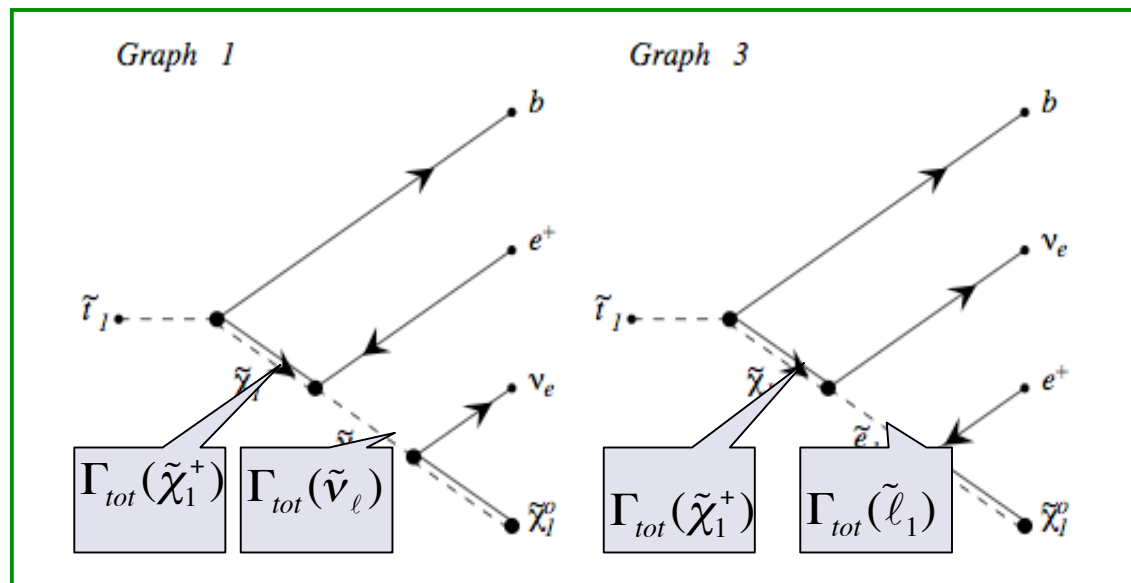


Feynman diagrams for “W-mode” and “lepton-mode”



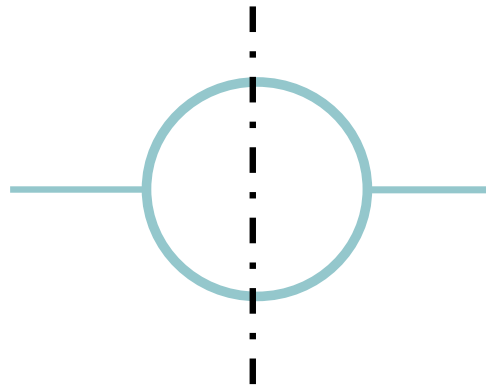
To obtain accurate
cascade decay width

We need
Correct total decay
widths
Of corresponding
particles



Systematic calculation of total decay widths with 1-loop 2-point function library in GRACE/SUSY- loop

	GeV
$\Gamma(\tilde{b}_1)$	0.0801
$\Gamma(\tilde{\chi}_1^+)$	1.0622
$\Gamma(\tilde{\nu}_e)$	0.1545
$\Gamma(\tilde{e}_1)$	0.1795



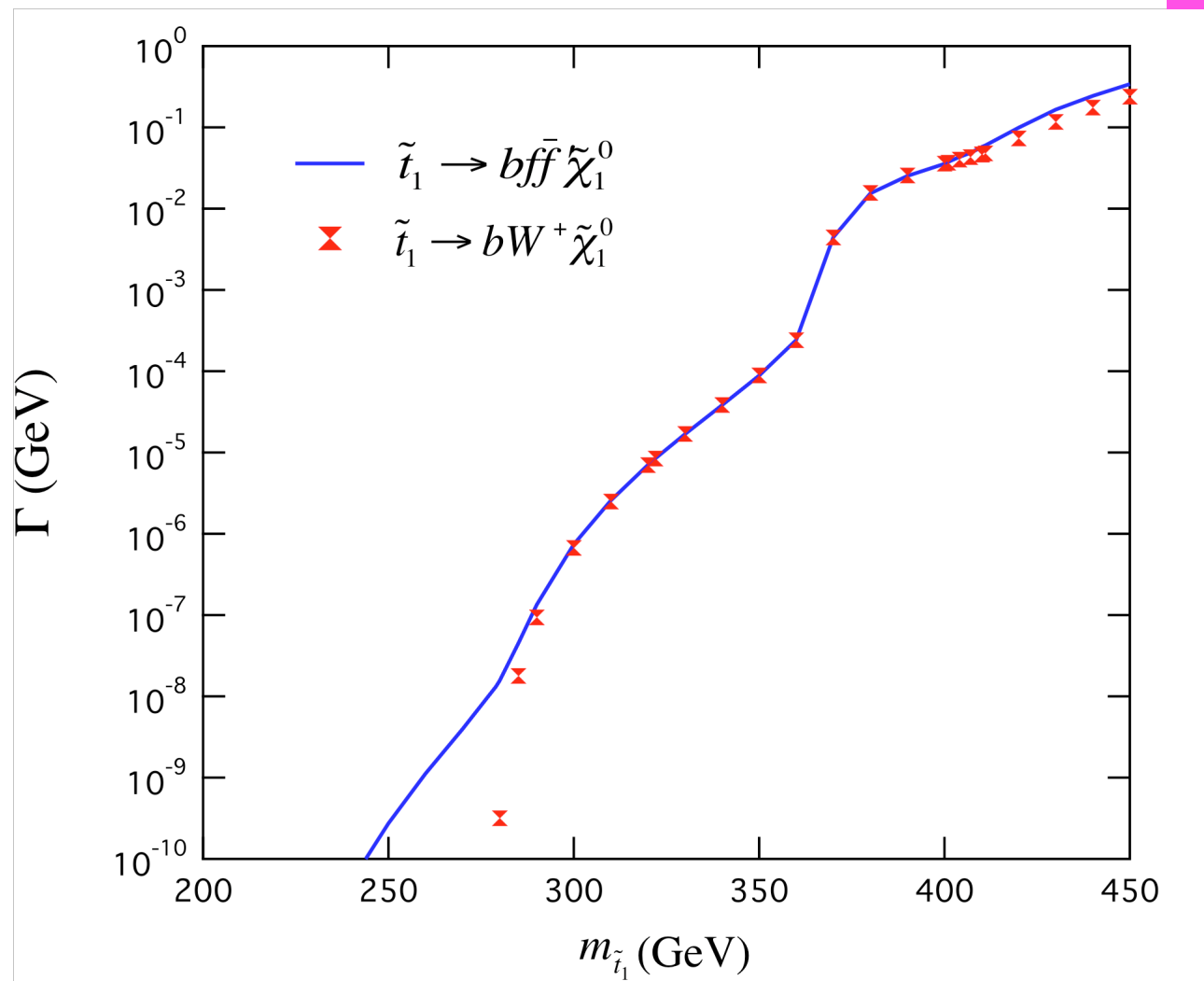
$$\Gamma_S = -\frac{\text{Im} \sum_s^S(m_s^2)}{m_s}$$

$$\Gamma_F = -2 \text{Im}(\sum_f^S(m_f^2) + m_f \sum_f^V(m_f^2))$$

All 2-point functions : automatically calculated

$m_{\tilde{t}_1}$ dependence of total width

For Set A





\$ Summary

- Various stop decays :
calculated using GRACE/SUSY
- QCD and ELW 1-loop corrections :
both important for SUSY phenomenology
with high accuracy
- 1-loop 2-point function library :
useful in calculation of cascade decays
of heavy sparticles