

GR@PPA Event Generator

GRACE-based event generators for hadron collision interactions

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GR@PPA

GRace @ Proton-Proton/Anti-proton

An extension of **GRACE** to hadron-collision interactions

$$\frac{d\sigma_{h_1 h_2 \rightarrow A+X}(s)}{d\Phi_A} = \sum_{a,b,i} \int_0^1 dx_1 \int_0^1 dx_2 f_{h_1 \rightarrow a}(x_1, \mu_F^2) f_{h_2 \rightarrow b}(x_2, \mu_F^2) \delta(\hat{s} - x_1 x_2 s) \frac{d\hat{\sigma}_{ab \rightarrow A_i}(\hat{s})}{d\hat{\Phi}_{A_i}}$$

Flavor sum
Parton distribution function (PDF)
GRACE

Initial state: variable flavor/momentum according to PDF
 Final state: generalization of quarks and gluons as "jets"

General features

Derivation of many subprocesses from a base process

C/P inversions, flavor/mass/coupling exchanges

→ Reduction of the program size

e.g., all $Z + 1$ jet production processes are derived from $u\bar{u} \rightarrow Z + g$ and $ug \rightarrow Z + u$.

Multi-process support

Automatic event mixing

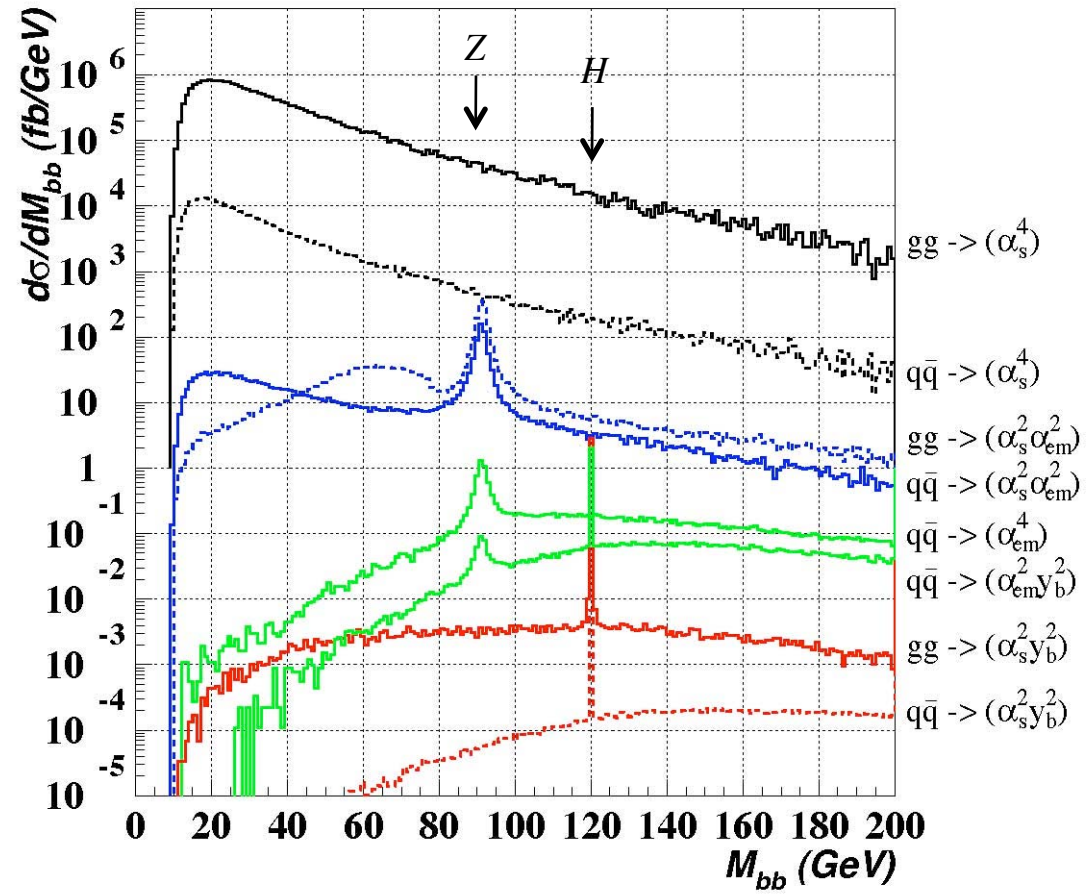
Interface to general-purpose event generators

GR@PPA is a parton-level event generator.

History of GR@PPA

- Jan. 2000: [NLO Working Group](#) was established.
- Oct. 2000: ACAT2000 (FNAL)
 - Talk by S. Odaka, *Integration of GRACE and PYTHIA*
- Feb. 2001: Tsuno named the 4b event generator as GR@PPA_4b.
- **Apr. 2002: GR@PPA_4b 1.0 released**
 - All $b\bar{b}b\bar{b}$ production processes including those mediated by Z and H
 - Interface to PYTHIA 6.1
 - [S. Tsuno et al., Comput. Phys. Commun. 151 \(2003\) 216](#); hep-ph/0204222
- Apr. 2003: GR@PPA_4b 2.0 released
 - LHA interface supported
- Feb. 2004: GR@PPA_ALL 2.6 released
 - W + (0-3) jets, Z + (0-2) jets, diboson (W^+W^- , ZW, ZZ), top pair were added.
- **Feb. 2006: GR@PPA 2.7 released**
 - W + 4 jets, Z + (3-4) jets, diboson + (1-2) jets, top pair + 1 jet, QCD (2-4) jets were added.
 - [S. Tsuno et al., Comput. Phys. Commun. 175, 665 \(2006\)](#); hep-ph/0602213

GR@PPA_4b



$\sqrt{s} = 14 \text{ TeV}$ at LHC (CTEQ6L, $p_T > 20 \text{ GeV}$, $|\eta| < 2.5$, $\Delta R < 0.4$)

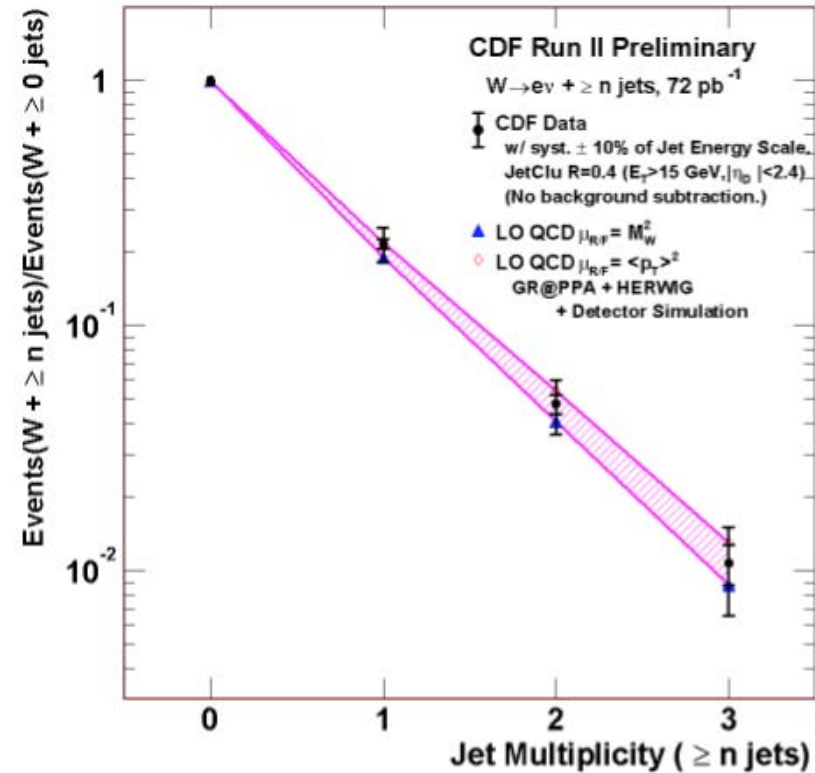
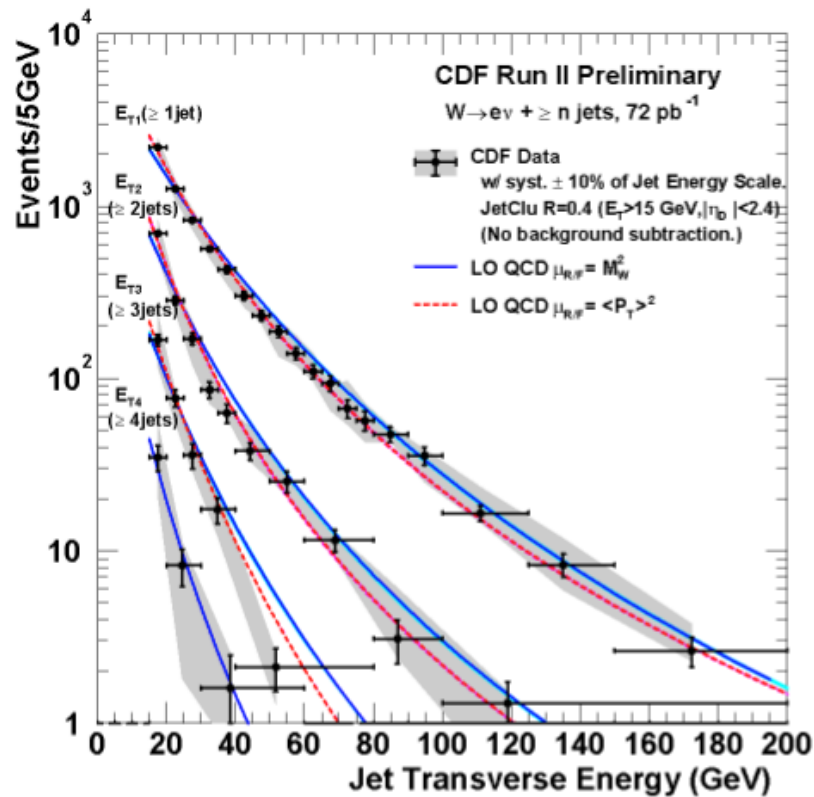
Condition given at the MC4LHC WS 2003

Cross section (pb)	Number of jets				
$W^-(e^- \nu_e) + n \text{ jets}$	0	1	2	3	4
ALPGEN	3904(6)	1013(2)	364(2)	136(1)	53.6(6)
MadEvent	3902(5)	1012(2)	361(1)	135.5(3)	53.6(2)
GR@PPA	3905(5)	1013(1)	361.0(7)	133.8(3)	53.8(1)

$W^+(e^+ \nu_e) + n \text{ jets}$	0	1	2	3	4
ALPGEN	5423(9)	1291(13)	465(2)	182.8(8)	75.7(8)
MadEvent	5433(8)	1277(2)	464(1)	182(1)	75.9(3)
GR@PPA	5434(7)	1273(2)	467.7(9)	181.8(5)	76.6(3)

W + jets at Tevatron Run II

PhD thesis of S. Tsuno (U. Tsukuba)



GR@PPA has some advantages against other event generators:

Heavy particle decays in matrix elements

Top pair production is a six-body process.

→ Exact spin/phase-space effects at the tree level

Support of multi-jet production processes

However,

Reliable only in those events having a large separation
between jets, due to a double-count problem

Double-count problem

A double counting of parton radiation effects in matrix elements (ME) and parton showers (PS) or PDF

The problem exists even if we do not apply PS, since the same radiation effects are included in PDF.

Several solutions (ME-PS matching) have been proposed and implemented in event generators.

ME correction in PYTHIA/HERWIG

CKKW method in Sherpa and MLM prescription in AlpGen
for multi-jet productions

a subtraction method in MC@NLO

a suppression method in POWHEG

NLO Working Group (NLO-WG)

<http://atlas.kek.jp/physics/nlo-wg/index.html>

A collaboration of people from Minami-Tateya group
and ATLAS-Japan group

Goal

Development of **NLO event generators** for multi-particle production
processes at hadron collisions based on GRACE

Dream

Automatic generation of NLO event generators

The purpose of GR@PPA is to establish a
framework for the event generation.

NLO event generators necessarily include radiative processes.

→ The **double counting** is a problem which must be solved in
NLO event generators.

Our solution to the problem

Leading-Log (LL) subtraction

The doubly counted radiation contributions are numerically subtracted from matrix elements of radiative processes.

$$\left| M_{A+1}(\hat{s}_{A+1}, \hat{\Phi}_{A+1}) \right|^2 - \left| M_A(\hat{s}_A, \hat{\Phi}_A) \right|^2 \times f_{LL}(Q^2, z = \hat{s}_A / \hat{s}_{A+1})$$

radiation factor
leading-log approximation

Subtracted are the divergent terms of radiative processes.

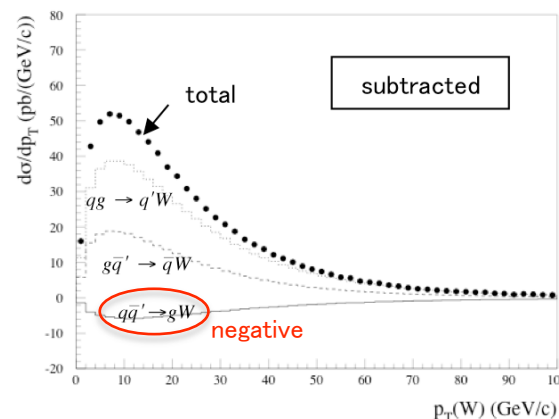
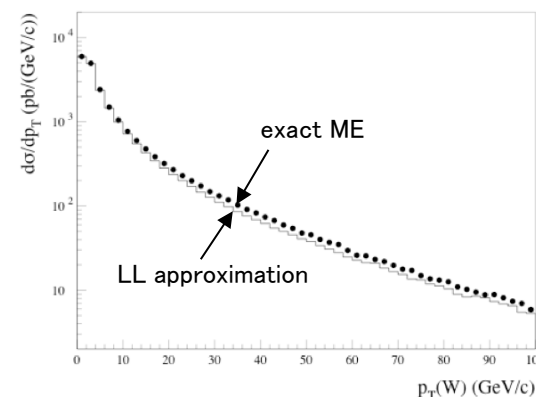
PS regularizes the divergence as an effect of multiple radiation.

→ Everything is finite after the subtraction.

The subtracted cross section may become negative, but it is not a serious problem unless the fraction becomes large.

$W + 1 \text{ jet @LHC}$

$p_T > 1 \text{ GeV}/c$ for numerical stability



Limited

PS implementation is limited by a certain energy scale (μ_{PS}).

→ Subtraction should also be **limited by μ_{PS}** .

Identity between PS and PDF.

→ $\mu_{\text{PS}} = \mu_F$ (factorization scale)

⇒ **Limited Leading-log (LLL) subtraction**

Y. Kurihara et al., Nucl. Phys. B654 (2003) 301; hep-ph/0212216

S. Odaka and Y. Kurihara, Eur. Phys. J. C 51 (2007) 867; hep-ph/0702138

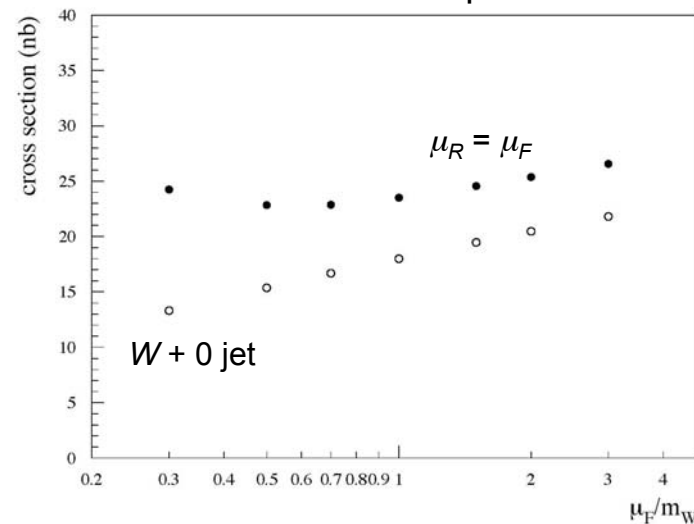
W production @LHC

“*W* + 0 jet” + “*W* + 1 jet”
with LLL subtraction

Good stability against the
variation of the factorization
scale

Showing a good matching between
ME and PDF

Factorization-scale dependence



Parton showers

The matching between the radiation factor and PS is crucial.

→ custom-made PS (**QCDPS**)

A forward-evolution PS in the initial state (space-like)

Based on a primitive definition of the Sudakov form factor at the leading order (LO)

An x -deterministic evolution technique to overcome the low-efficiency problem

Equivalent to the QCD evolution in LO PDFs

Y. Kurihara et al., Nucl. Phys. B654 (2003) 301; hep-ph/0212216

An appropriate definition of the **branch kinematics (model)** is crucial to achieve a good matching in transverse activities; *e.g.*, recoil p_T .

⇒ p_T -prefixed branch kinematics

S. Odaka and Y. Kurihara, Eur. Phys. J. C 51 (2007) 867; hep-ph/0702138

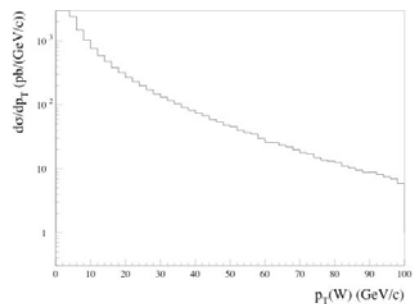
S. Odaka, arXiv:0907.5056; to be published in Mod. Phys. Lett. A

We have also developed a backward-evolution PS with the same kinematics model (QCDPSb), and a PS for the final state (QCDPSf) for consistency.

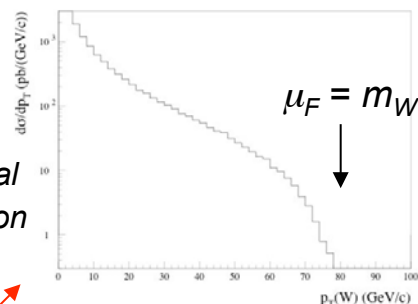
Concept of NLO event generation

p_T spectrum of W bosons as a sample

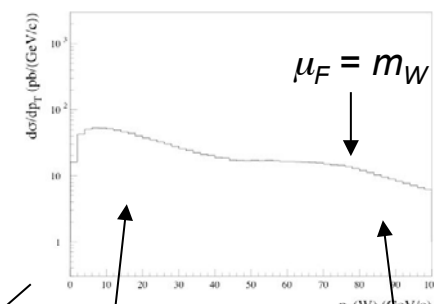
Radiation by $W + 1$ jet ME



LLL (Limited Leading-Log) terms



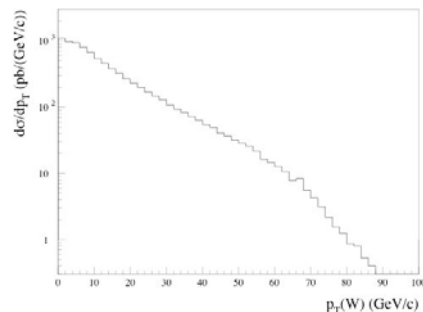
LLL-subtracted $W + 1$ jet ME



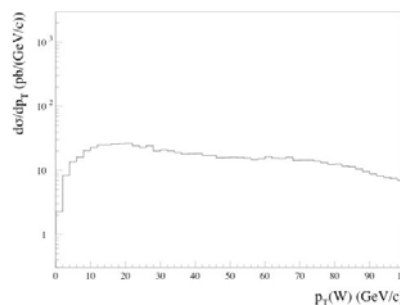
numerical subtraction

matching

Non-rad. \otimes PS
(Born + virtual/soft/collinear corr.) \otimes LLL



+



\otimes PS

Non-LL

Non-LL +
hard LL

*NLO event
generator
with PS*

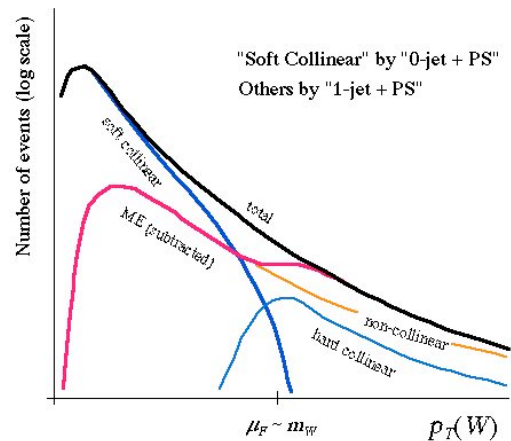
GR@PPA new version

Implementation of the matching method and PS
for single and double weak-boson productions

⇒ GR@PPA 2.8

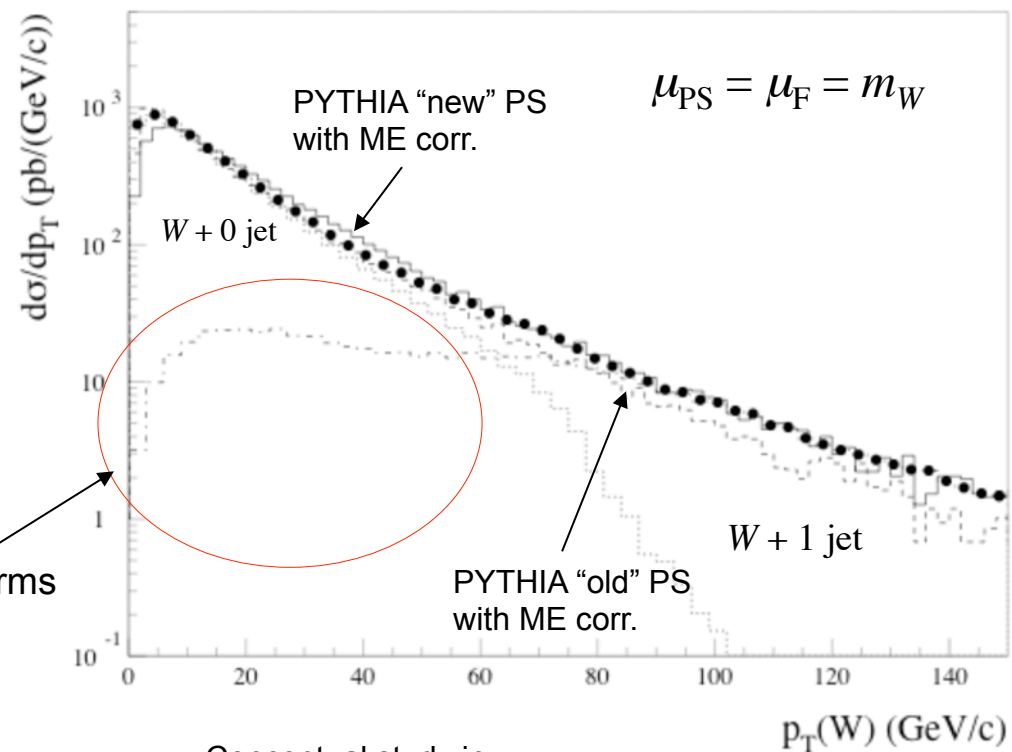
MEs in GR@PPA are still at the tree level;
i.e., no virtual corrections.

W production @LHC



My prospect at PhysSim WS
at KEK in 2004

Non-collinear terms



Conceptual study in

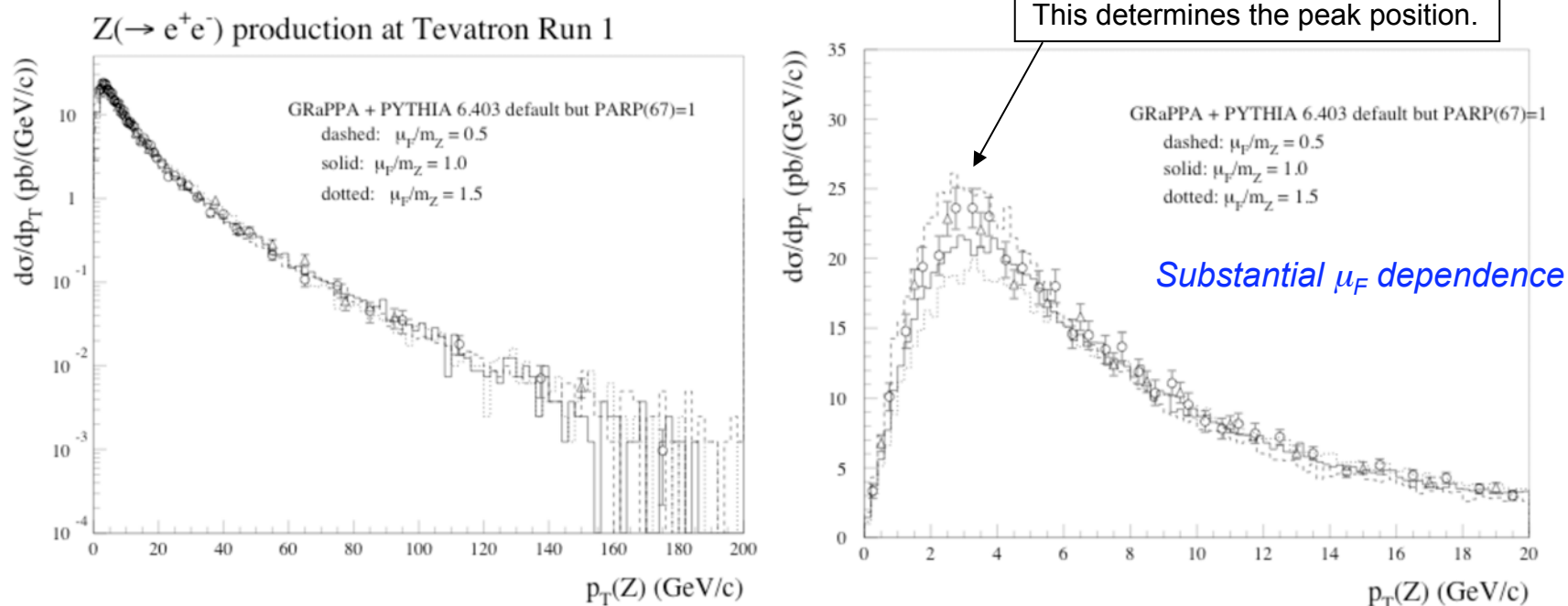
S. Odaka and Y. Kurihara, Eur. Phys. J. C 51 (2007) 867; hep-ph/0702138

Low- Q simulations by PYTHIA/HERWIG are yet to be applied.

Z production at Tevatron

GR@PPA 2.8 + PYTHIA 6.4

PYTHIA for simulating soft PS ($1.0 < Q < 4.6$ GeV), **primordial k_T** ($\langle k_T \rangle = 2.0$ GeV/c), hadronization, and decays



Circles: CDF, Phys. Rev. Lett. 84, 845 (2000)

Triangles: D0, Phys. Rev. D 61, 032004 (2000) $\times 1.12$

D0 data and simulations are normalized to the total cross section of CDF.

Nearly perfect through the entire measurement range

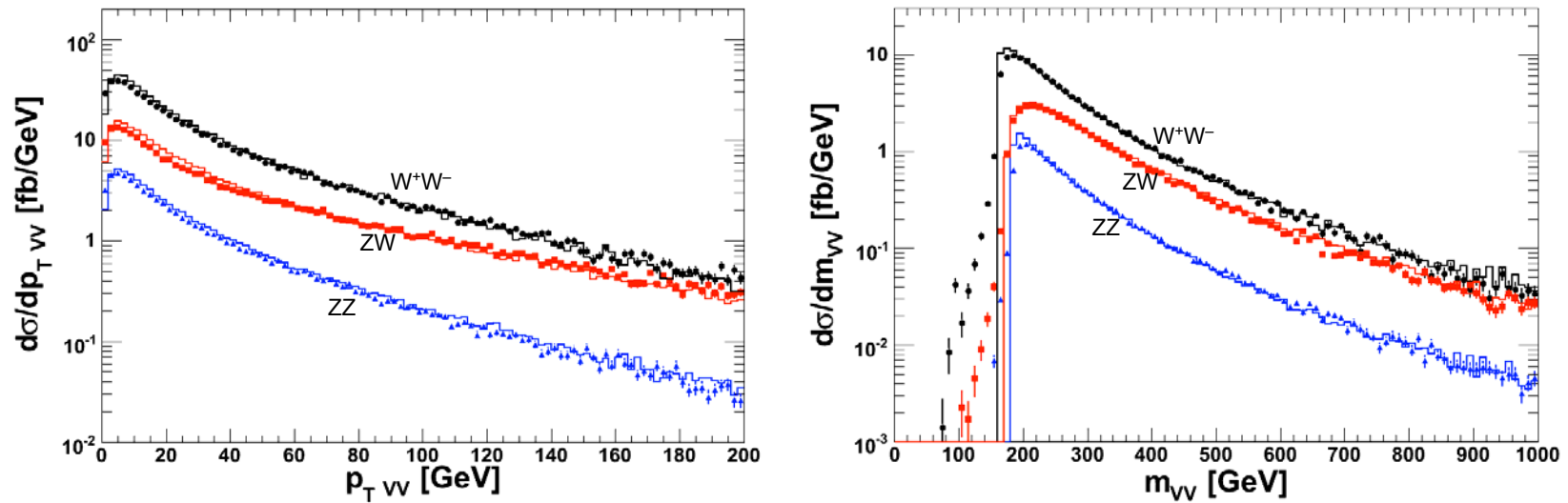
No tunable parameter in GR@PPA

Diboson (double weak-boson) production @LHC

Comparison with MC@NLO

Plots: GR@PPA 2.8 + Pythia 6.4

Histograms : MC@NLO3.31+Herwig6.510.3+Jimmy4.31.3



Reasonable agreement

GR@PPA is yet to be at NLO.

Zero decay widths in these MC@NLO simulations.

Summary

- NLO Working Group at KEK
 - Established in 2000,
 - Aiming at developing NLO event generators for multi-particle production processes at hadron collisions based on GRACE.
 - GR@PPA event generators have been developed in order to establish a framework of the event generation.
 - GR@PPA is still at the tree level, but supporting many multi-particle production processes.
- GR@PPA 2.8 is almost ready to release;
 - Implementing an initial-state jet matching (ME-PS matching) for single W and Z productions and diboson (W^+W^- , ZW and ZZ) productions,
 - Including a forward-evolution PS and a backward-evolution PS for the initial state, as well as a PS for the final state.
 - The simulation surprisingly well reproduces the Z-boson p_T spectrum measured at Tevatron.
 - An important step towards NLO event generators

Next

Jet matching in γ production processes

QED final-state matching together with QCD

⇒ GR@PPA 2.9 ?

NLO event generator

Consistent application of virtual corrections to
non-radiative processes

⇒ GR@PPA 3.x ?

Further automatization

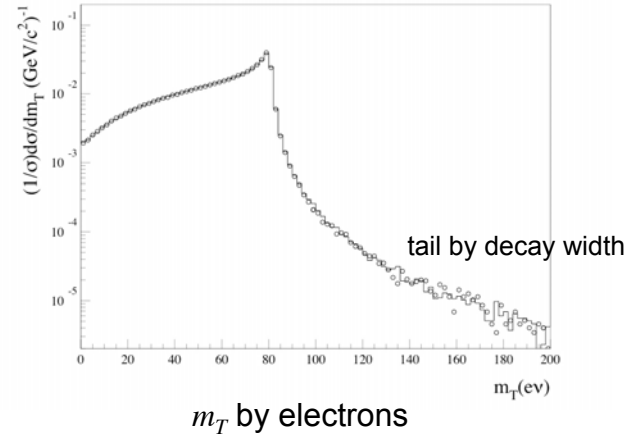
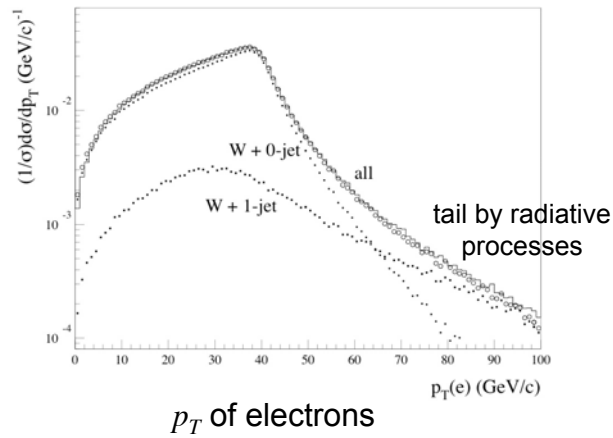
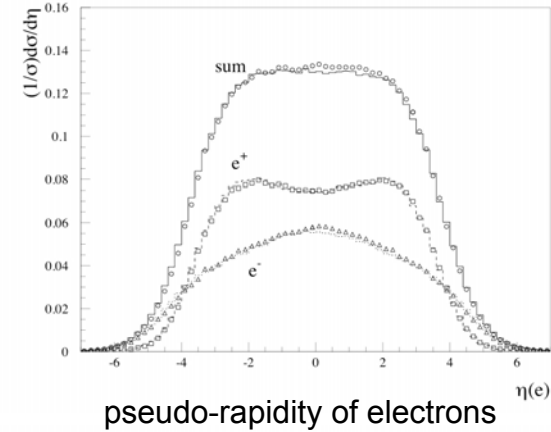
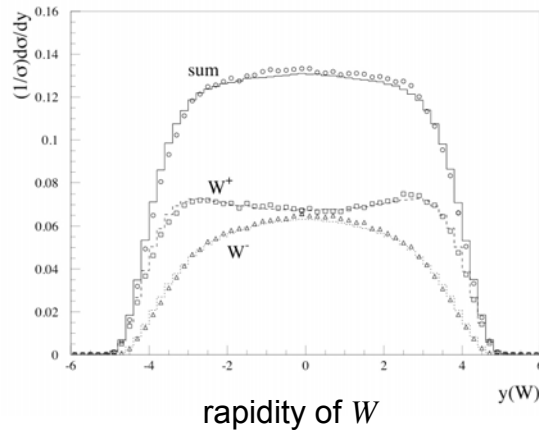
To reduce mistakes in the coding

⇒ GR@PPA 4.x ?

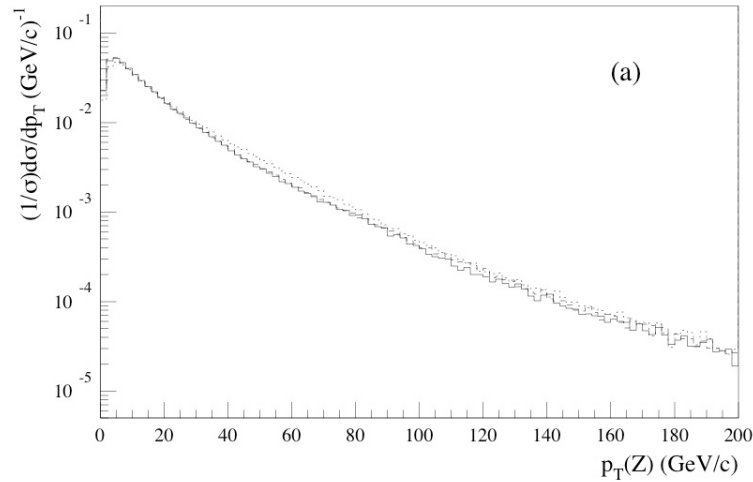
W production @LHC

Comparison with PYTHIA

Plots: GR@PPA, Histograms: PYTHIA



Z production @LHC



Solid: GR@PPA 2.8 + PYTHIA 6.421

Dashed: PYTHIA 6.421 built-in with new PS

Dotted: HERWIG 6.510

We will be able to plot measurement results soon.

